

# High-resolution Computed Muon Tomography

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# Outline

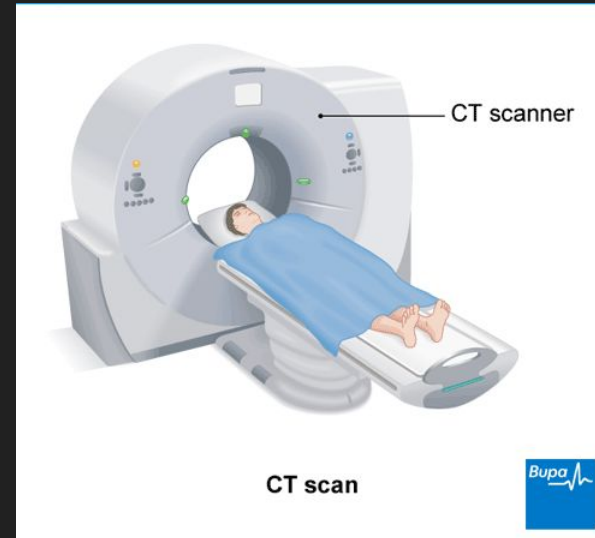
1. What is computed tomography?
2. Why muon tomography
3. Advantage of using muon beams
4. Potential applications

# What is Computed Tomography

Tomography : image by section

Computed Tomography : application of computer in obtaining a cross section image.

CT-scan : using X-ray for medical imaging and diagnostics

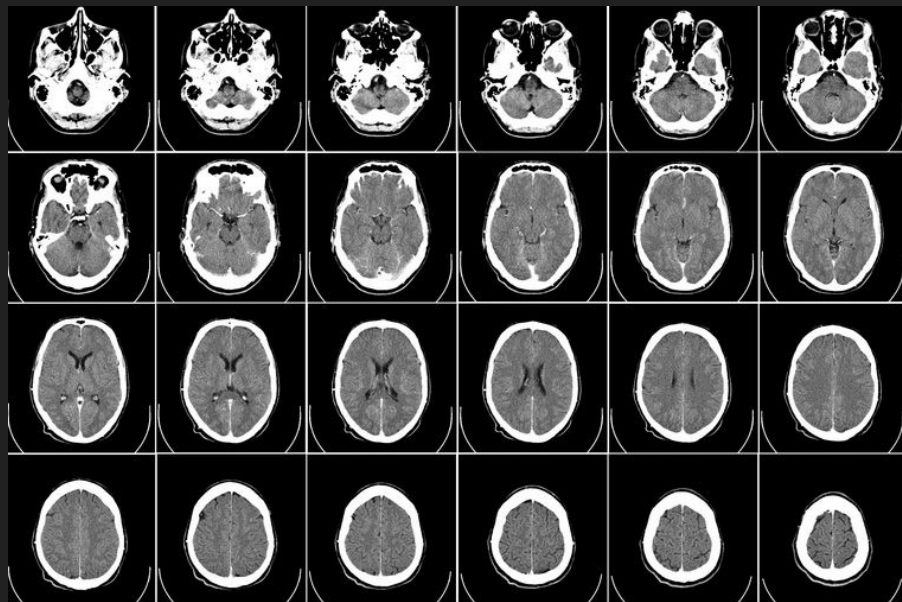


# What is Computed Tomography

X-ray scan: only projection



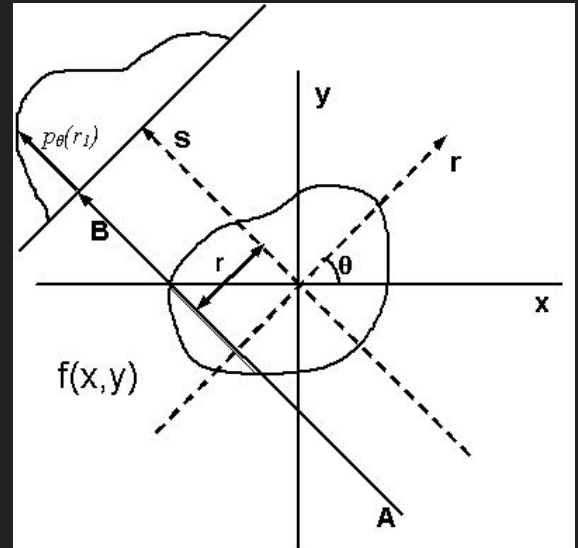
CT: 3D reconstruction



# Tomographic Reconstruction

Mathematically: given a 2D scalar function (e.g. density), if it's integral projection (e.g. intensity loss in X-ray) is known at every direction, is it possible to find out the original scalar function.

Plainly: if you scan a suitcase in every orientation, can you find out the shape of the object.



# Tomographic Reconstruction

Answer is yes (obviously)

First introduced in 1917 by Johann Radon, known as Radon transform.

Later filtered back projection, iterative algorithm and many more proprietary algorithms

- Better algorithm means better precision at lower dosage

# e.g. Filtered Backprojection

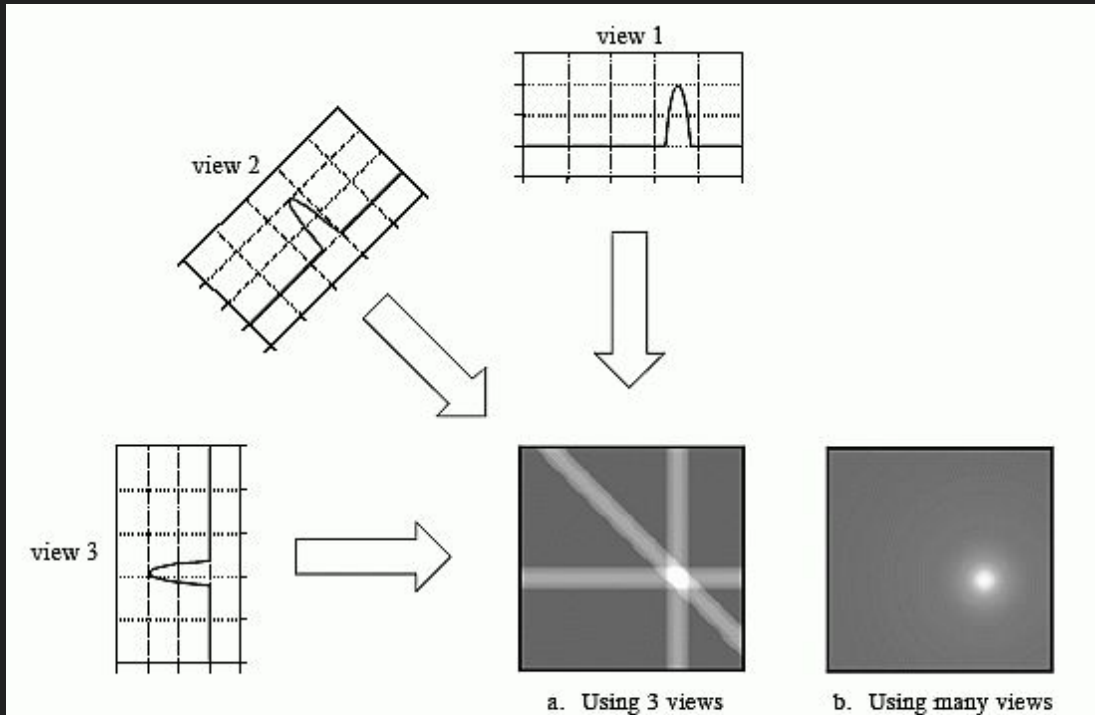
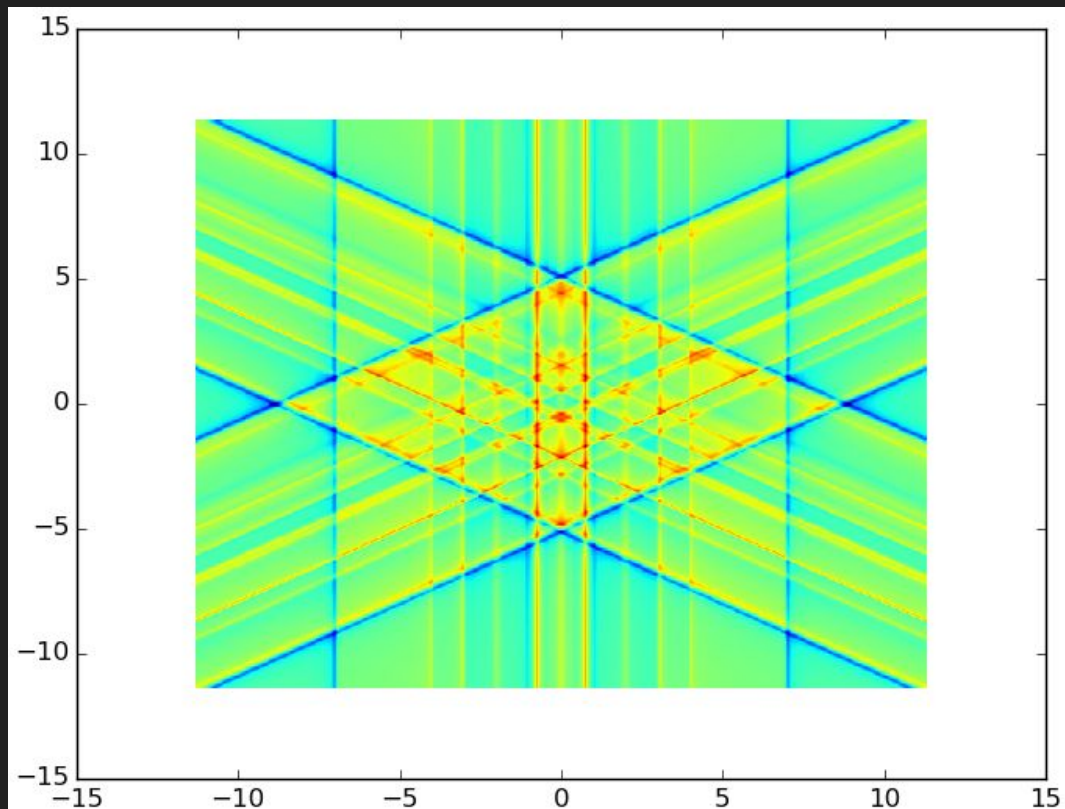


FIGURE 25-16

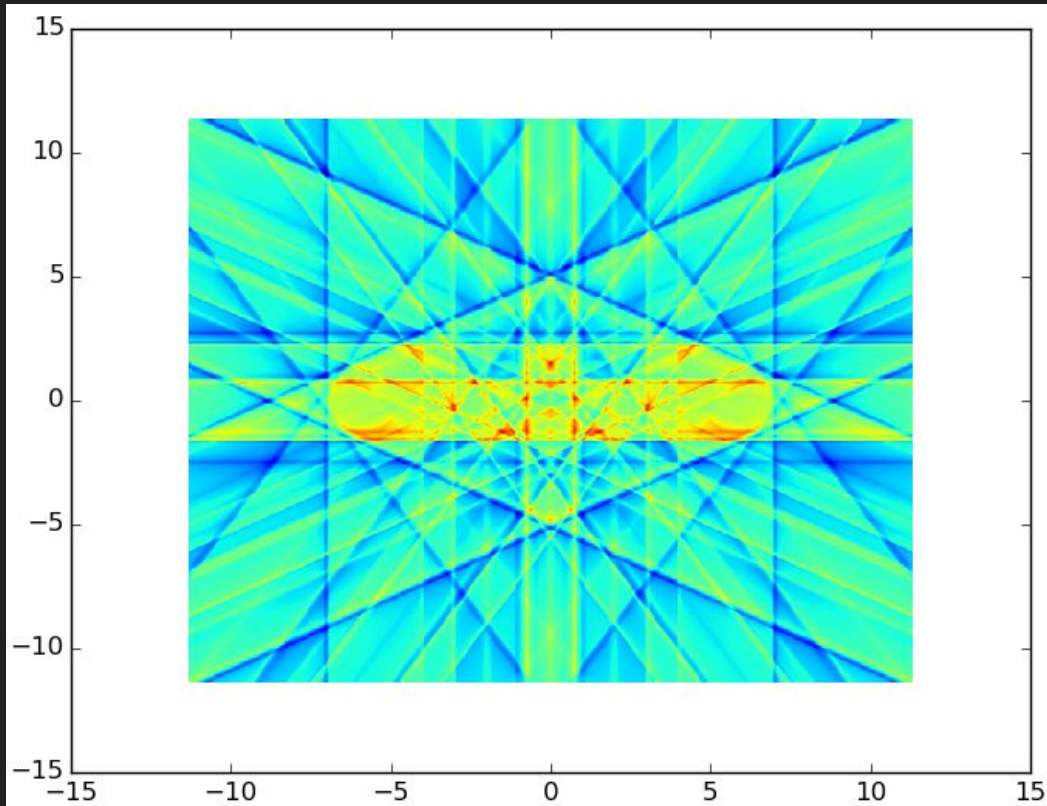
Backprojection. Backprojection reconstructs an image by taking each view and *smearing* it along the path it was originally acquired. The resulting image is a blurry version of the correct image.

# FBP in action - 3 back projections

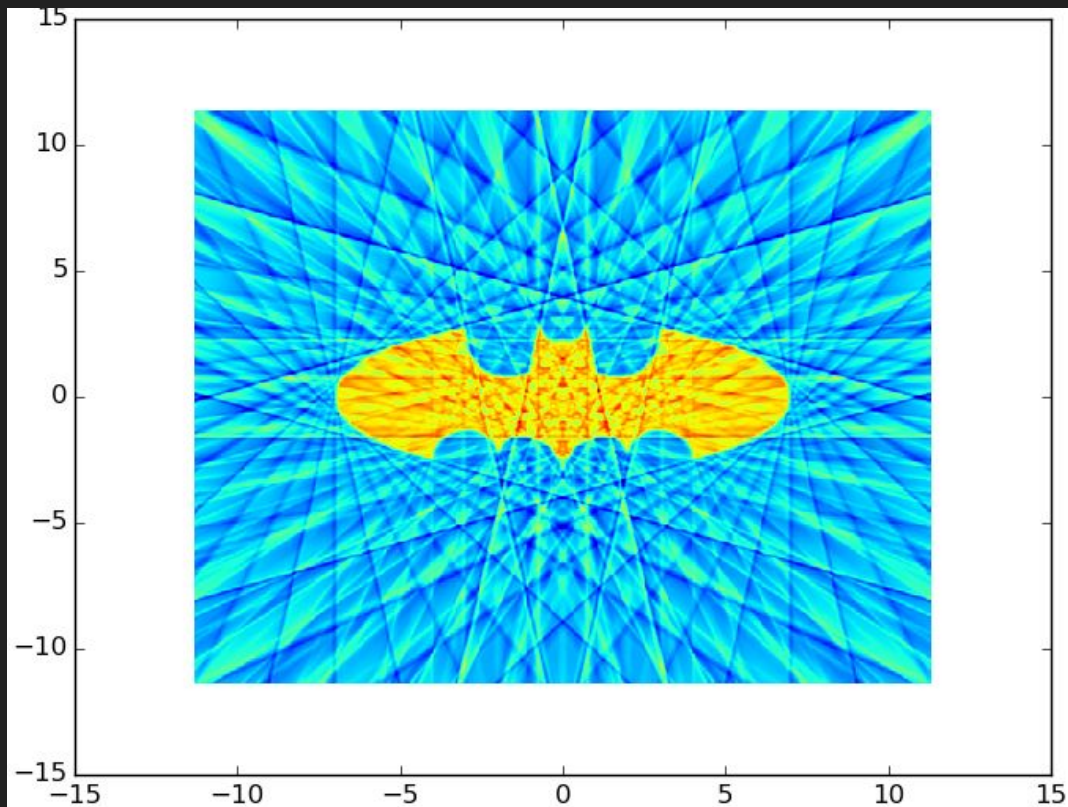




# FBP in action - 6 back projections



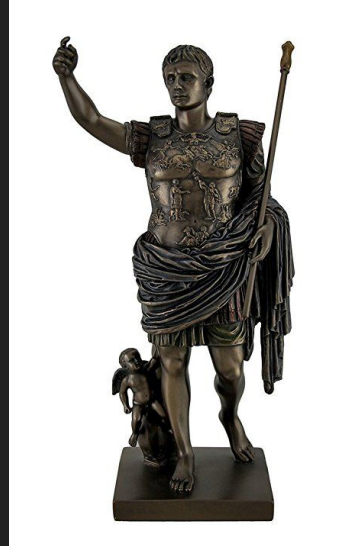
# FBP in action - 18 back projections



# Initial Motivation for Muon Tomography

100 keV X-ray: attenuation coefficient  $\sim 3.5 / \text{cm}$

- After 2 cm of Cu, intensity is 0.1%



# Why Muon Tomography

Muon is more penetrating than photons:

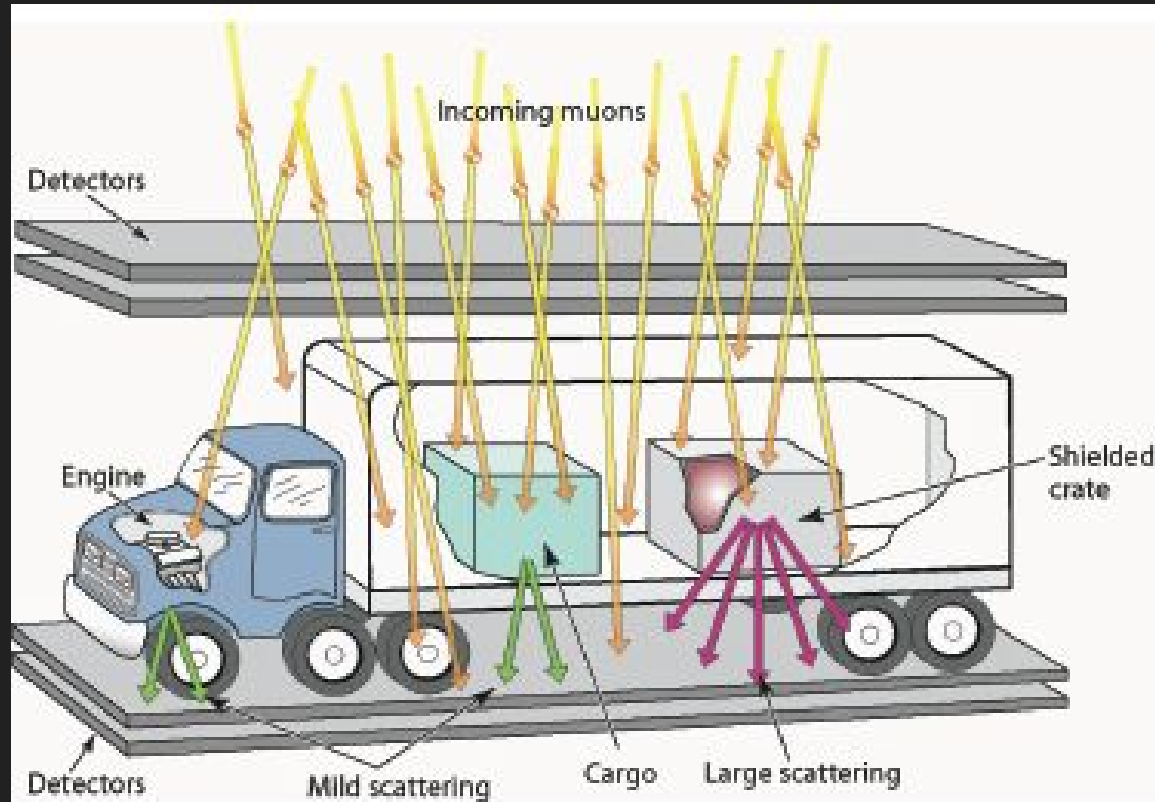
- Muons lose roughly 2 MeV per cm of water,
- 100 keV X-ray: attenuation coefficient  $\sim 3.5$  /cm
  - After 2 cm of Cu, intensity is 0.1%

Cosmic muon has been used to image Pyramids, volcanoes, nuclear reactors and cargos.

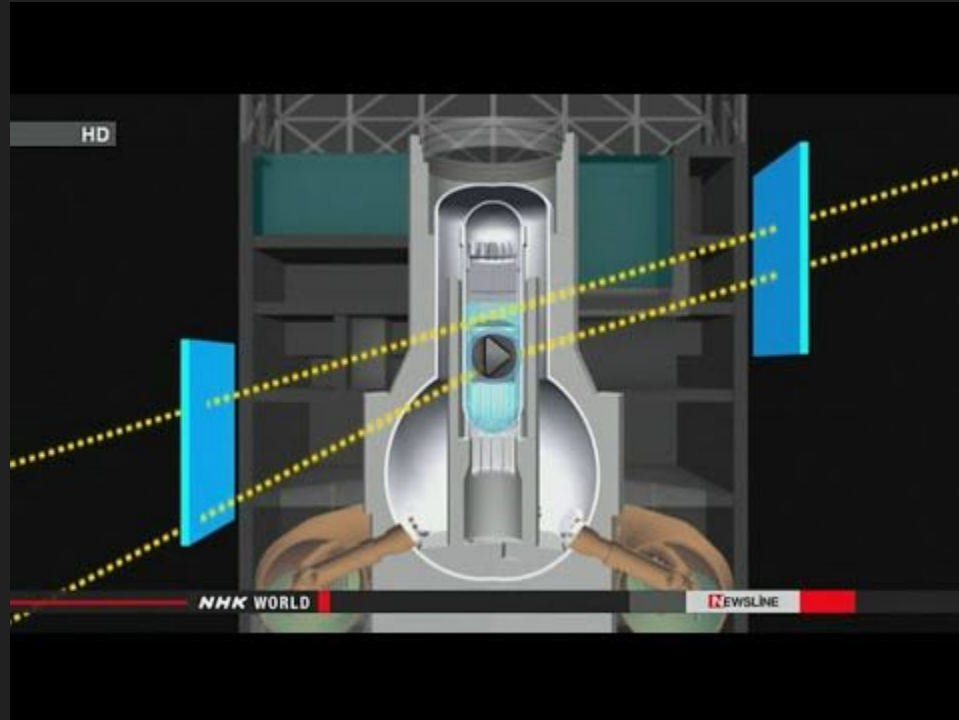
# Cosmic muon helps find hidden chamber



# Cosmic muon helps find nuclear material



# Cosmic muon can help see the core of Fukushima



## Limitation of using cosmic muons

On the surface, roughly 1 muon per  $\text{cm}^2$  per second

Can wait for months before hidden chamber is found

Better not wait for too long to scan a cargo, or to find out what is happening to a reactor.



Using muons from accelerator beams

Control over energy and flux; faster imaging.

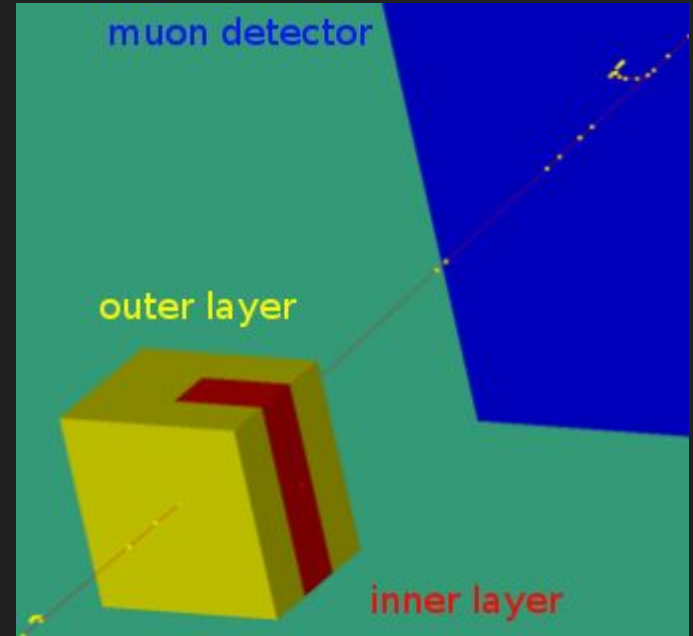
More expensive, not available everywhere, special facility needed.

# Simulation Setup

“Sandwiched geometry”

A different material is sandwiched inside one material.

Monoenergetic muon beam and a Muon detector is used to measure energy loss as function of XY



# Modulation transfer coefficient

Figure 1: Scan of an Edge

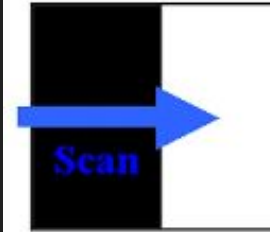


Figure 2: Edge Scan Function

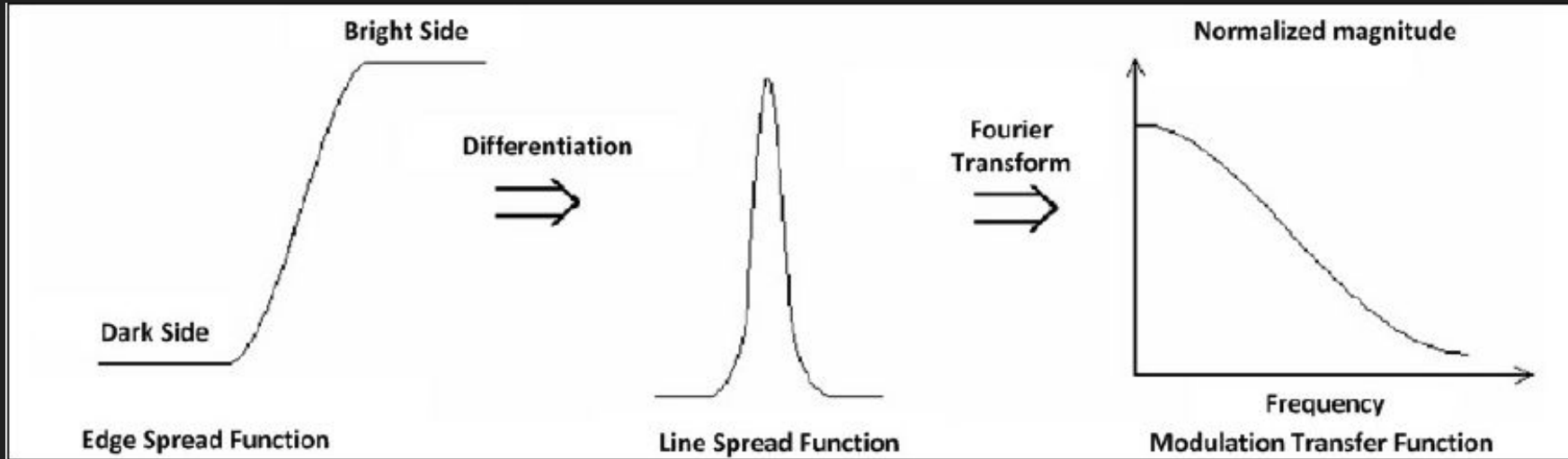
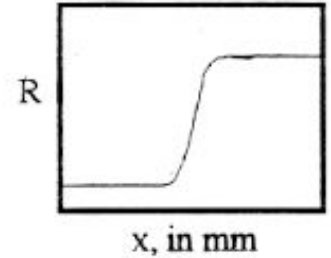
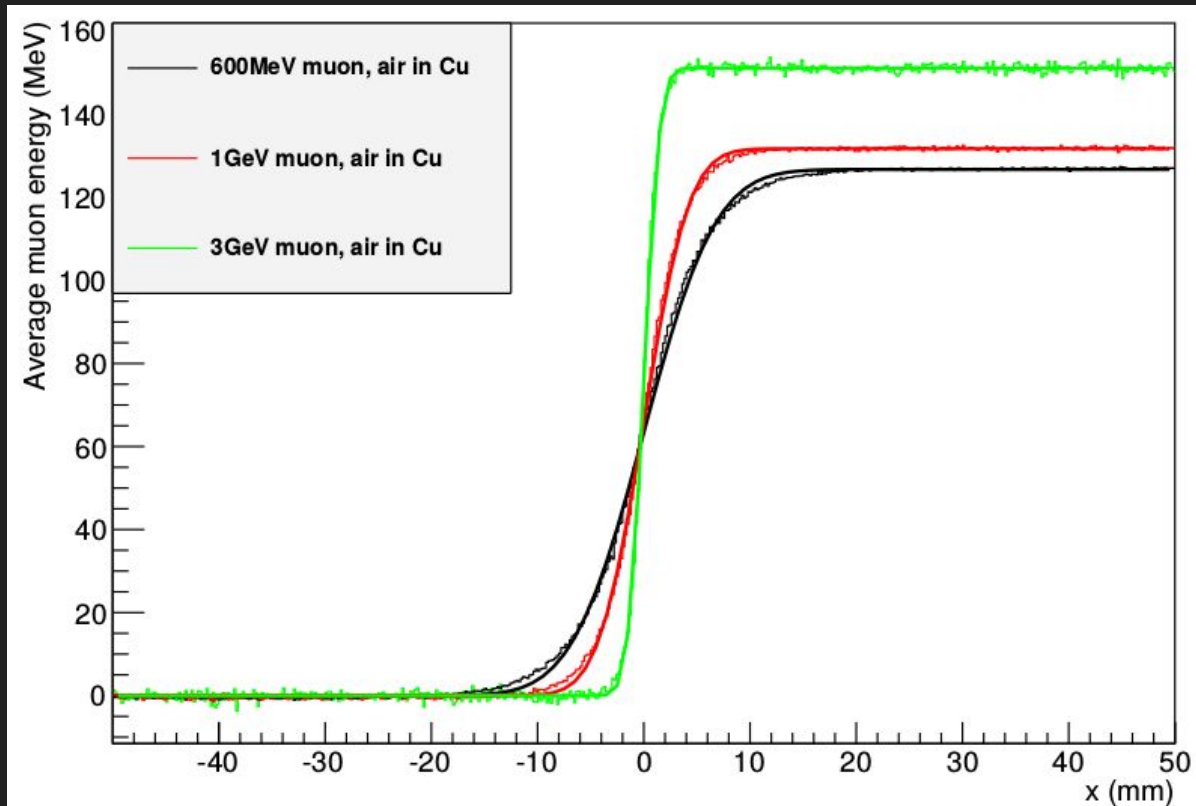
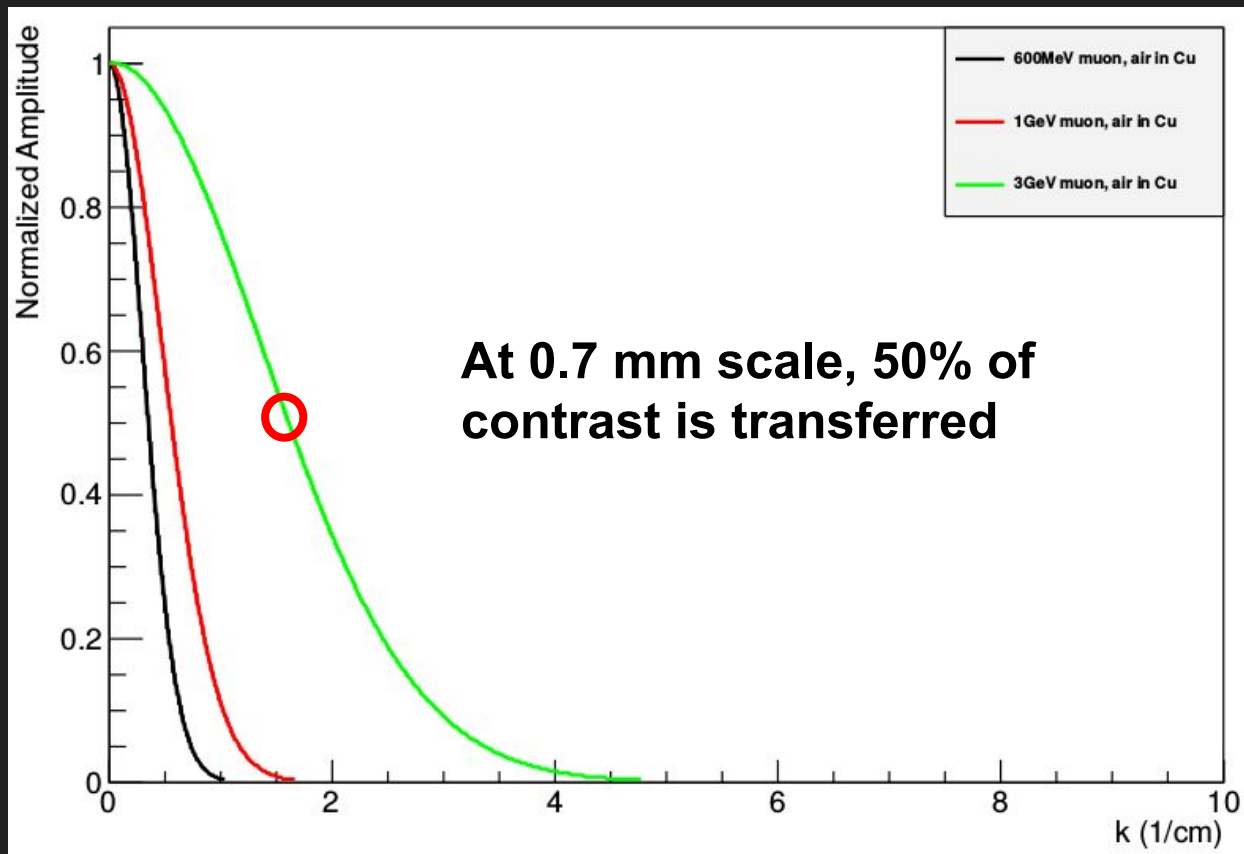


Figure 3. Computation of the Modulation Transfer Function using the knife-edge target.

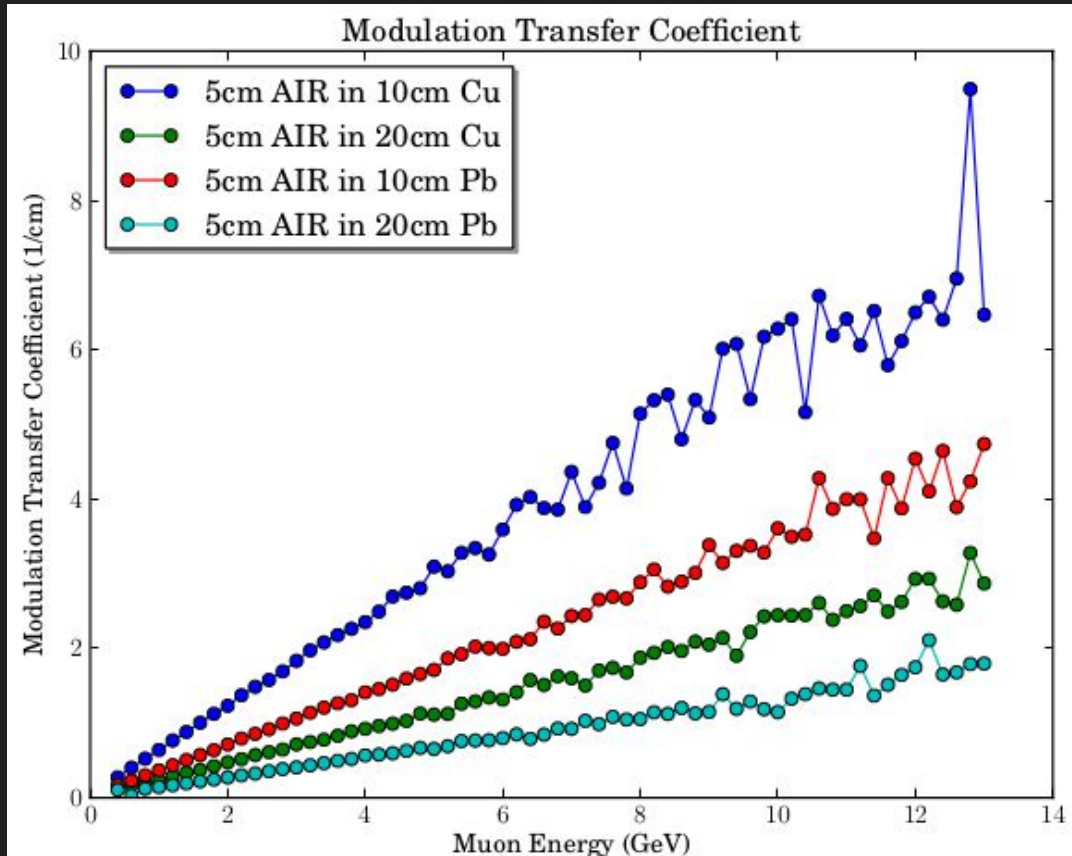
# Edge-spread function



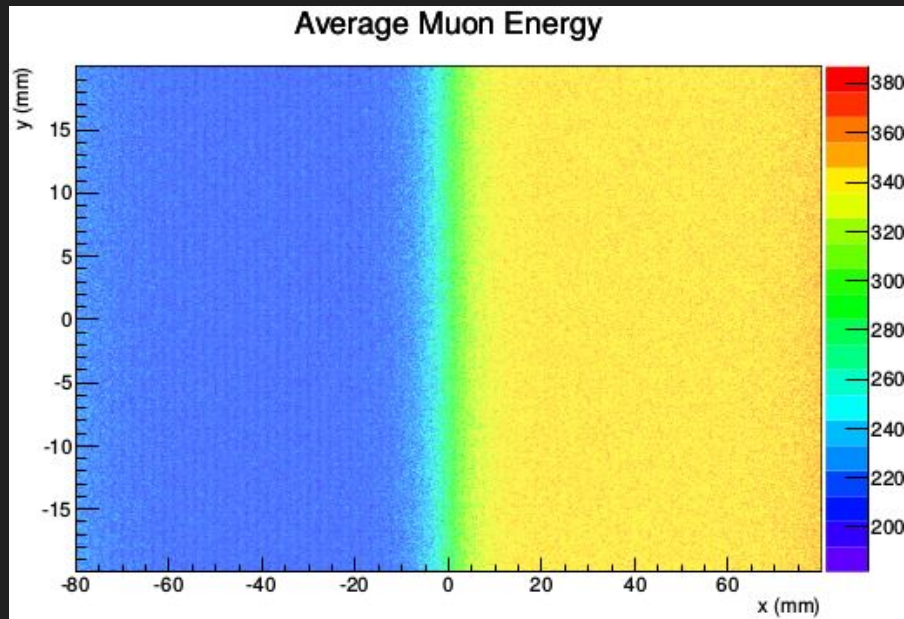
# Modulation-transfer function



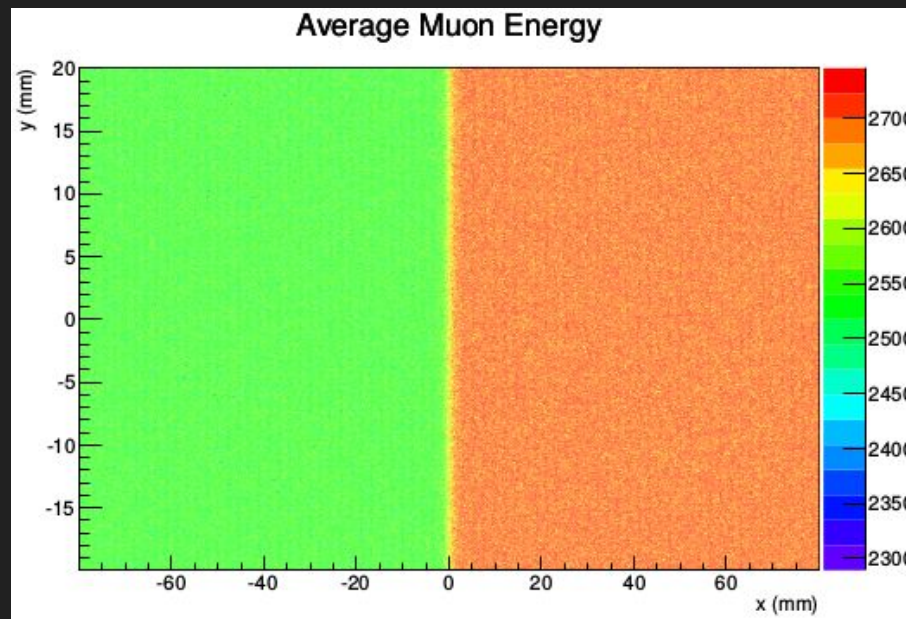
# Modulation transfer for different material and geometry



# The cost of increased resolution

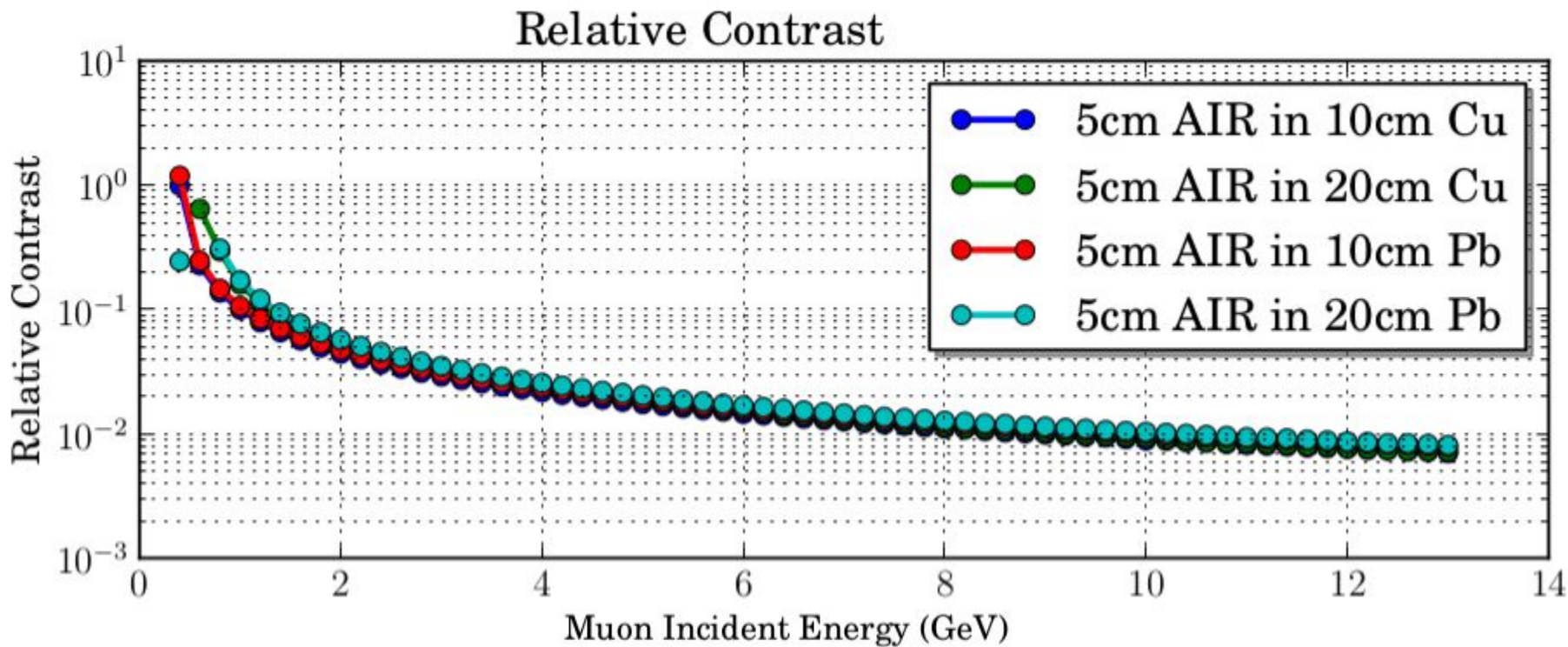


600 MeV



3 GeV

# The cost of increased resolution





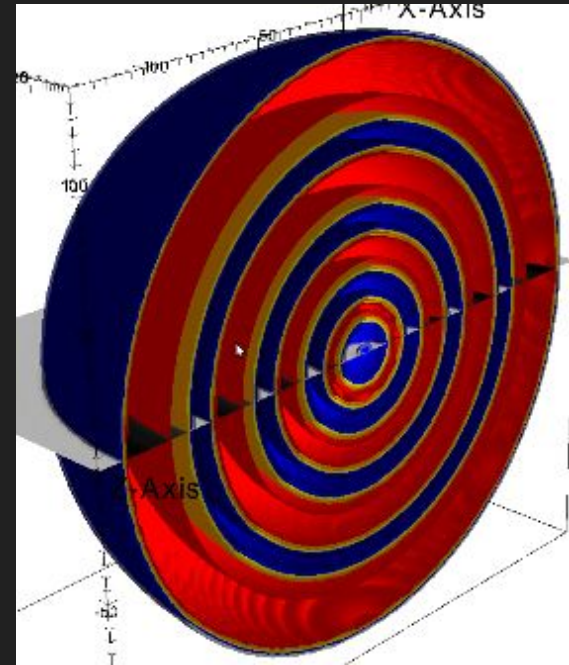
## A few comments:

1. Muon tomography will have more information than mean energy loss, e.g. scattering, calculation by Bethe-Bloch.
2. Multispectrum muon beam
  - a. Low energy for rough scan,
  - b. High energy for precision.

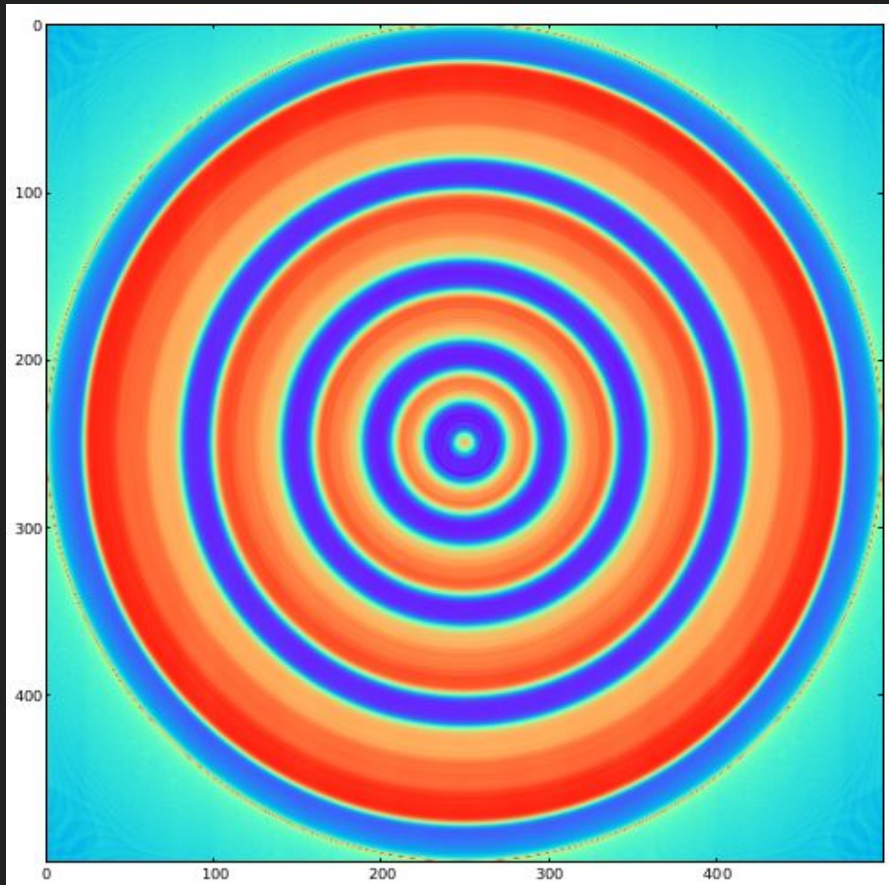
# Performance in tomographic reconstruction

## Test object:

- 5 layers of concentric spheres, thickness 3, 9, 15, 21, 30 mm
- Between each concentric sphere is 1 cm of water
- Each metallic layer is equal amount of copper, iron and lead



# Performance in tomographic reconstruction



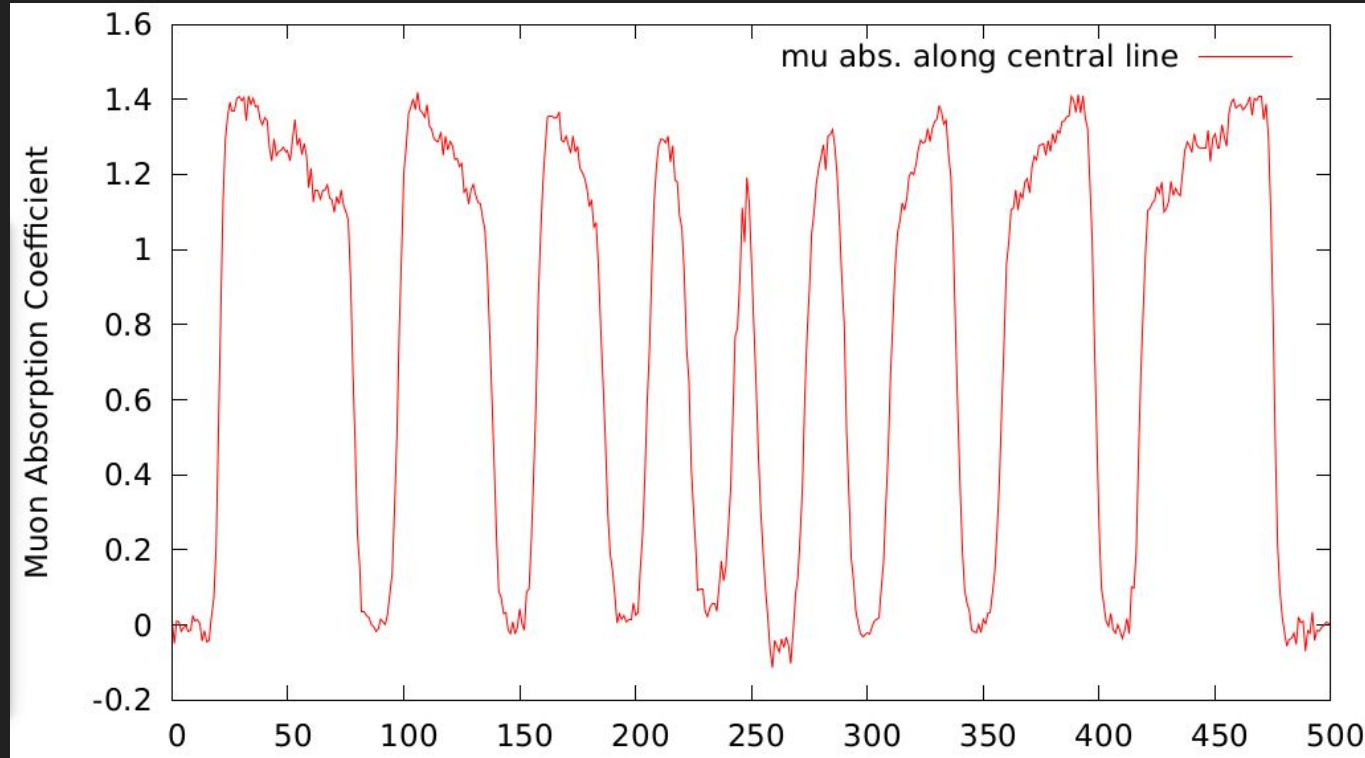
Density distribution  
reconstructed with FBP

Blue - water

In some of outer layers,  
different material  
density is clearly visible

# Performance in tomographic reconstruction

In outer layers, material density clearly visible



# Practical consideration:

1. Special muon beam would be ideal, but expensive too.
2. Muon neutrinos are produced by pion decay, with all muon dumped away

a.

$$E_\nu = \frac{m_\pi^2 - m_\mu^2}{2E_\pi - 2p_\pi \cos \theta}$$
$$\approx \frac{(1 - m_\mu^2/m_\pi^2)}{1 + \gamma^2 \theta^2} E_\pi. \text{ (small angle)}$$

- b. For NuMI beam in FermiLab, neutrino - 1~3 GeV, muon is 3 ~ 10 GeV.
- c.  $10^7 / \text{cm}^2$  over  $1 \text{ m}^2$  per spill over  $\sim 2 \text{ us}$ , need highly pixelated trackers operating at hundreds of MHz

# Future prospects:

1. A better reconstruction algorithm
2. Challenge is instrumental: required instruments exist
3. Interest in muon physics and neutrino physics
  - a.  $g-2$ , NOvA, future muon collider
4. Interest in archaeology, industry and border protection
  - a. Potential support from archaeologists in NY and DoE

# references

- [1] B. Suerfu and C. G. Tully, High resolution muon computed tomography at neutrino beam facilities, JINST 11 P02015, 2016
- [2] M. Slaney, et al., Principles of Computerized Tomographic Imaging.
- [3] M. Rossi, et al., Nuclear Science, IEEE Transactions on 46, 897 (1999).
- [4] L. W. Alvarez, et al., Science 167, 832 (1970),
- [5] H. K. Tanaka, et al., Earth and Planetary Science Letters 263, 104 (2007),
- [6] A. Anastasio, et al., Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment.
- [7] J. Chistiansen and M. Garcia-Sciveres, Tech. Rep., CERN-LHCC-2013-008.