

Calorimetry in the 21st century

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Decisions about the future require a good understanding of the past

Outline:

- *A brief history (50 years) of calorimetry*
- *Common misconceptions*
- *Options for the future*
- *Conclusions*

*Some milestones in the development of calorimetry
as an experimental technique
in nuclear, particle & astrophysics
in the past 50 years*

Milestones

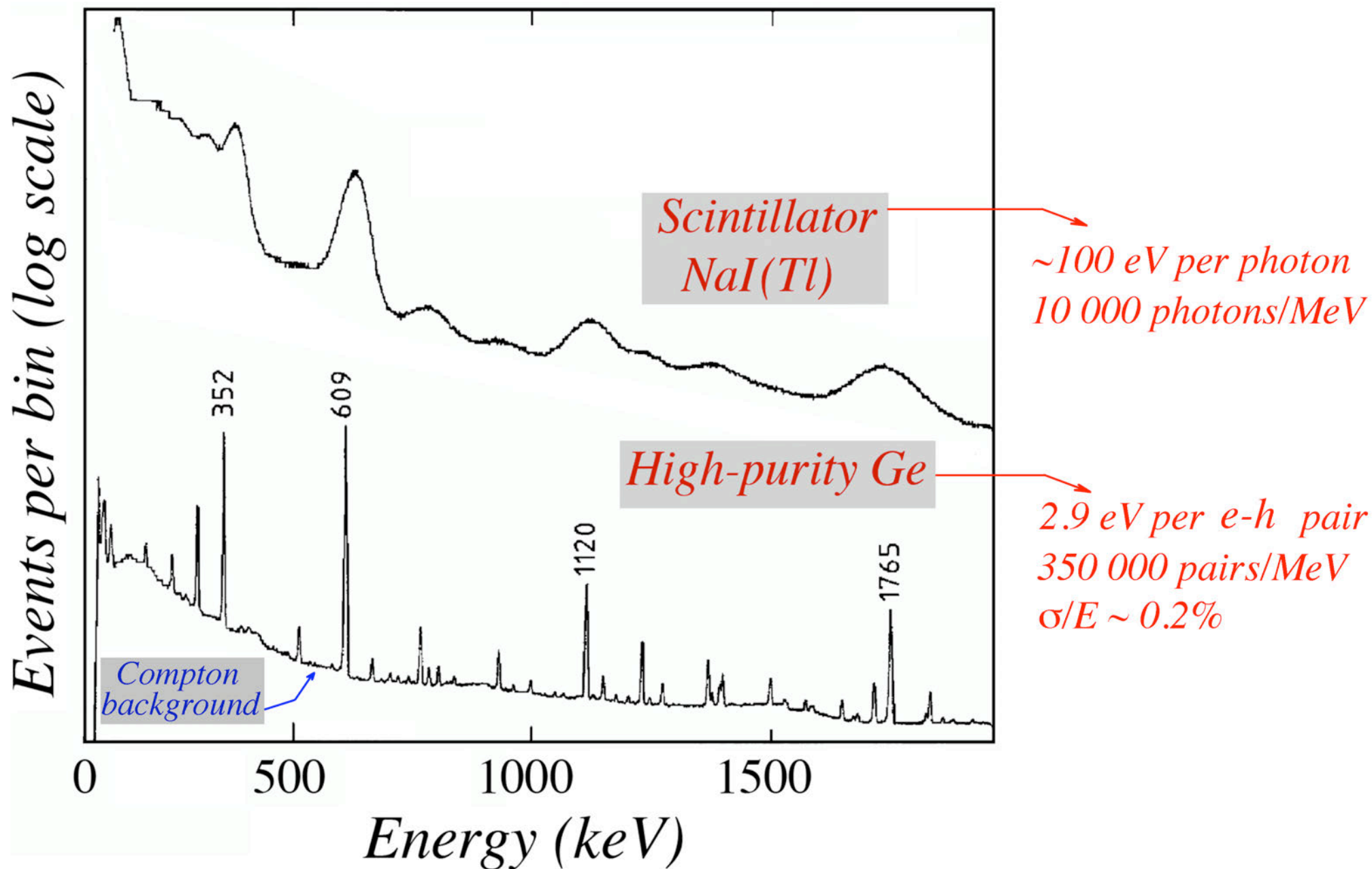
- 1965 - *Quantum leap in signal quanta (e-h pairs in semiconductors)*

Performance of calorimeters *improves with energy*
($\sim E^{-1/2}$ if statistical processes are the limiting factor)

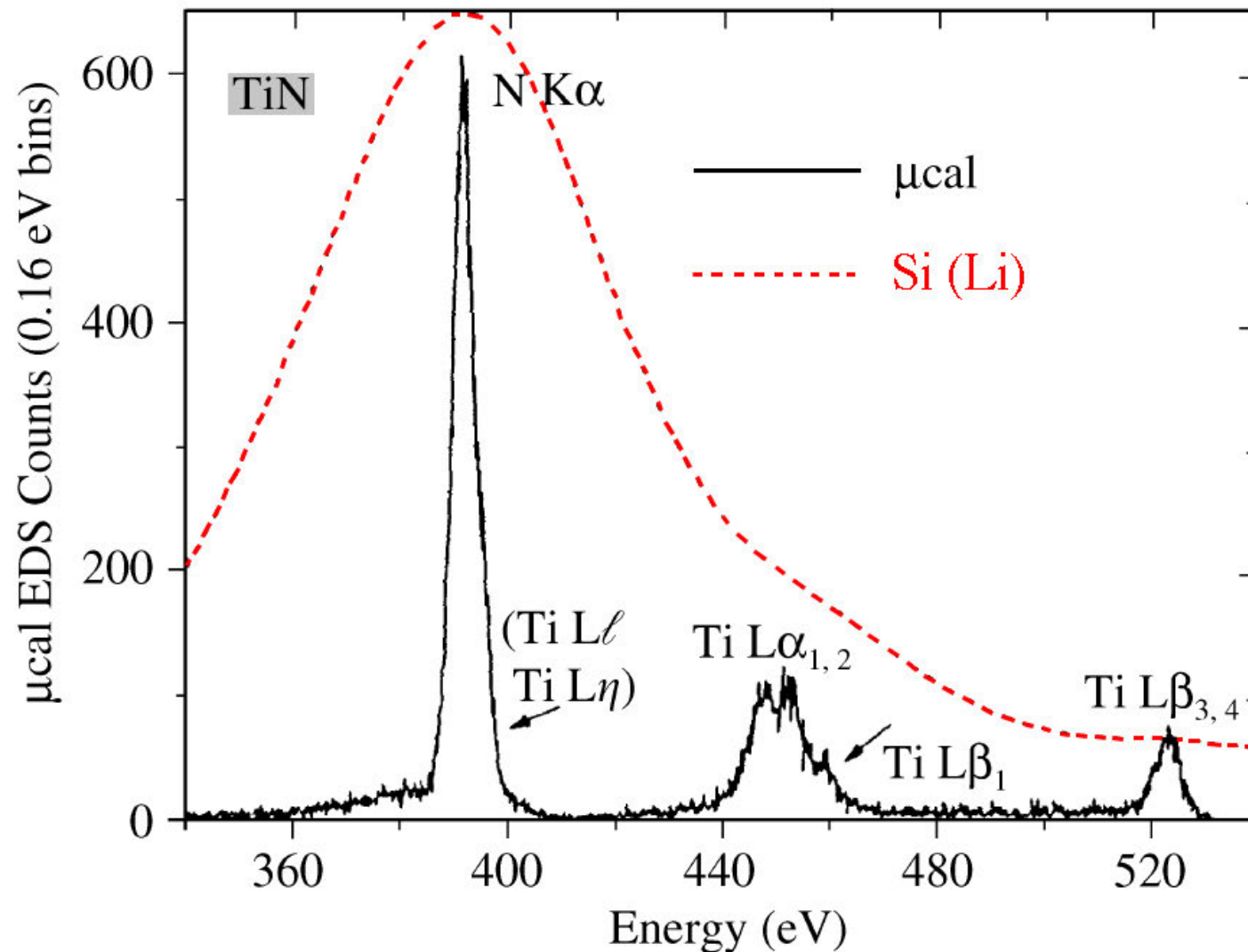
*If $E \propto \text{signal}$, i.e. $E \propto \# \text{ signal quanta } n \rightarrow \sigma(E) \propto \sqrt{n}$
 $\rightarrow \text{energy resolution } \frac{\sigma(E)}{E} \propto 1/\sqrt{n} \propto 1/\sqrt{E}$*

Nuclear γ ray detectors

Energy resolution dominated by signal quantum fluctuations (?)



*One can do even better in cryogenic calorimeters!
(binding energy Cooper pairs \sim meV)*



A brief history of calorimetry

(used as a particle detection technique)

- In the 1960s, particle physics started to make the transition from the bubble chamber era to experiments based on electronic counters*
- The detectors basically formed a magnetic spectrometer, in which all charged particles produced in reactions on a fixed target were analyzed:*
 - Momentum from effects Lorentz force*
 - Energy (mass) from time-of-flight or dE/dx*
- For the detection of the neutral reaction products (overwhelmingly γ s from π^0 decay), one used scintillating crystals, developed in the 1950s for nuclear spectroscopy, and called these “shower counters”*
- Using properly chosen materials (high Z !), even very-high-energy γ s can be fully absorbed in detectors of limited length (<30 cm), and be measured with spectacularly good energy resolution*

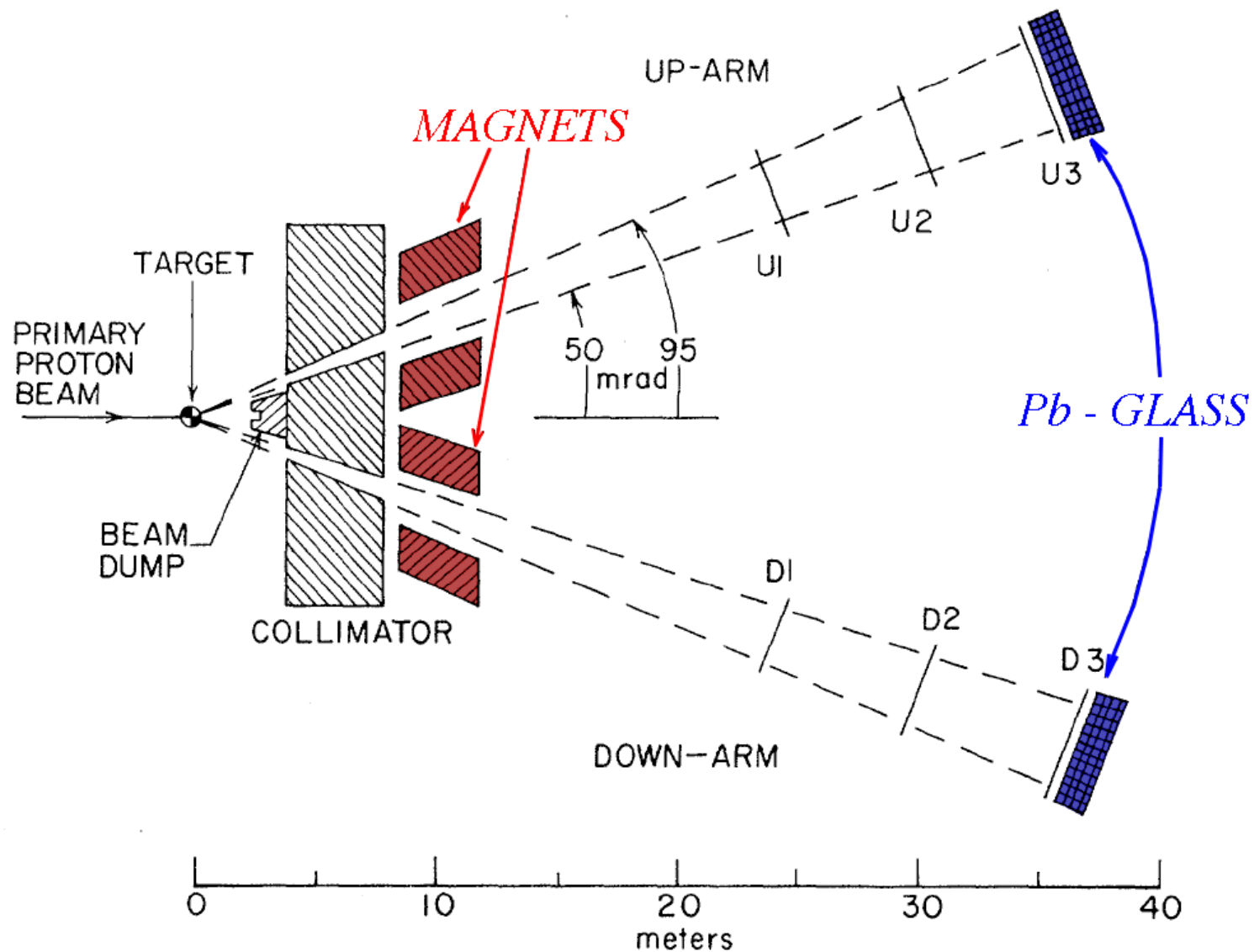
Milestones

- 1965 - *Quantum leap in signal quanta (e - h pairs in semiconductors)*
- 1970 - *Shower counters in HEP (crucial for discovery b -quark)*

1970s - Shower counters in magnetic spectrometers

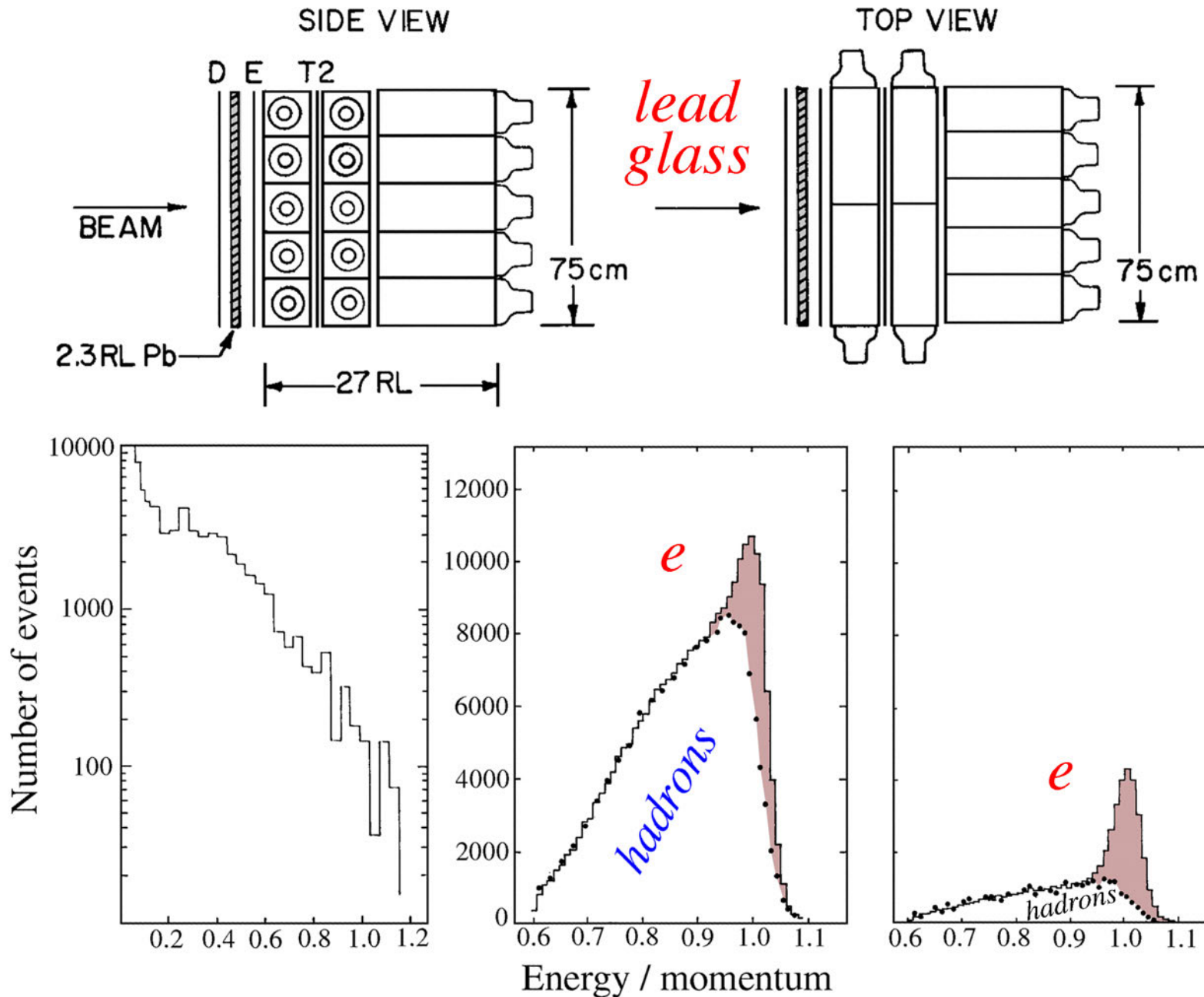
Example: E70 / 288 @ Fermilab

Discovered Upsilon $\rightarrow l^+ l^-$



Shower counters in the 1970s

(electron identification in a fixed-target experiment - NIM 127, 495)

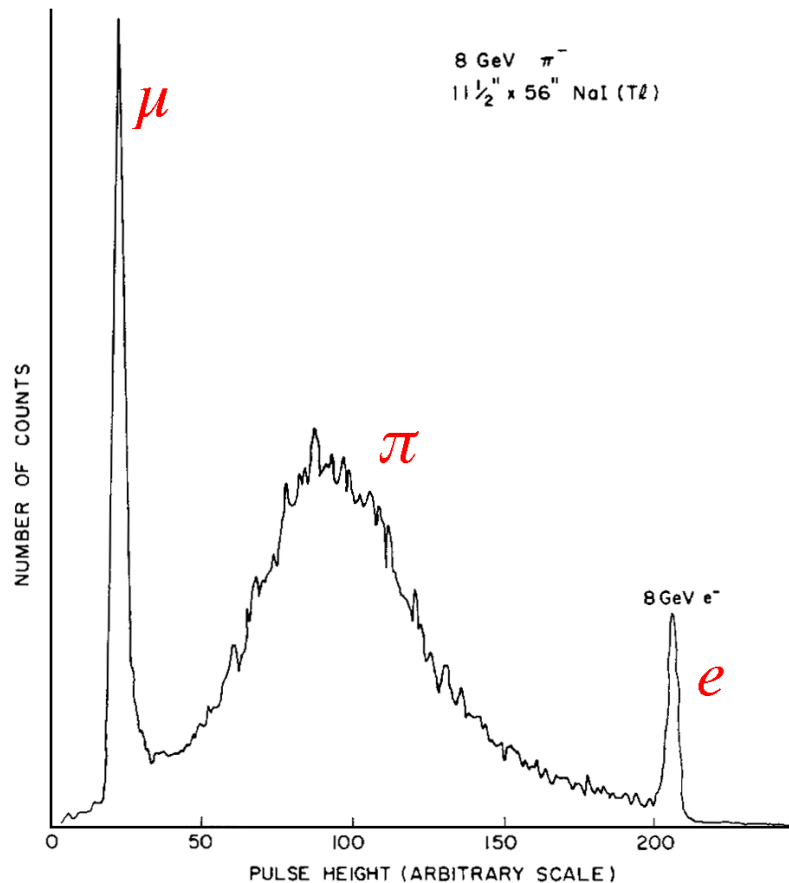


Early indication that hadron calorimetry is different!

NIM 75 (1969) 130

450 kg of NaI (Tl) crystals

Tested with 8 GeV particle beams



Conclusions of authors:

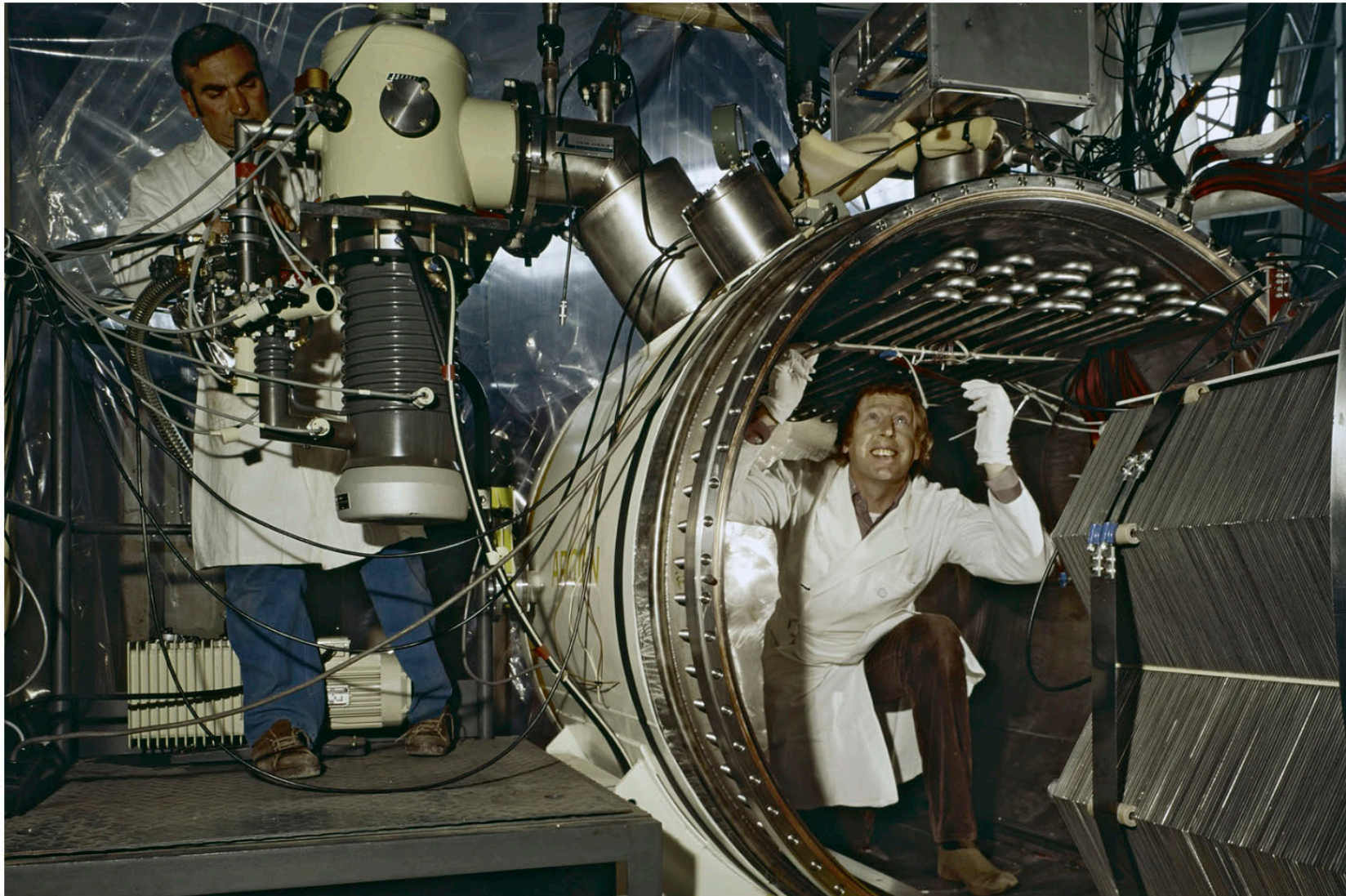
- *50% of energy leaks out*
- *MC: much less leakage*
- *Same results at 4, 12, 16 GeV*
- *Resolution did NOT improve with E*

Milestones

- 1965 - *Quantum leap in signal quanta (e-h pairs in semiconductors)*
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- 1974 - *Liquid argon calorimetry invented*

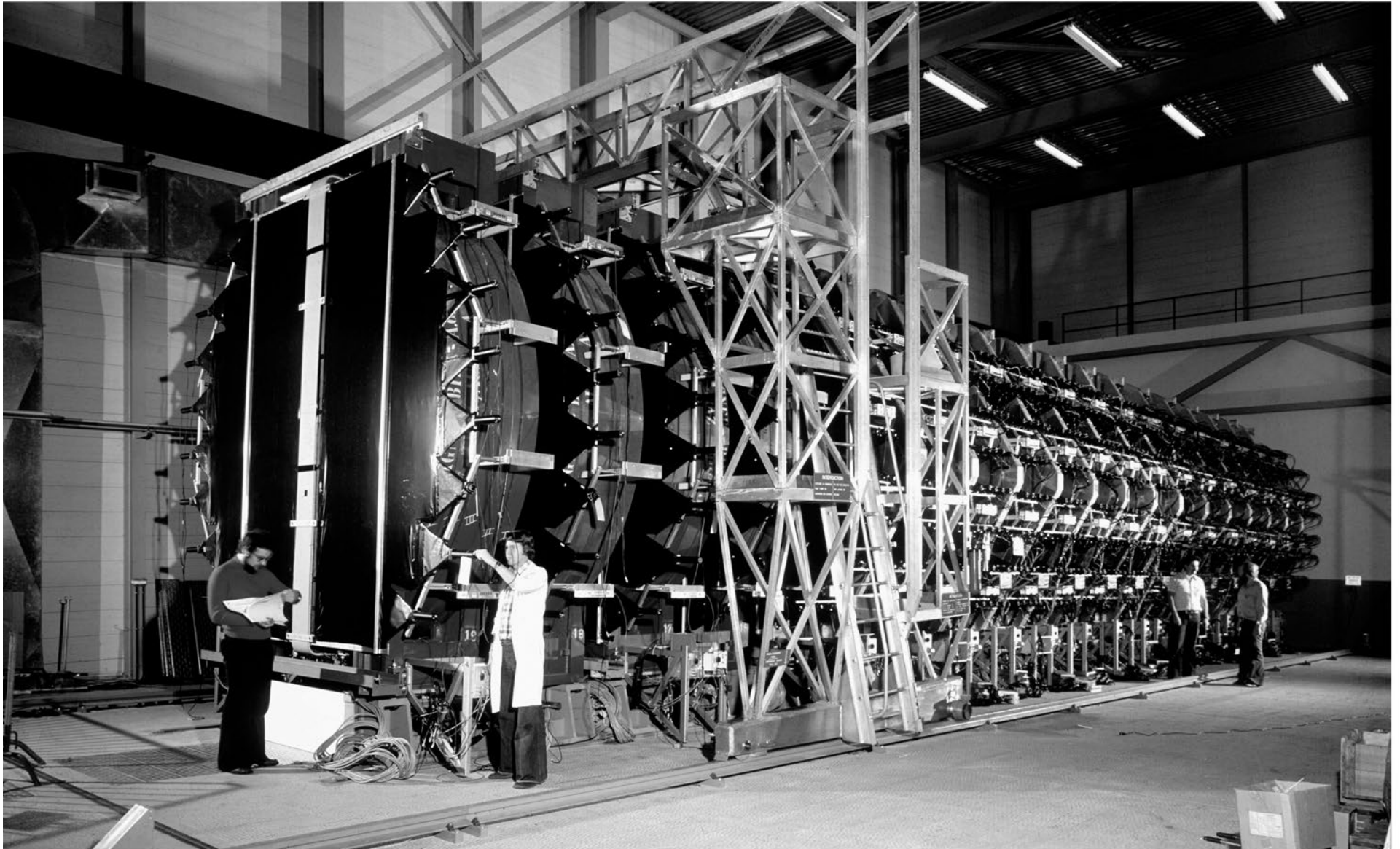
Willis/Radeka Lar calorimeter for an ISR experiment (1974)

*Direct collection of ionization charge
in a dense sampling medium*



*1975 - Calorimeters take on new tasks
(target, trigger counter, tracking, particle ID)*

WA1



Milestones

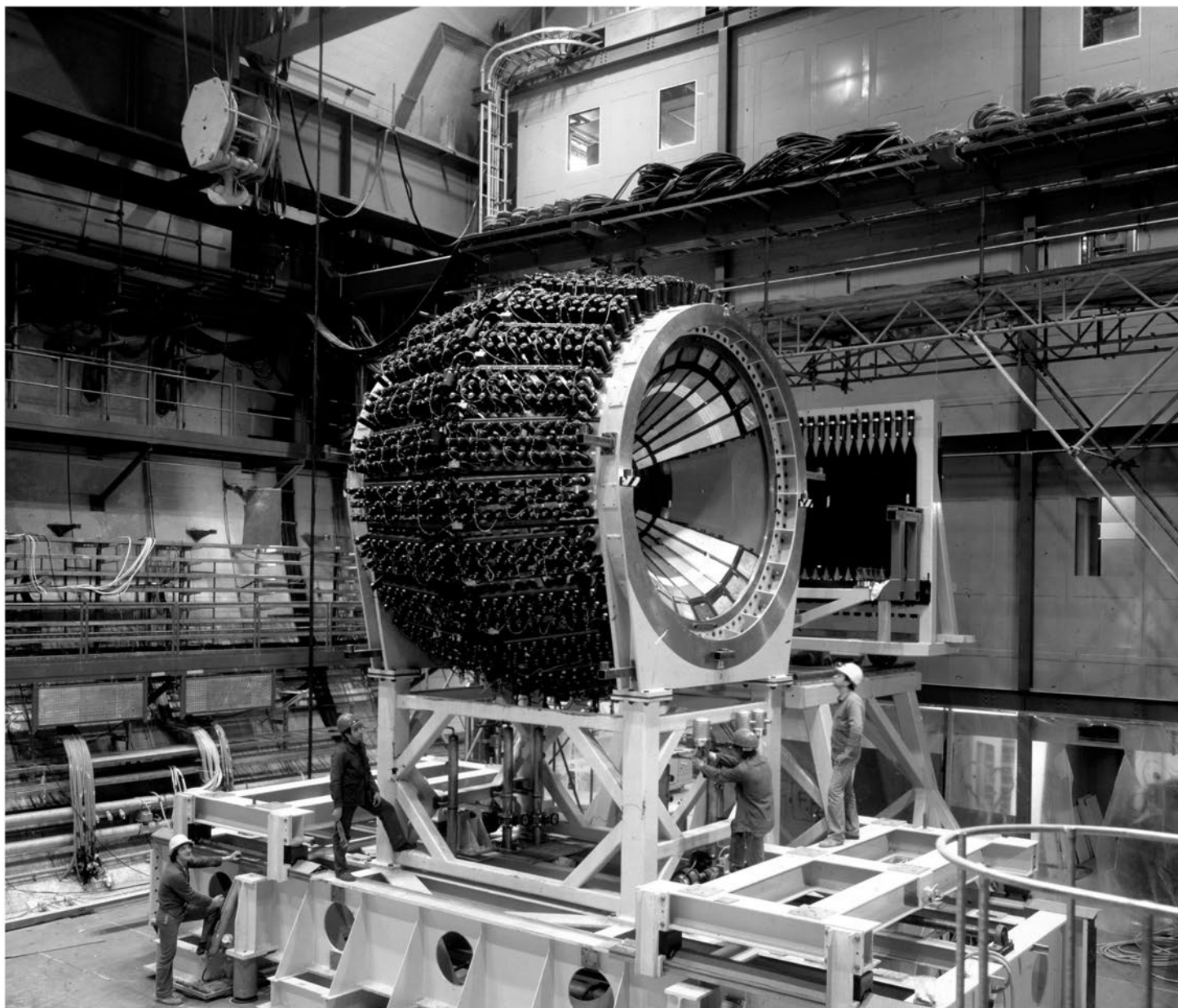
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- 1980 - *4π calorimeters introduced (crucial for discovery W boson)*

1980 - Calorimeters become crucial component of 4π experiments

(event selection: trigger on energy flow parameters such as missing E_T)

Led to discovery of $W \rightarrow e\nu$, $W \rightarrow \mu\nu$

*UA2
(CERN)*



Example of energy flow information

$$e^+e^- \rightarrow W^+W^-$$

$(\sqrt{s} = 181 \text{ GeV})$

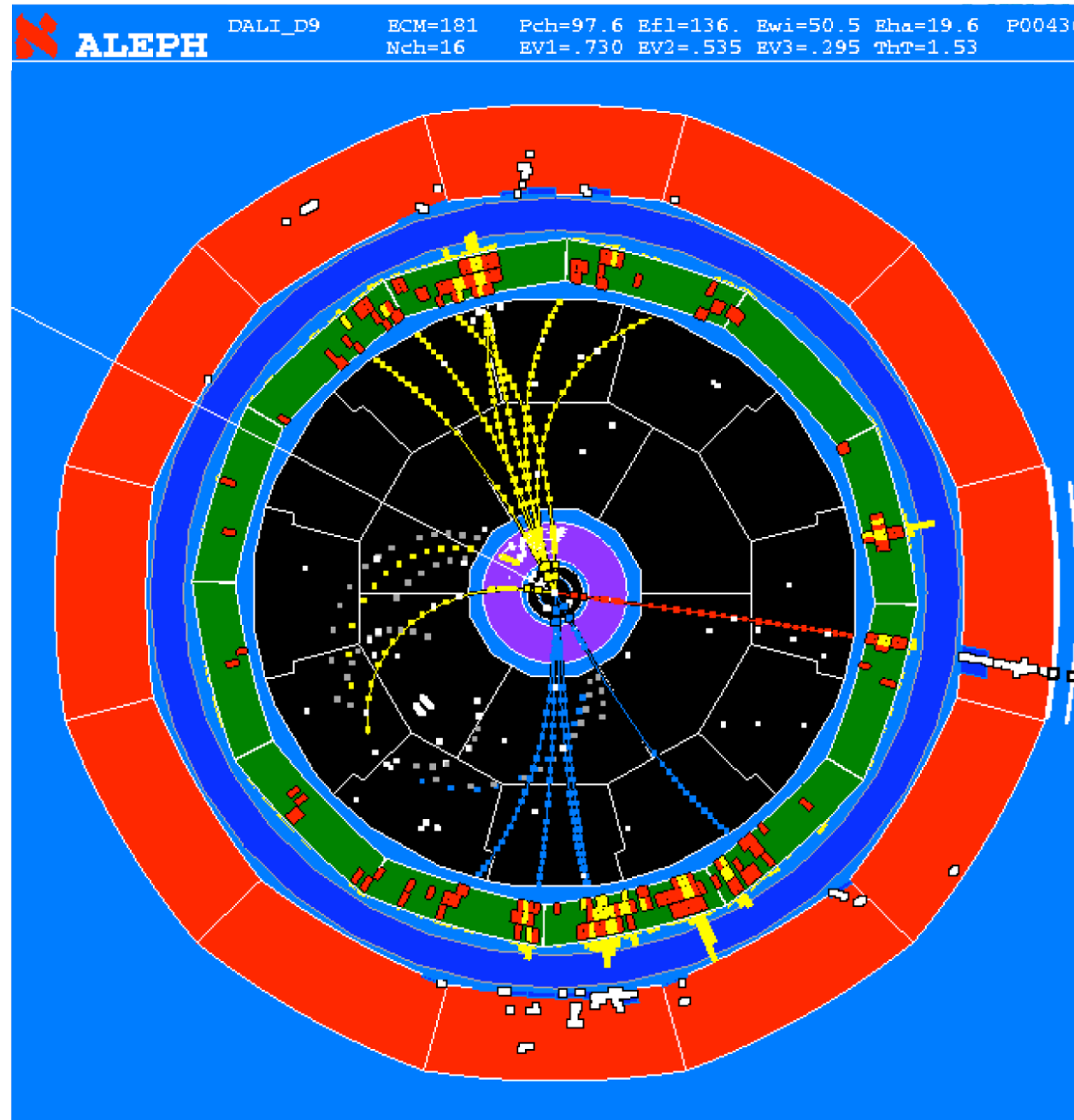
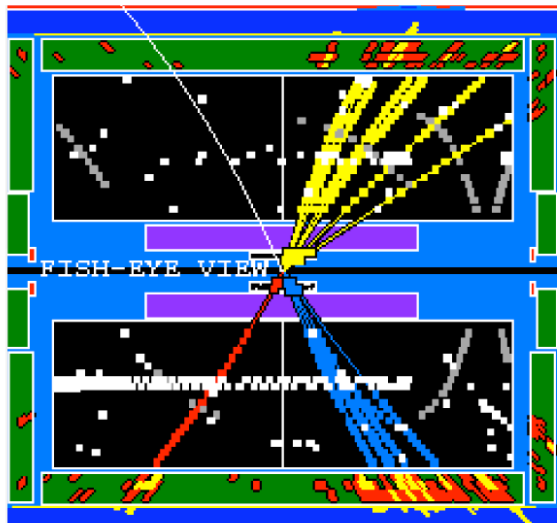
$$WW \rightarrow qq\mu\nu_\mu$$

In final state:

2 hadronic jets

1 energetic muon

missing $E_T(\nu_\mu)$



Milestones

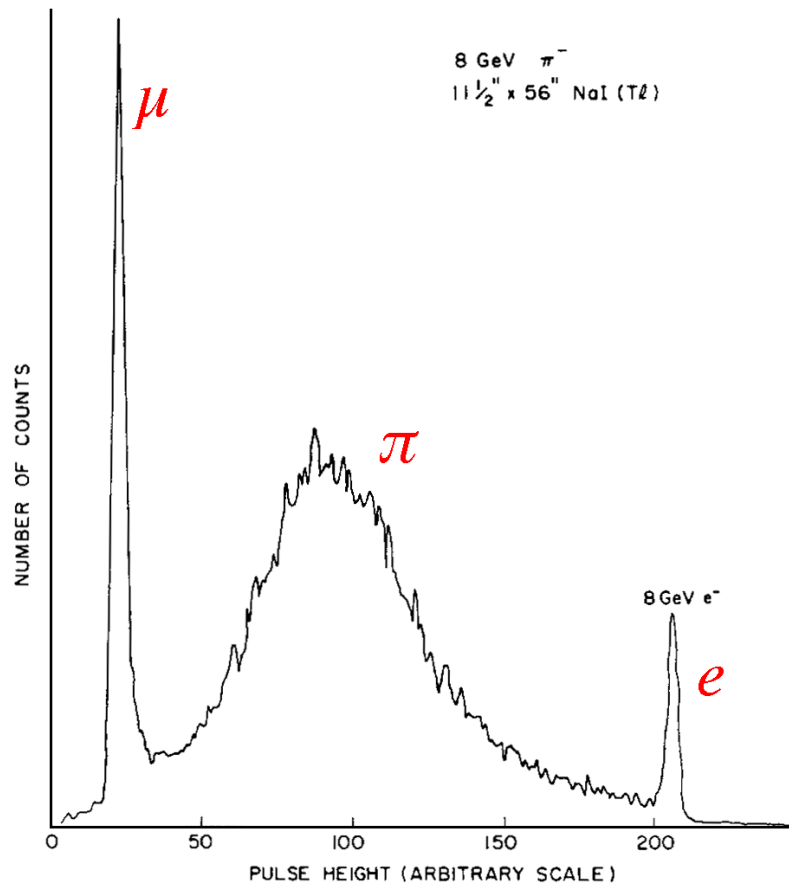
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NIM 75 (1969) 130

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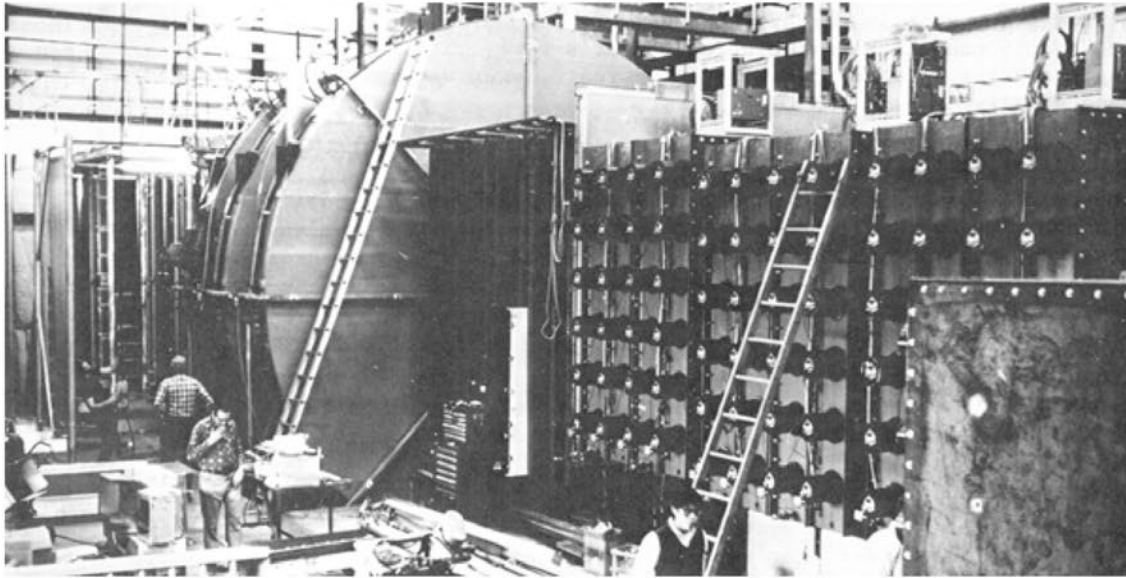
Tested with 8 GeV particle beams



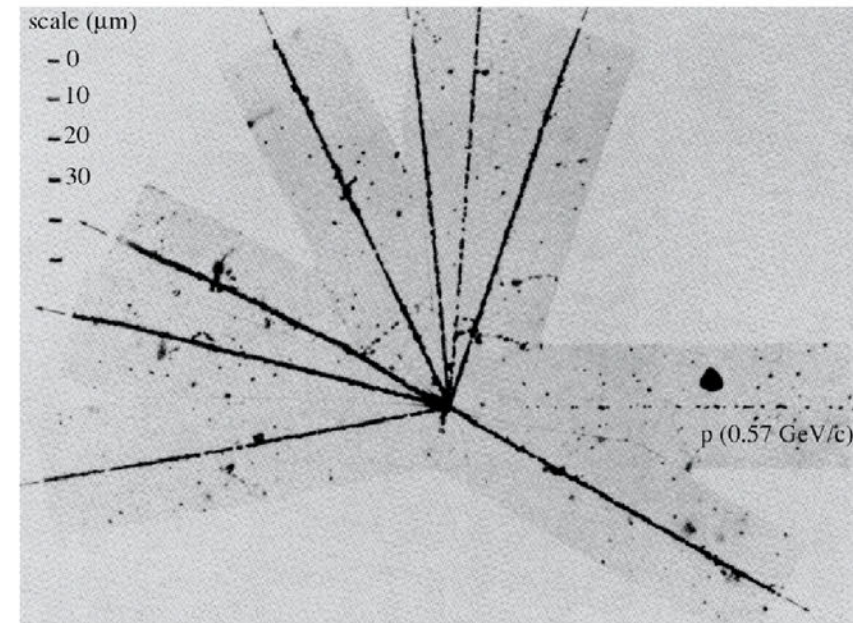
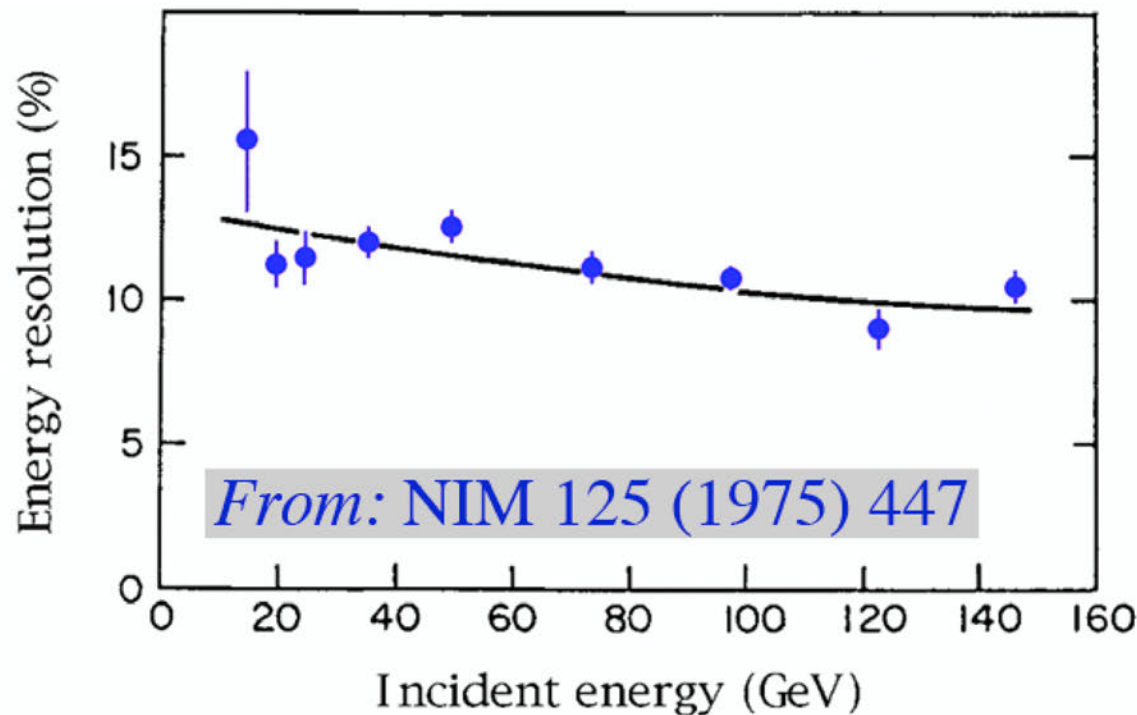
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Energy resolution of a homogeneous hadron calorimeter (60 tonnes of liquid scintillator)



Statistical processes are NOT the limiting factor here. Resolution is limited by fluctuations in invisible energy losses in the non-em shower component, e.g. in nuclear interactions



High resolution hadron calorimetry had become a reality

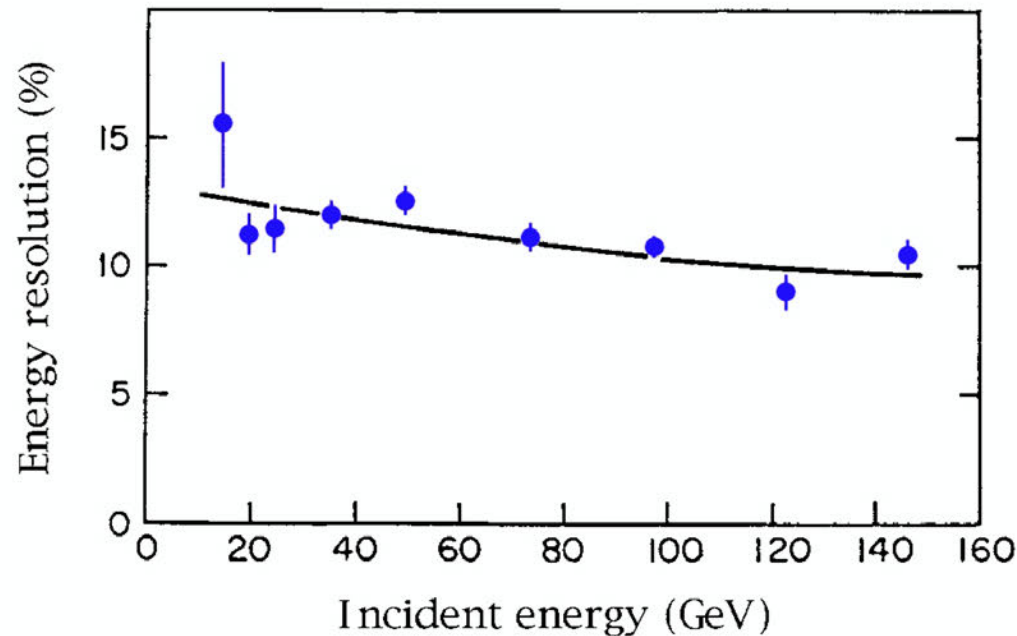


Figure 9: The hadronic energy resolution as a function of energy, for a homogeneous calorimeter consisting of *60 tonnes of liquid scintillator*

NIM 125 (1975) 447

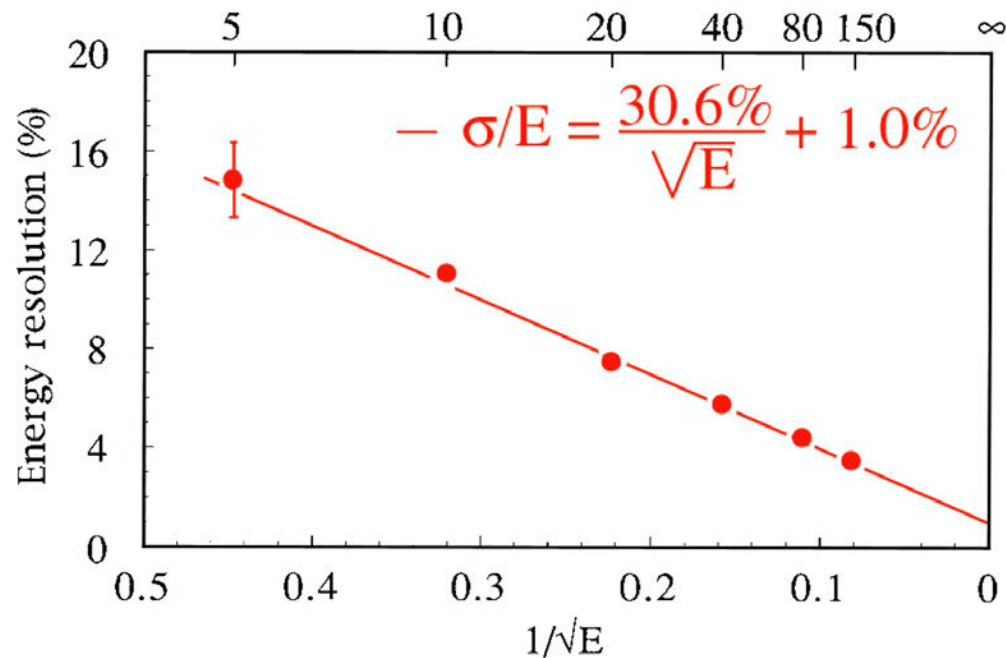
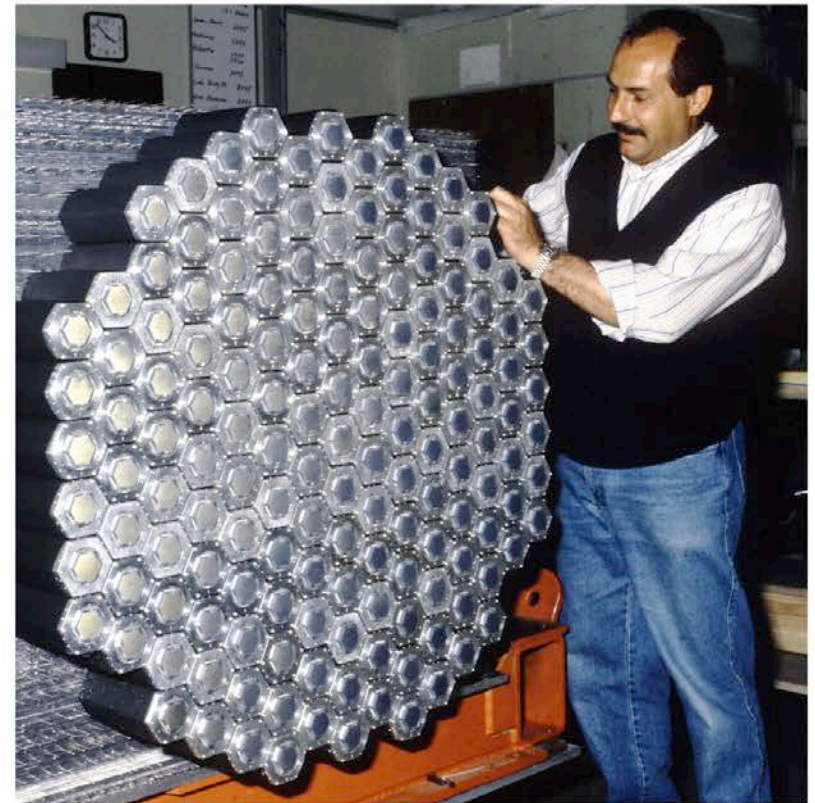
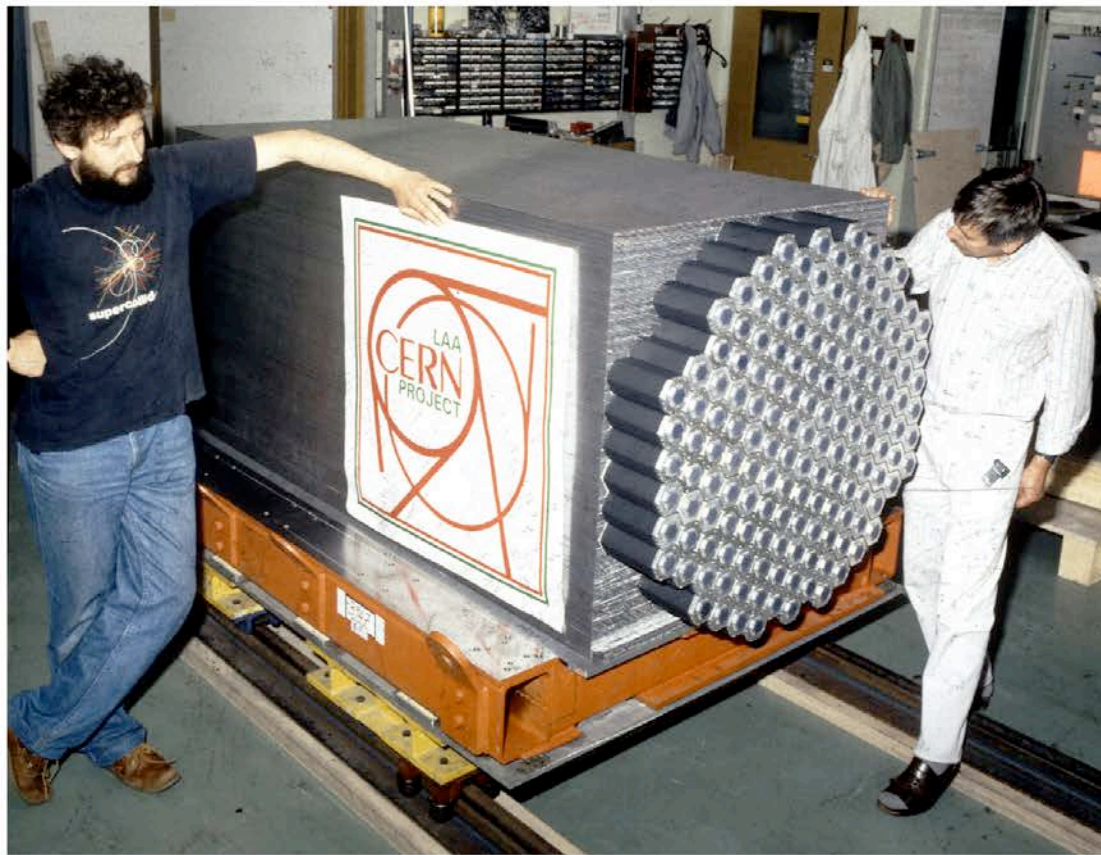


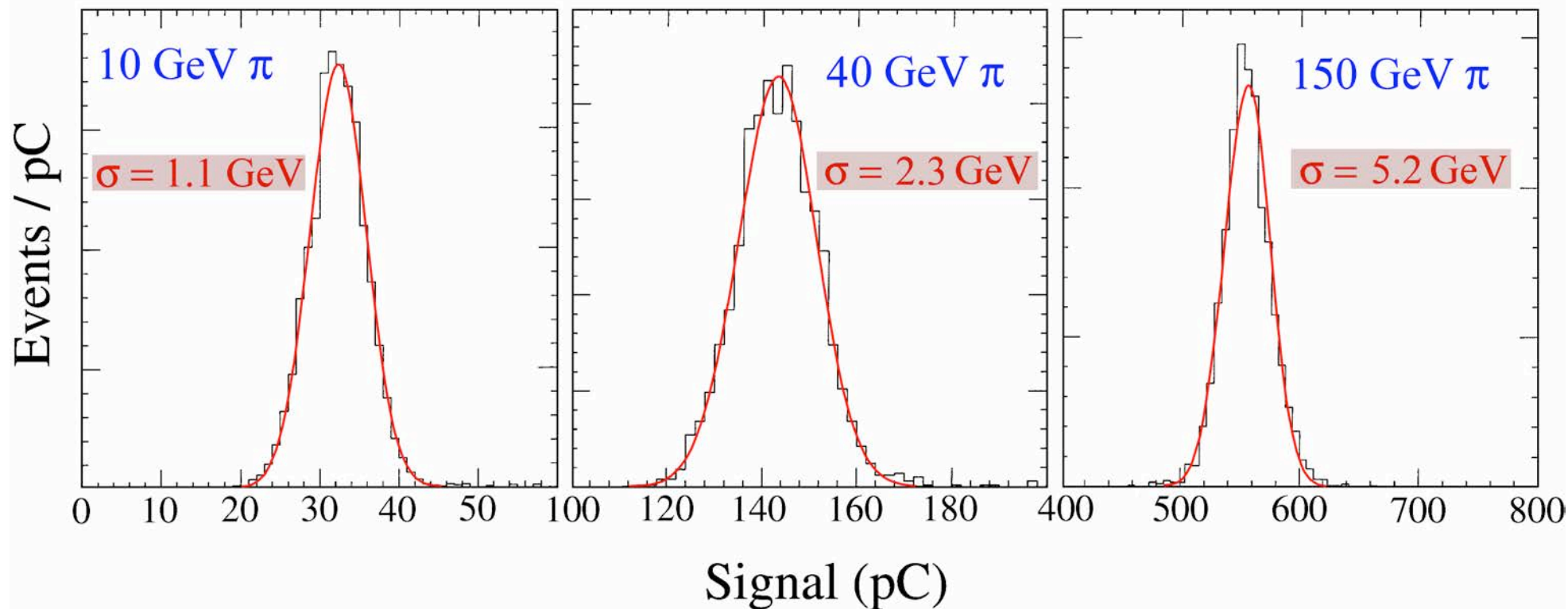
Figure 10: The hadronic energy resolution as a function of energy, for the compensating SPACAL *lead/plastic-scintillator calorimeter* (sampling fraction 2%)

NIM A308 (1991) 481

SPACAL 1989



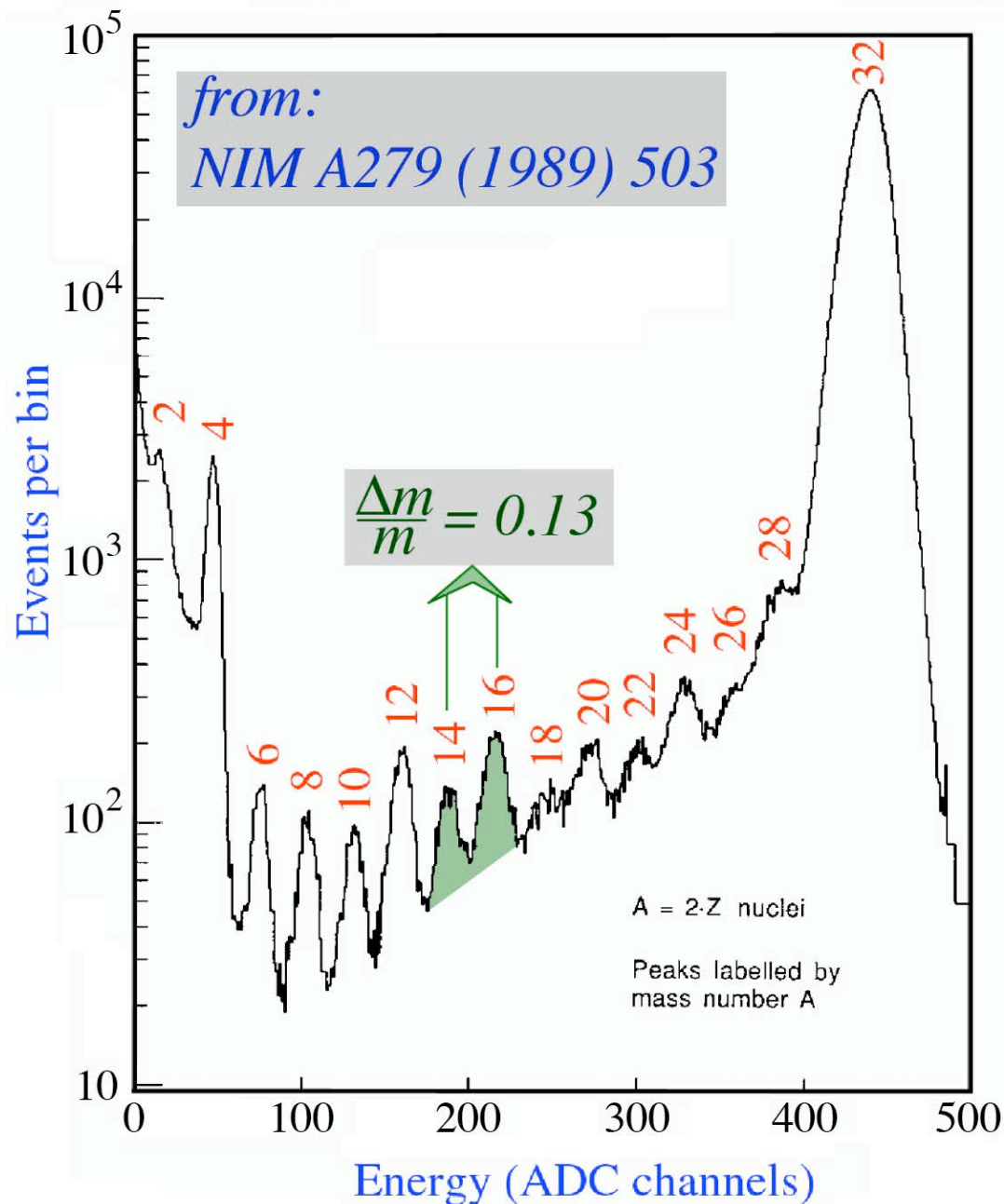
Hadronic signal distributions in a compensating calorimeter



from: NIM A308 (1991) 481

Hadron calorimetry in practice

Energy resolution in a compensating calorimeter



W/Z separation:

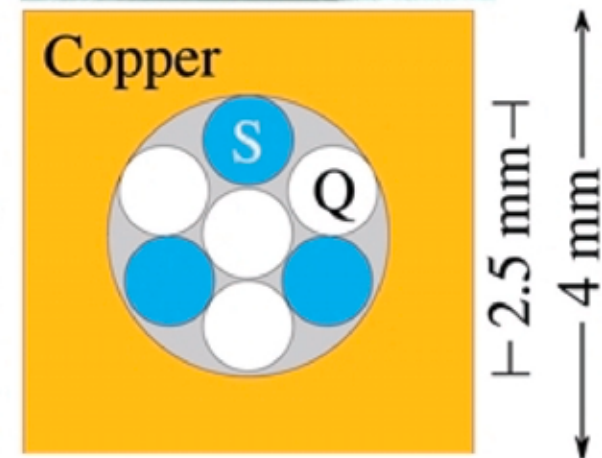
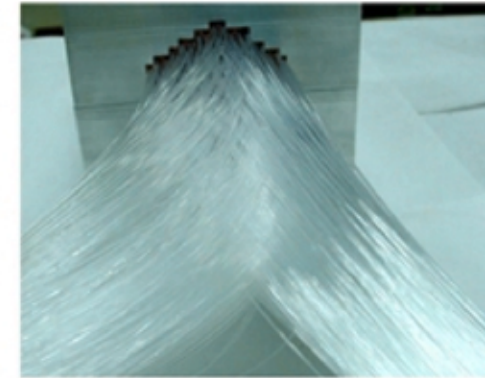
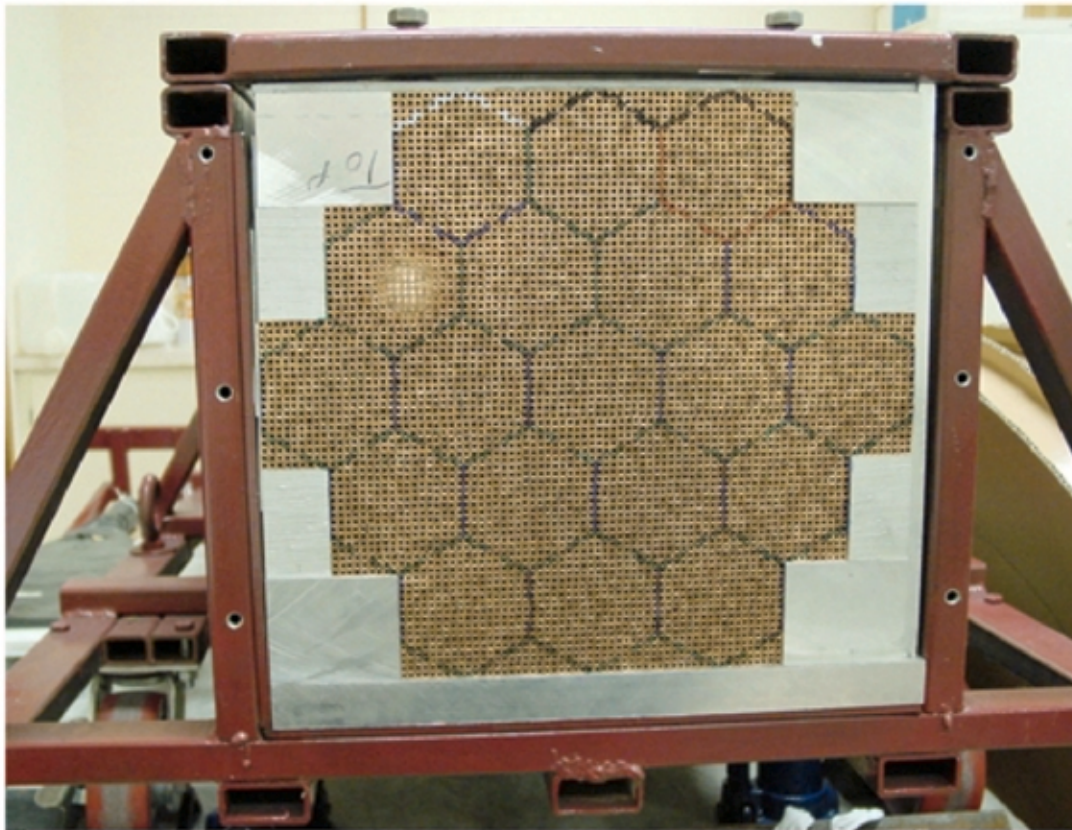
$$\frac{\Delta m}{m} \sim 0.11$$

The WA80 calorimeter as high-resolution spectrometer.
Total energy measured with the calorimeter for minimum-bias events revealed the composition of the momentum-selected CERN heavy-ion beam

Milestones

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- 2000 - *Merits of dual-readout calorimetry experimentally demonstrated*

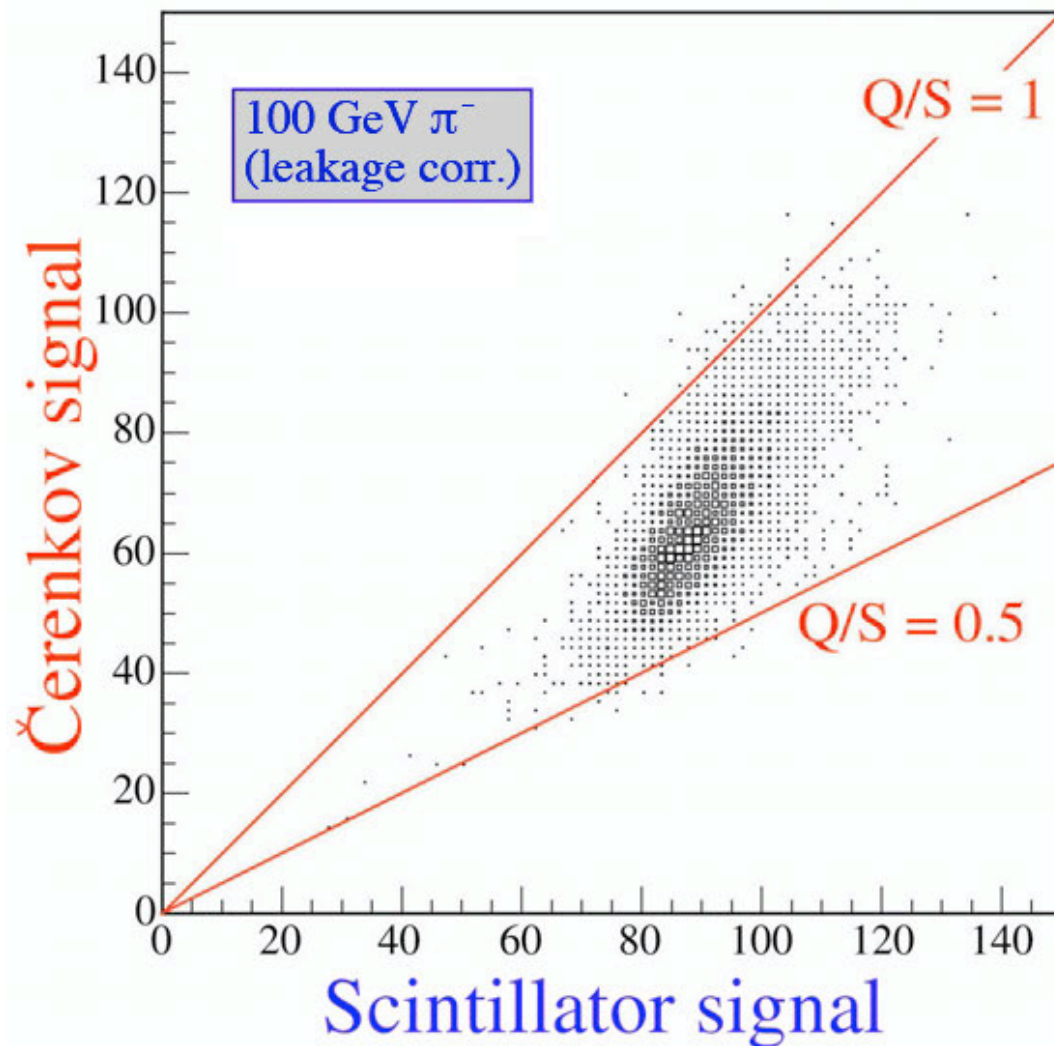
DREAM: Structure



- *Some characteristics of the DREAM detector*

- **Depth** 200 cm ($10.0 \lambda_{\text{int}}$)
- Effective **radius** 16.2 cm ($0.81 \lambda_{\text{int}}$, $8.0 \rho_M$)
- **Mass** instrumented volume 1030 kg
- Number of **fibers** 35910, diameter 0.8 mm, total length ≈ 90 km
- Hexagonal **towers** (19), each read out by 2 PMTs

DREAM: How to determine f_{em} and E ?



$$S = E \left[f_{em} + \frac{1}{(e/h)_S} (1 - f_{em}) \right]$$

$$Q = E \left[f_{em} + \frac{1}{(e/h)_Q} (1 - f_{em}) \right]$$

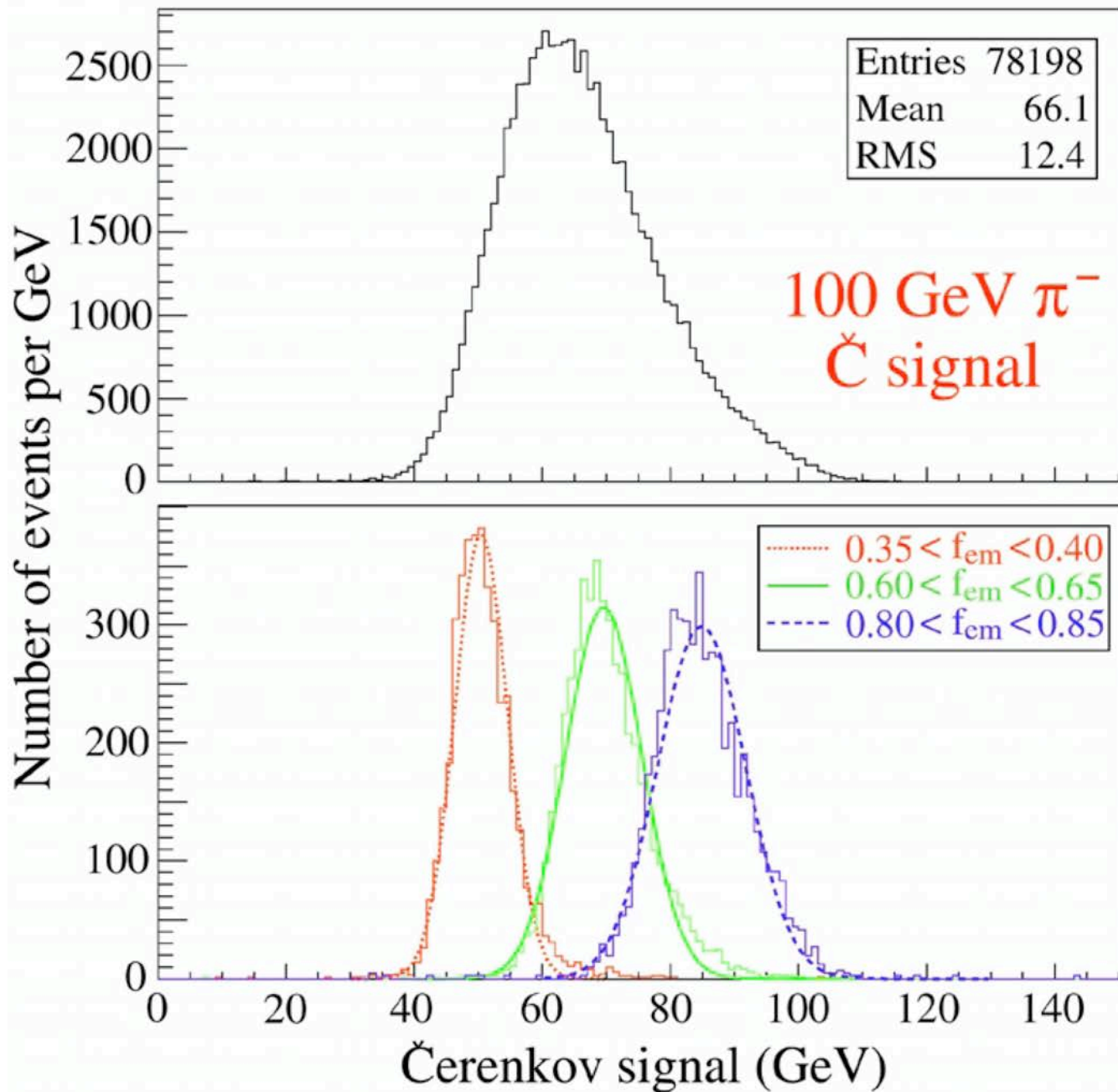
e.g. If $e/h = 1.3$ (S), 4.7 (Q)

$$\frac{Q}{S} = \frac{f_{em} + 0.21 (1 - f_{em})}{f_{em} + 0.77 (1 - f_{em})}$$

$$E = \frac{S - \chi Q}{1 - \chi}$$

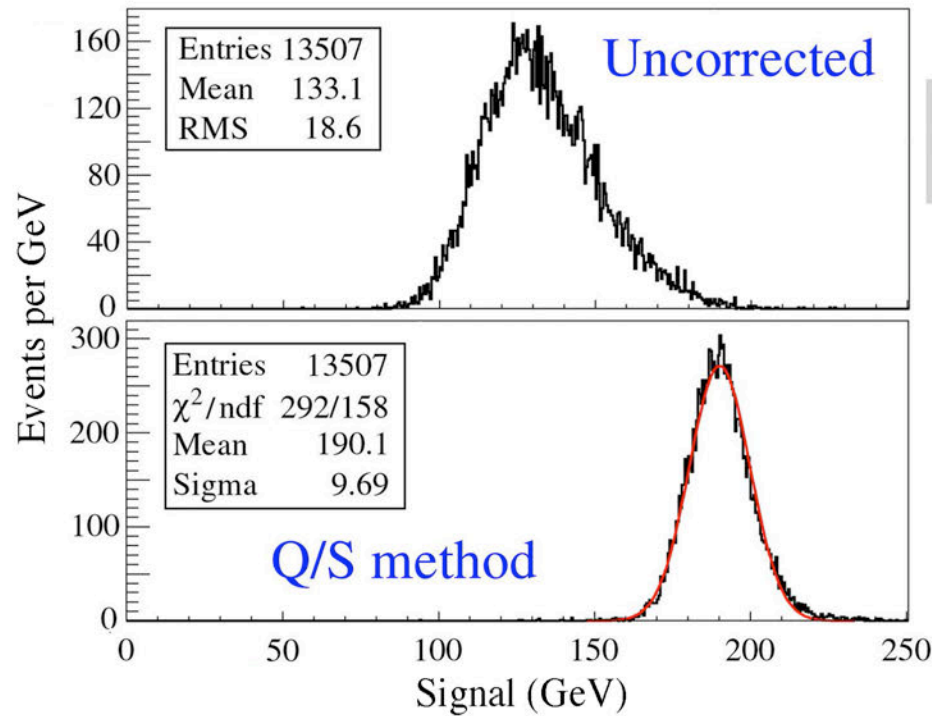
with $\chi = \frac{1 - (h/e)_S}{1 - (h/e)_Q} \sim 0.3$

DREAM: Effect of event selection based on f_{em}



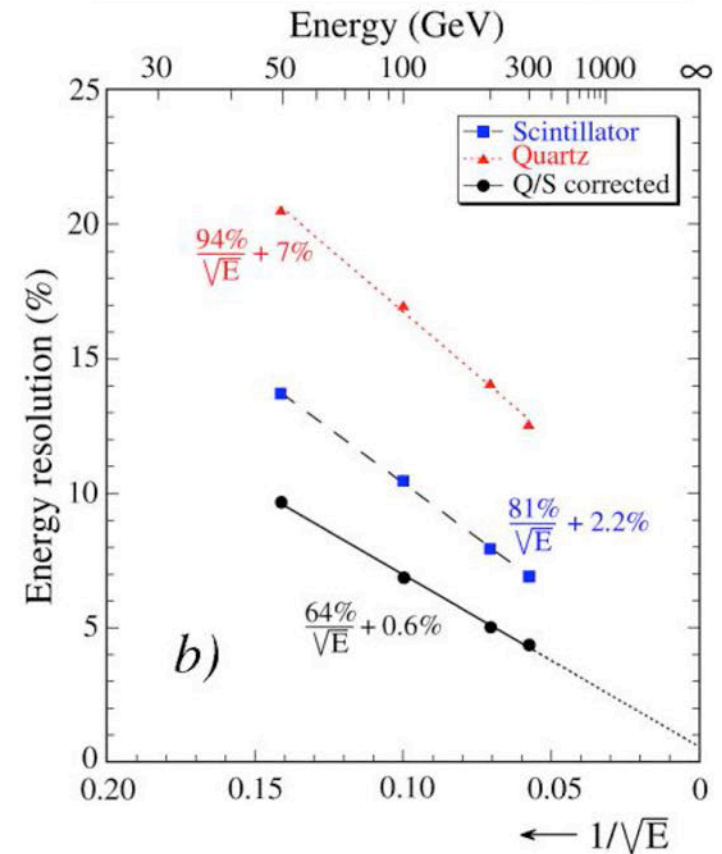
From:
NIM A537 (2005) 537

Effects of Q/S corrections on

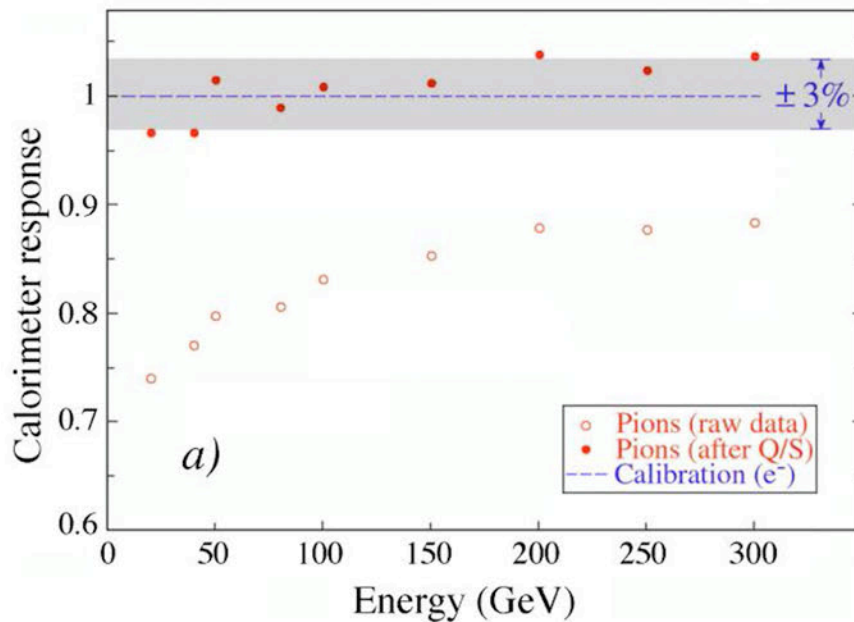


Calorimeter response function

jet energy resolution



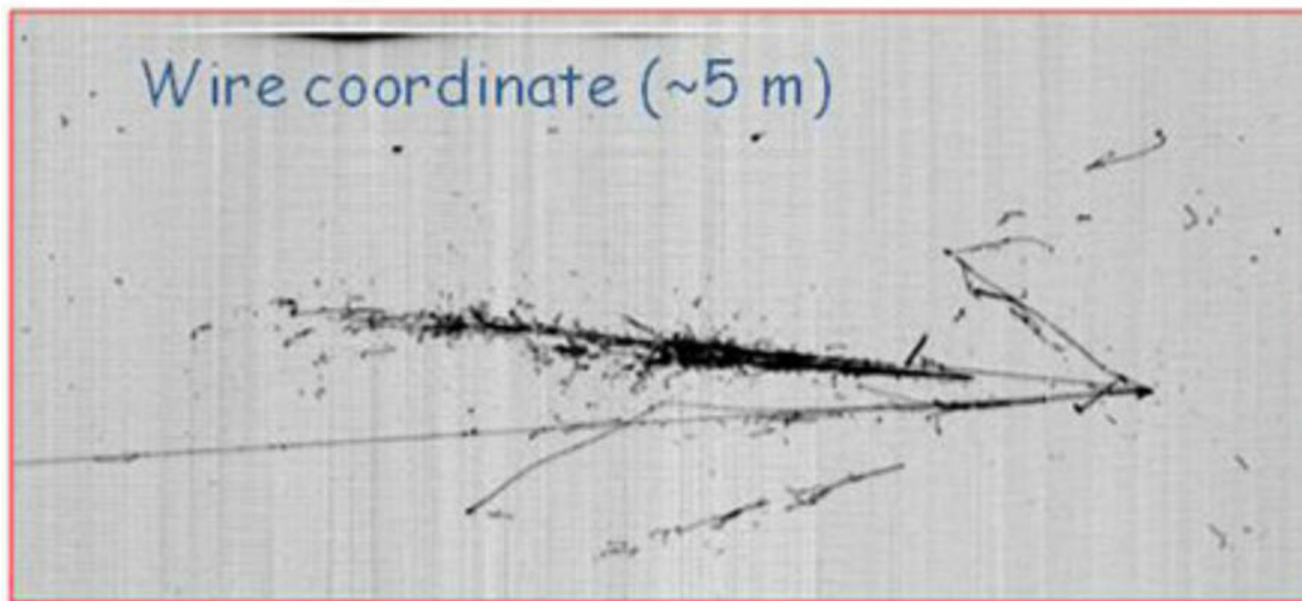
hadronic signal linearity



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- 2005 - *Imaging calorimetry demonstrated (LAr)*

2005 - Imaging calorimetry pioneered by ICARUS (LAr)



CERN to Gran Sasso ν beam



Some common (sometimes dangerous)

misconceptions

about calorimetry

Misconceptions about calorimetry

- *A shower is a collection of mips*

*A shower is a collection of different shower particles
(e , γ , π , p , n)*

*In a sampling calorimeter, these are sampled differently
The shower composition changes as the shower develops*

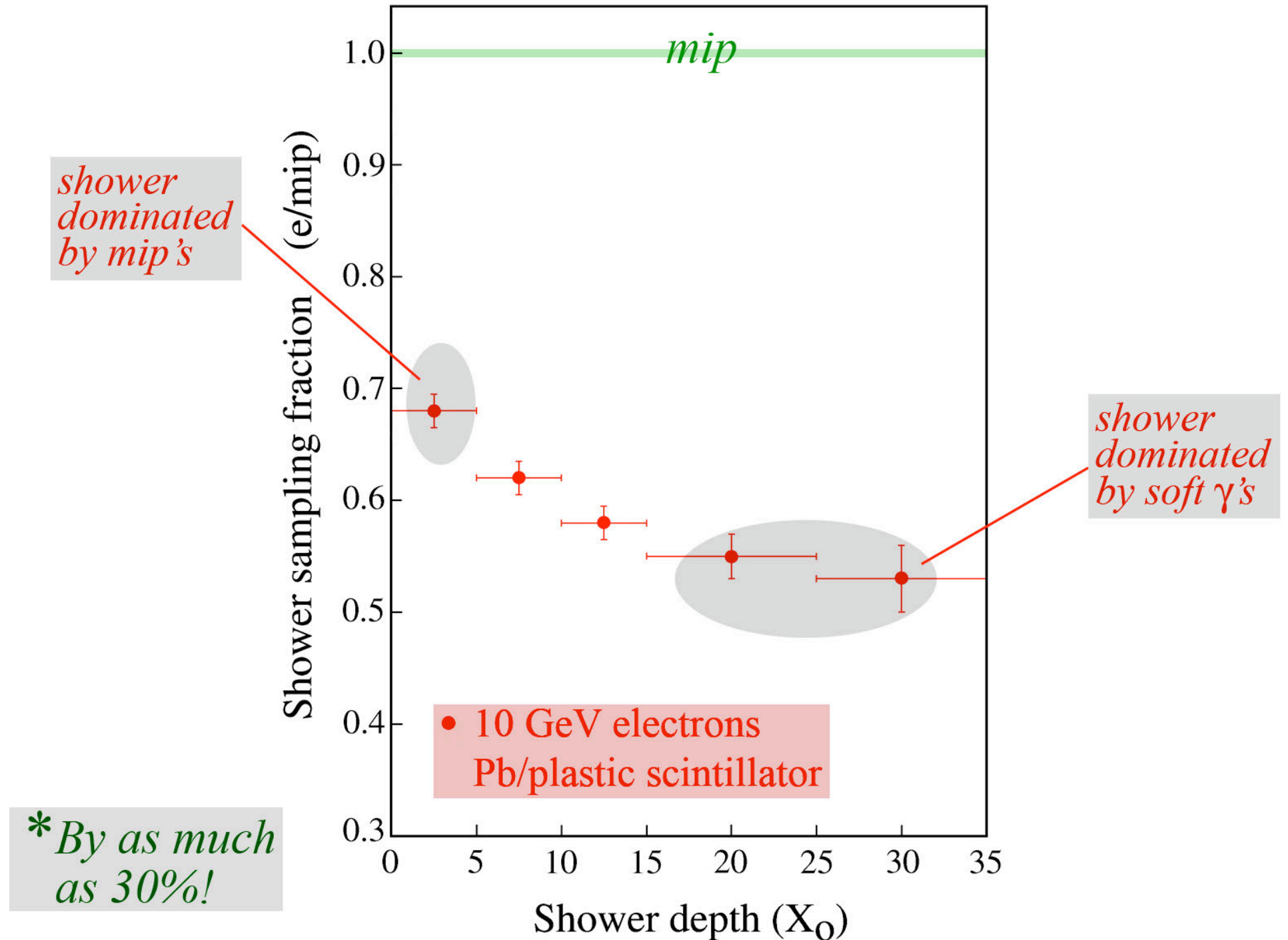
Misconceptions about calorimetry

- *A shower is a collection of mips*

This misconception is

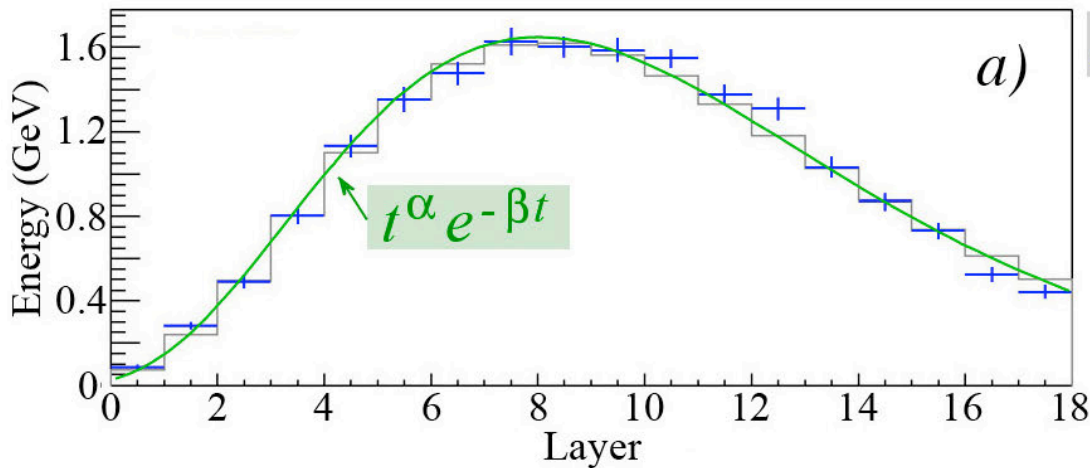
THE SOURCE OF MANY CALIBRATION PROBLEMS

*The sampling fraction changes as shower develops**



Calibration misery of longitudinally segmented devices

Example: AMS (em showers!)



Source: NIM A490 (2002) 132

Pb/scintillating fiber (18 layers)

Calibrated with mip's:

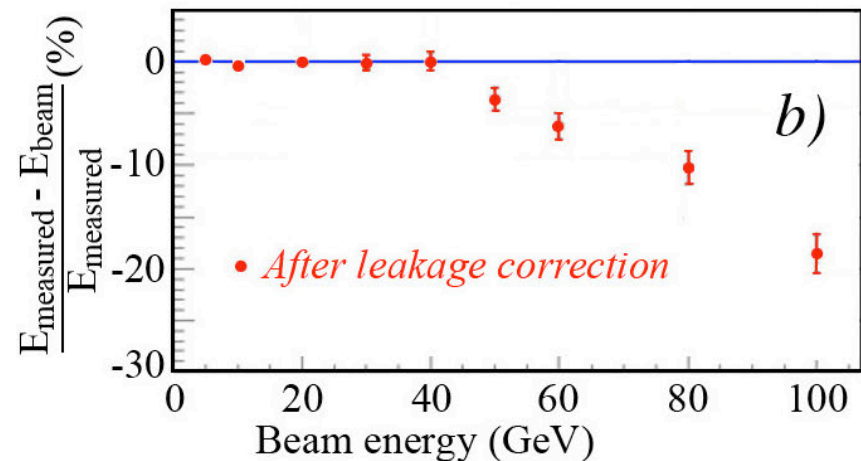
11.7 MeV/layer

Leakage estimated from fit to measured shower profile

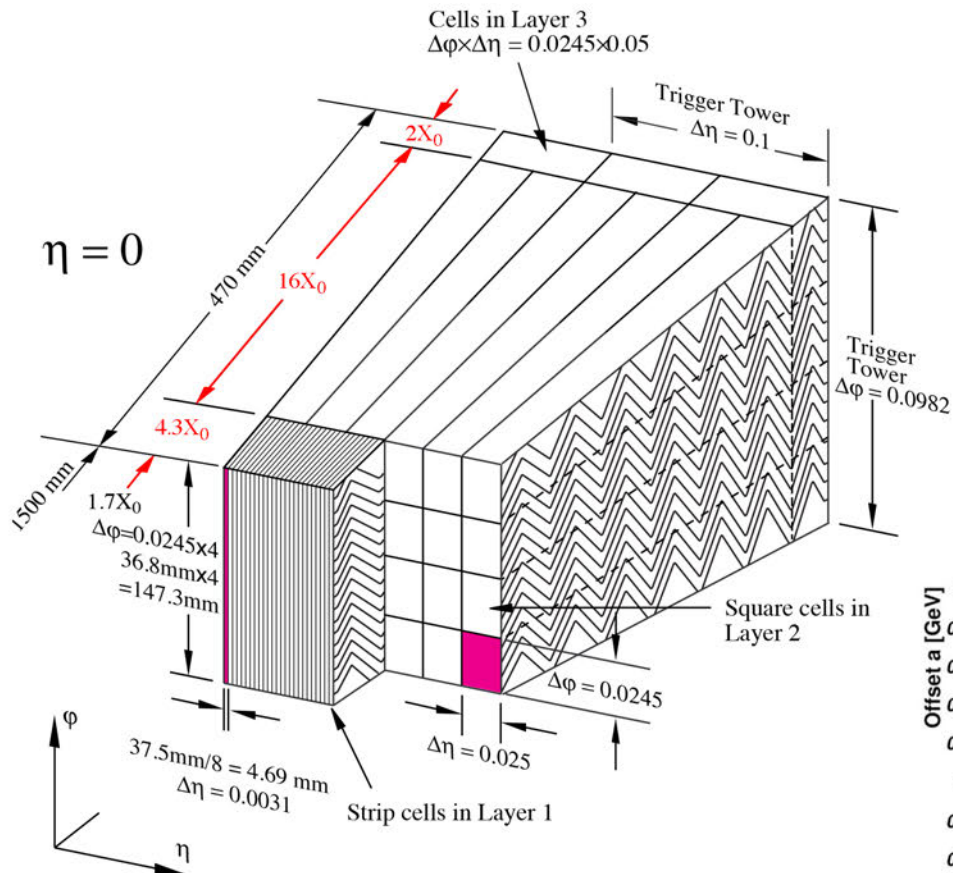
However:

In em shower, signal per GeV decreases as shower develops

→ (leakage) energy based on measured signals underestimates reality

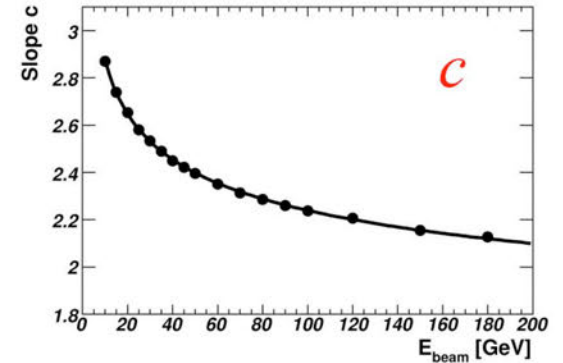
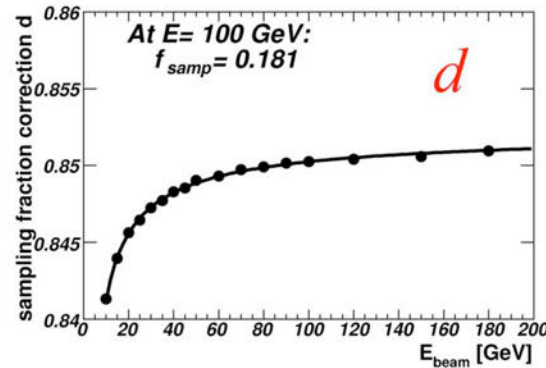
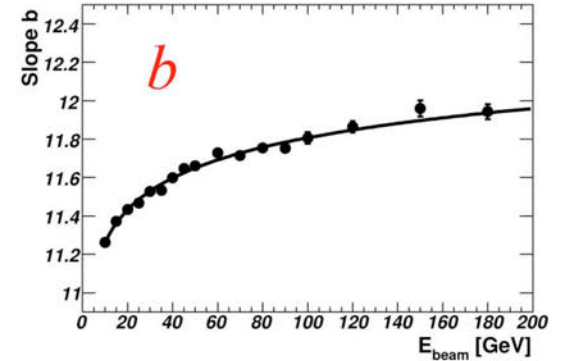
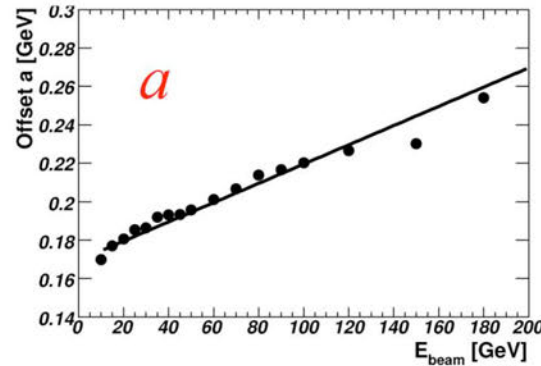


Required very elaborate MC simulations to solve, since effects depend on energy and direction incoming particle



Calibration of the ATLAS ECAL

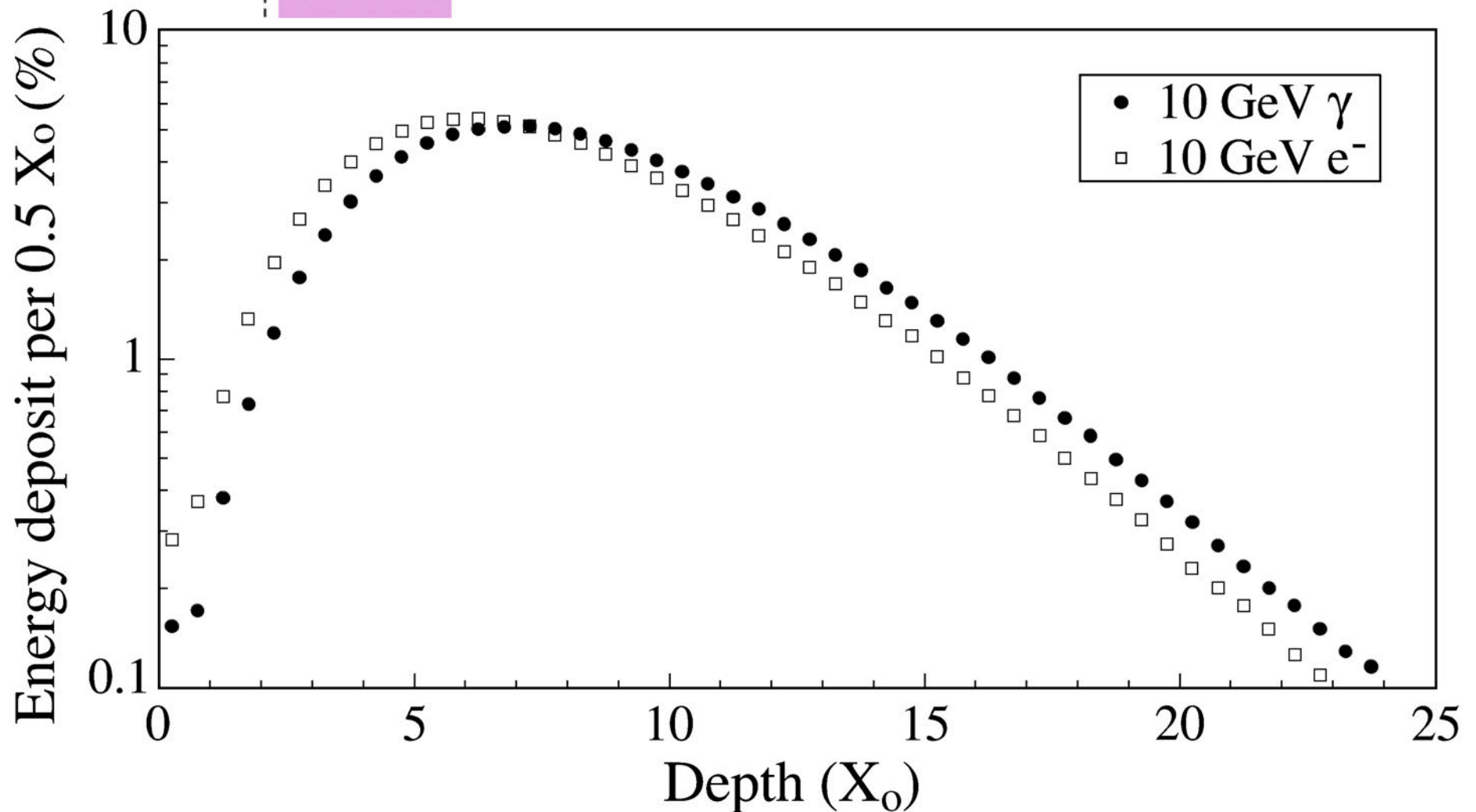
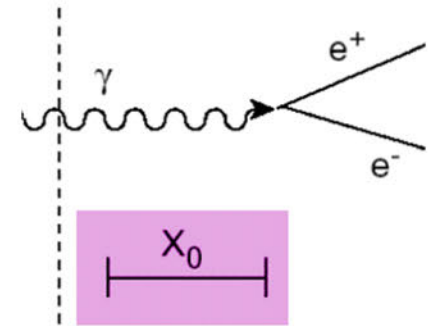
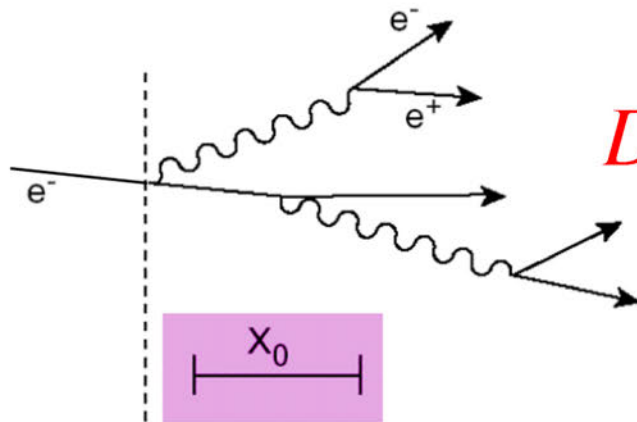
(for electrons, NOT γ s)



$$E^{\text{rec}} = \left(a(E) + b(E) E_0^{\text{vis}} + c(E) (E_0^{\text{vis}} \cdot E_1^{\text{vis}})^{0.5} + \frac{1}{d(E) f_{\text{samp}}} \sum_{i=1,3} E_i^{\text{vis}} \right) \cdot f_{\text{cell impact}}(\Delta\Phi) \cdot (1 + f_{\text{leakage}})$$

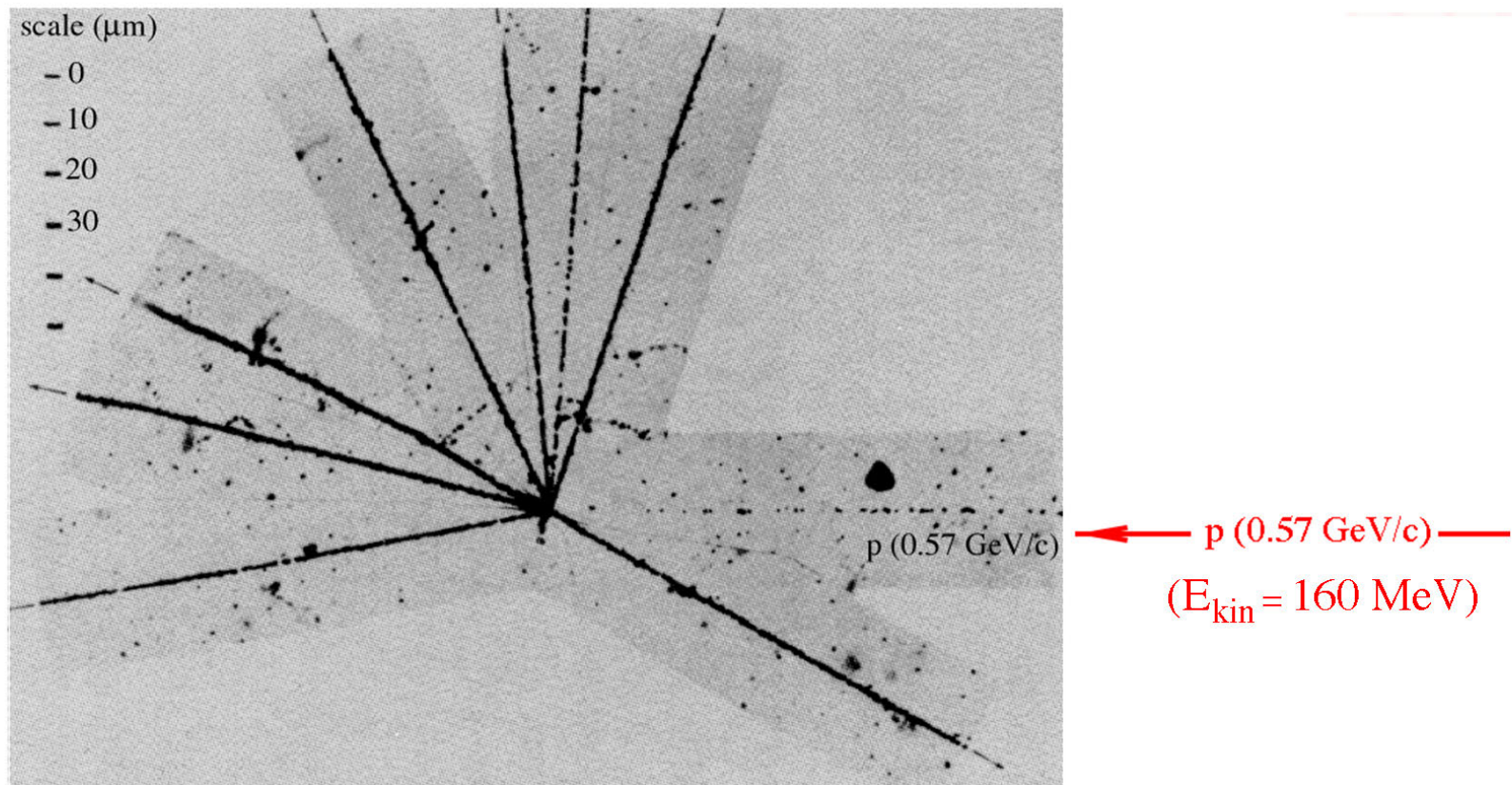
In a calorimeter, showers initiated by electrons and γ s

**DEVELOP
DIFFERENTLY**

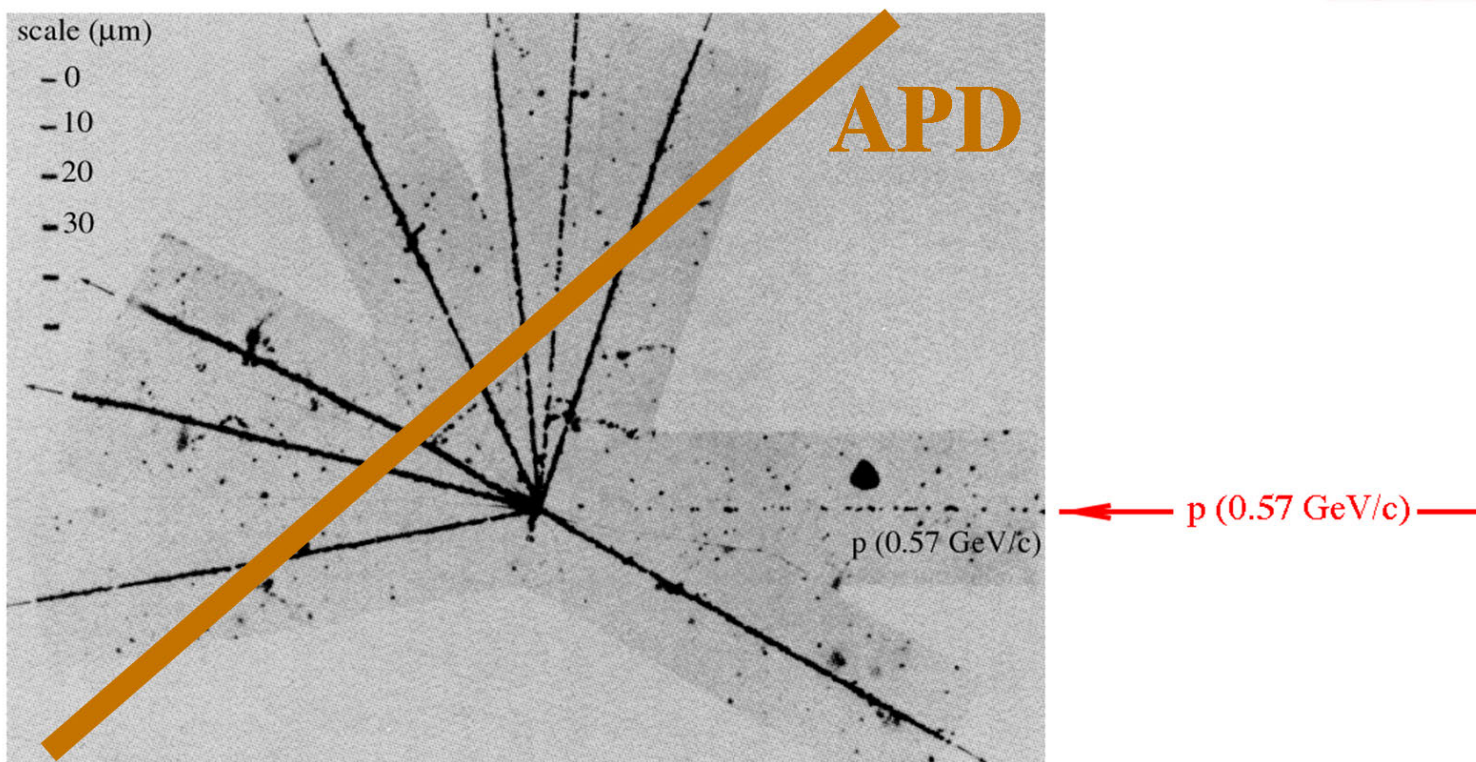
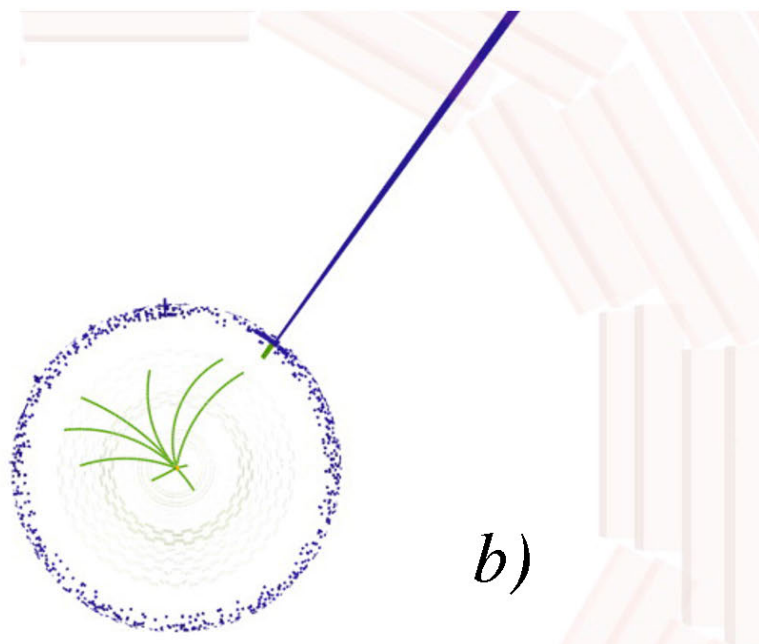
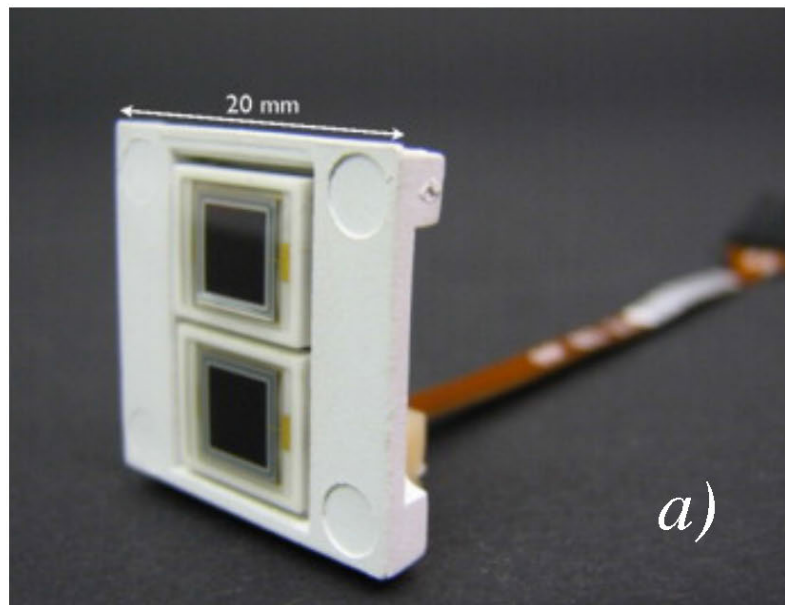


Catastrophic effects of ONE individual shower particle (1)

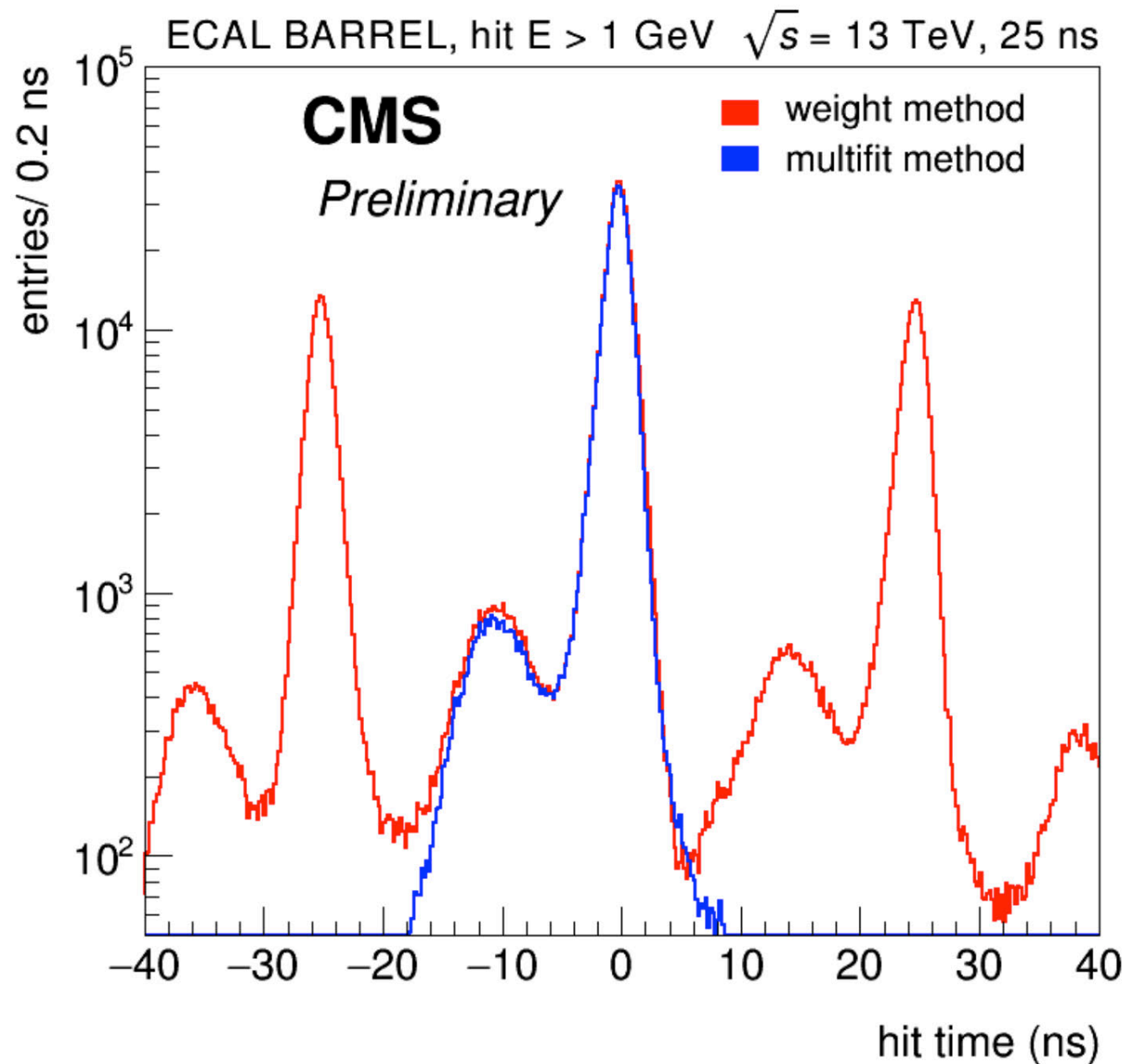
A typical process inside a hadronic shower



“Spike” events in CMS



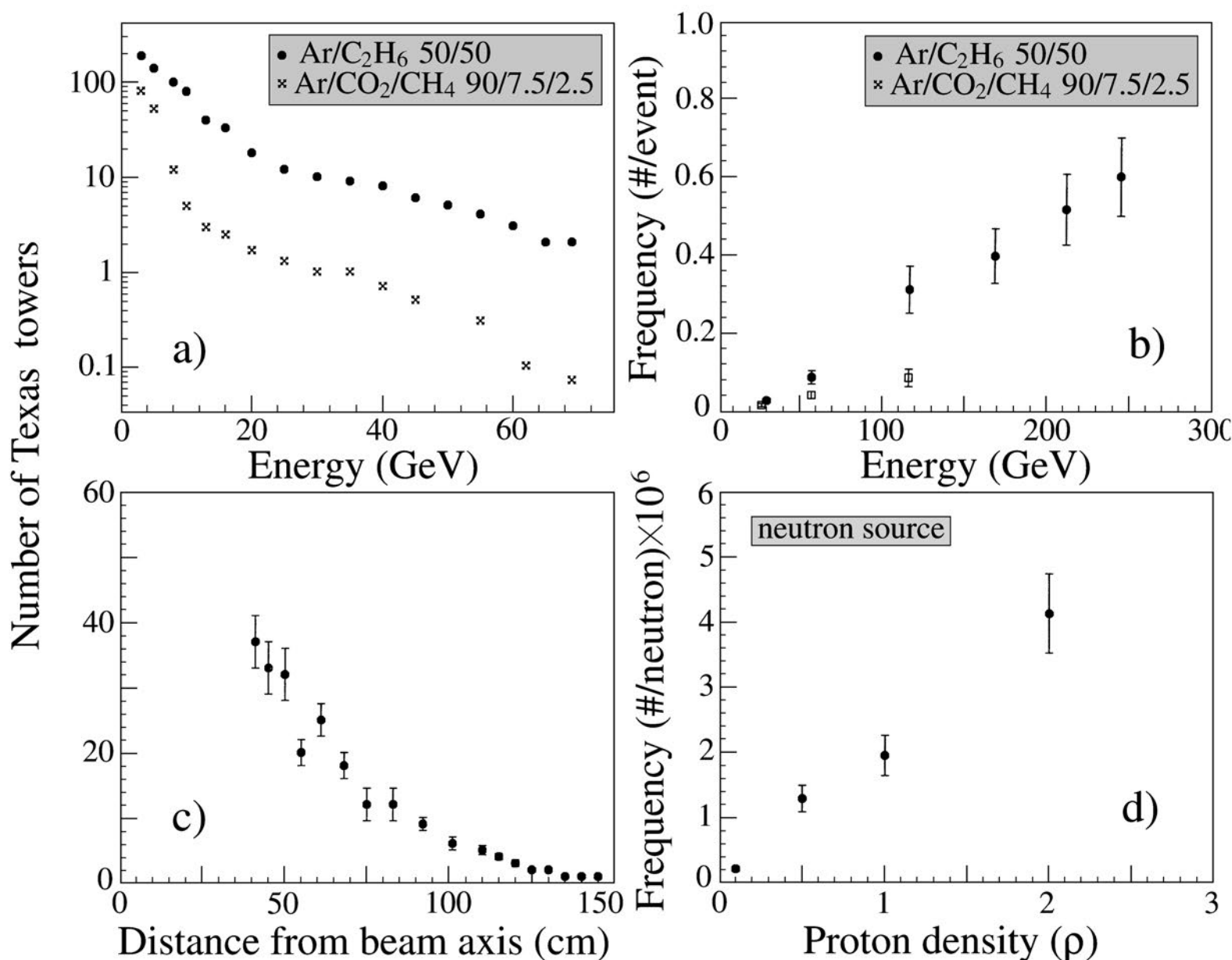
Spikes in CMS ECAL (after Swiss-cross elimination!)



Catastrophic effects of ONE individual shower particle (2)

The Texas Tower effect (CDF, 1988)

Sampling fraction mips = 10^{-5} \longrightarrow 100 GeV shower \equiv 1 MeV in gas!



Catastrophic effects of ONE individual shower particle (3)

(my prediction: bets, anyone?)

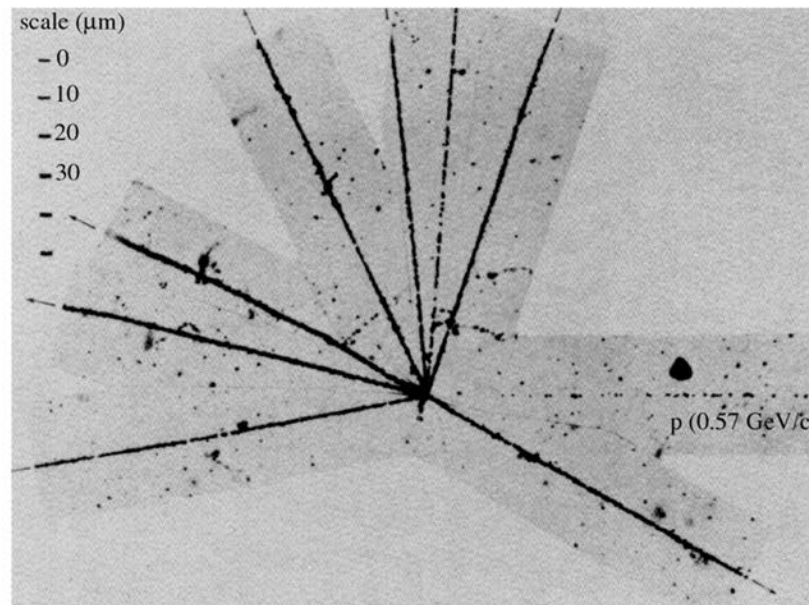
The high-luminosity CMS upgrade of the endcap calorimeter system has a section (FH) consisting of 5 cm thick brass absorber plates, interleaved with 100 μm silicon.

Sampling fraction for mips = $6 \cdot 10^{-4}$

*An event such as this one
(initiated by a 160 MeV proton)
may deposit 30 MeV in one Si layer*

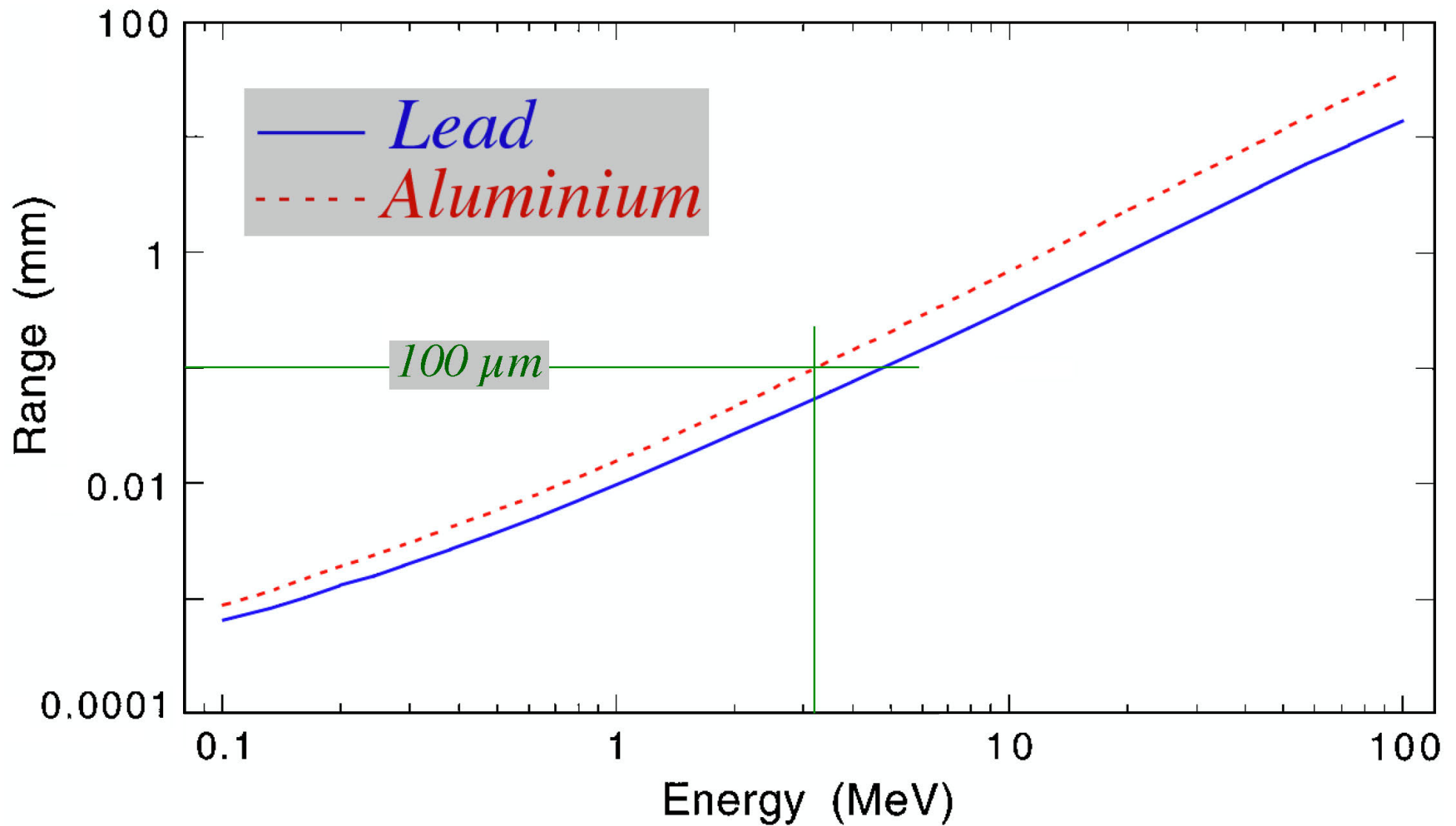
No signal saturation!

*This will be interpreted
as a 50 GeV energy deposit!*



*p (0.57 GeV/c)
($E_{\text{kin}} = 160 \text{ MeV}$)*

The range of low-energy protons in different materials



Misconceptions about calorimetry

- *A shower is a collection of mips*
- *Energy resolution \equiv width of signal distribution*

A comment for those who want to “optimize” energy resolution

*Energy resolution = precision with which the energy of a particle
or jet showering in the calorimeter can be determined*

*A narrow signal distribution may ONLY be interpreted as a good energy
resolution if it is centered around the correct energy value*

Therefore, signal linearity is an integral aspect of good energy resolution

Results of miscalibration: Mass dependence

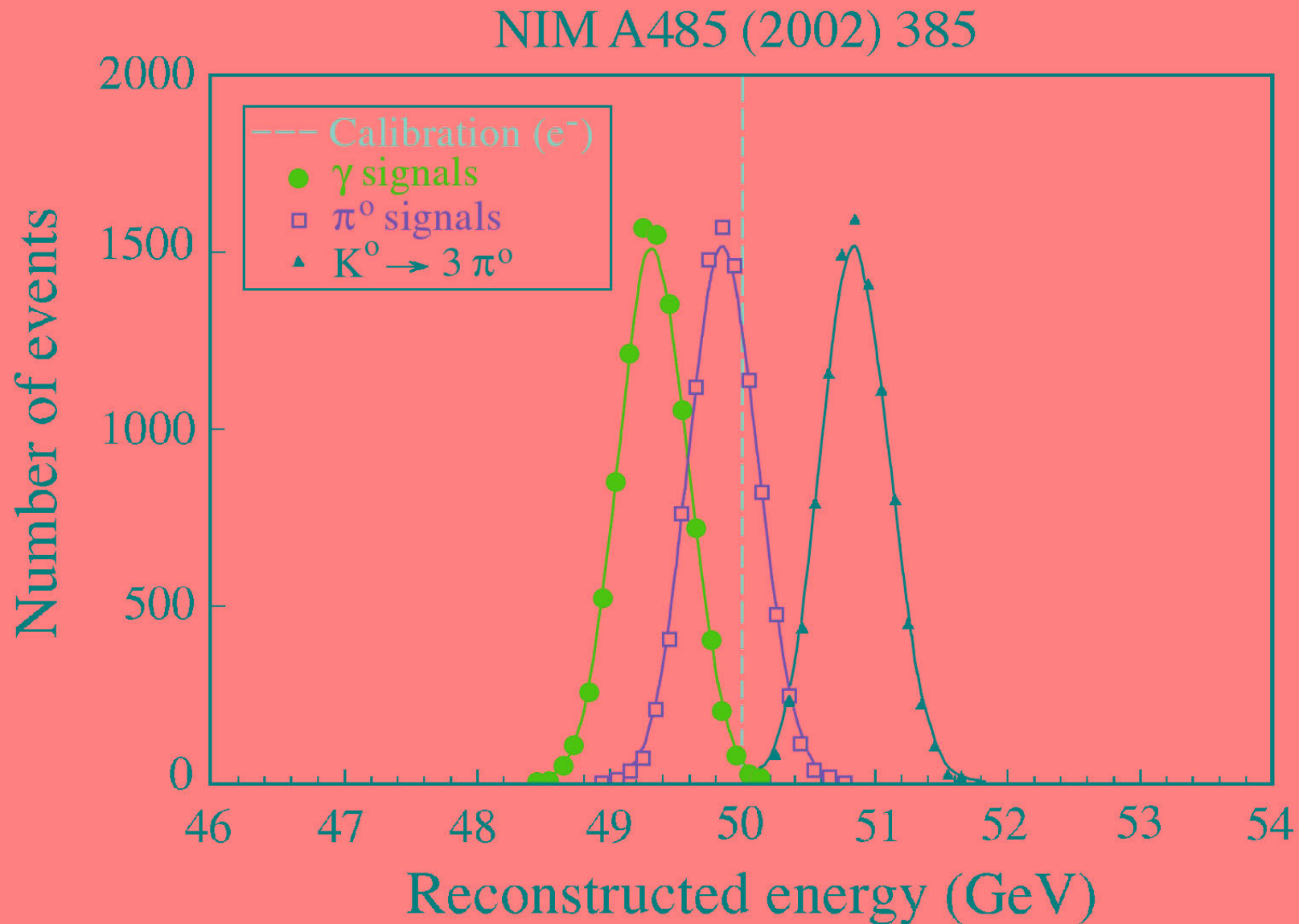
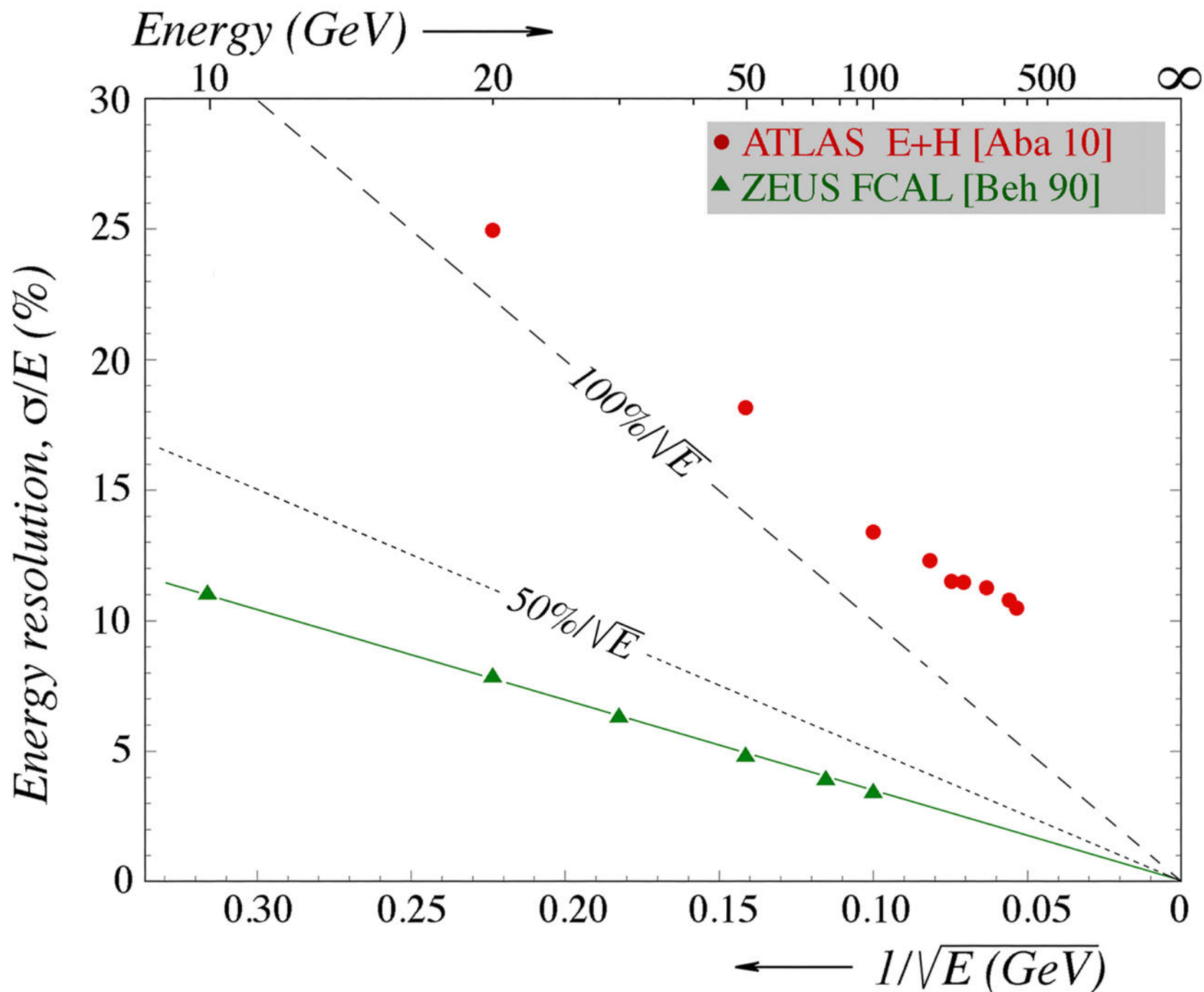


Figure 14: Signal distributions for γ s and various hadrons decaying into all- γ final states. All particles have the same nominal energy and the detector, which has an intrinsic resolution of 0.5% for em showers of this energy, was calibrated with electrons using $B/A = 0.8$. See text for details.

Misconceptions about calorimetry

- *A shower is a collection of mips*
- *Energy resolution \equiv width of signal distribution*
- *Energy resolution scales like $E^{-1/2}$*

Hadronic energy resolution of compensating vs modern calorimeters

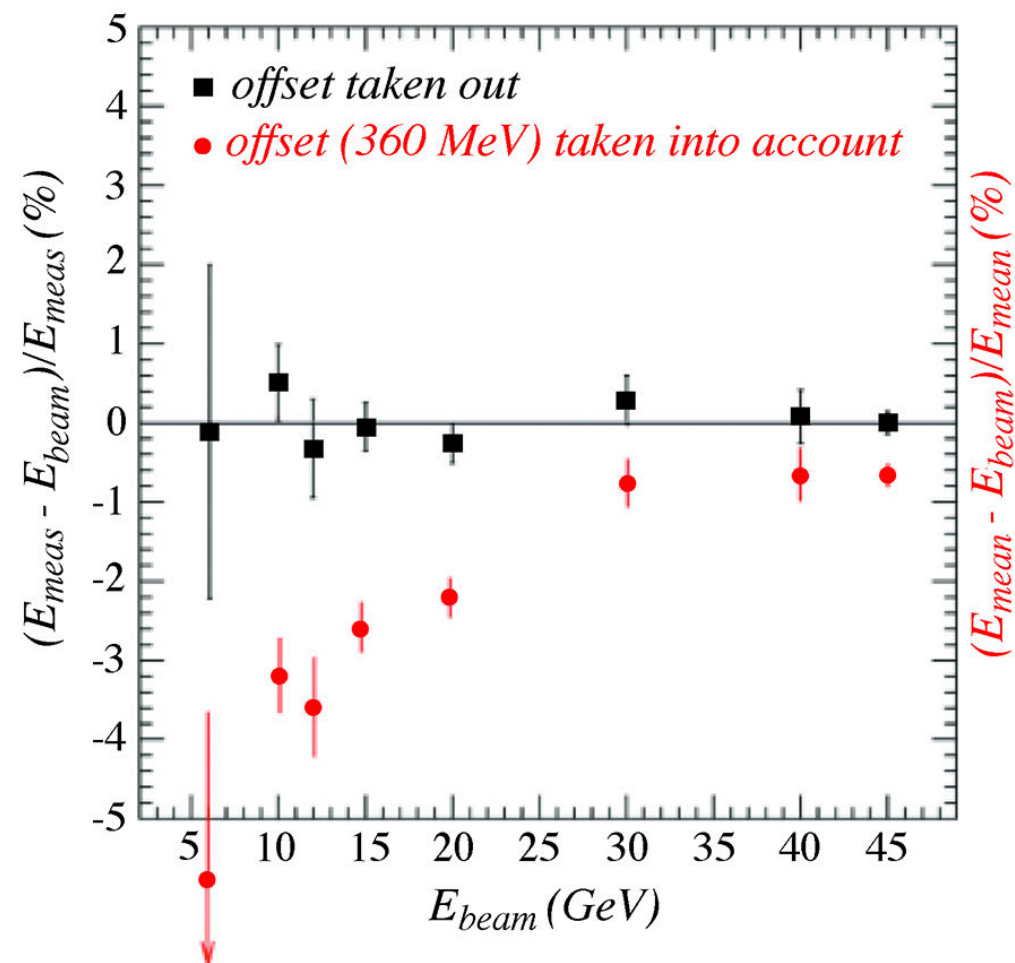
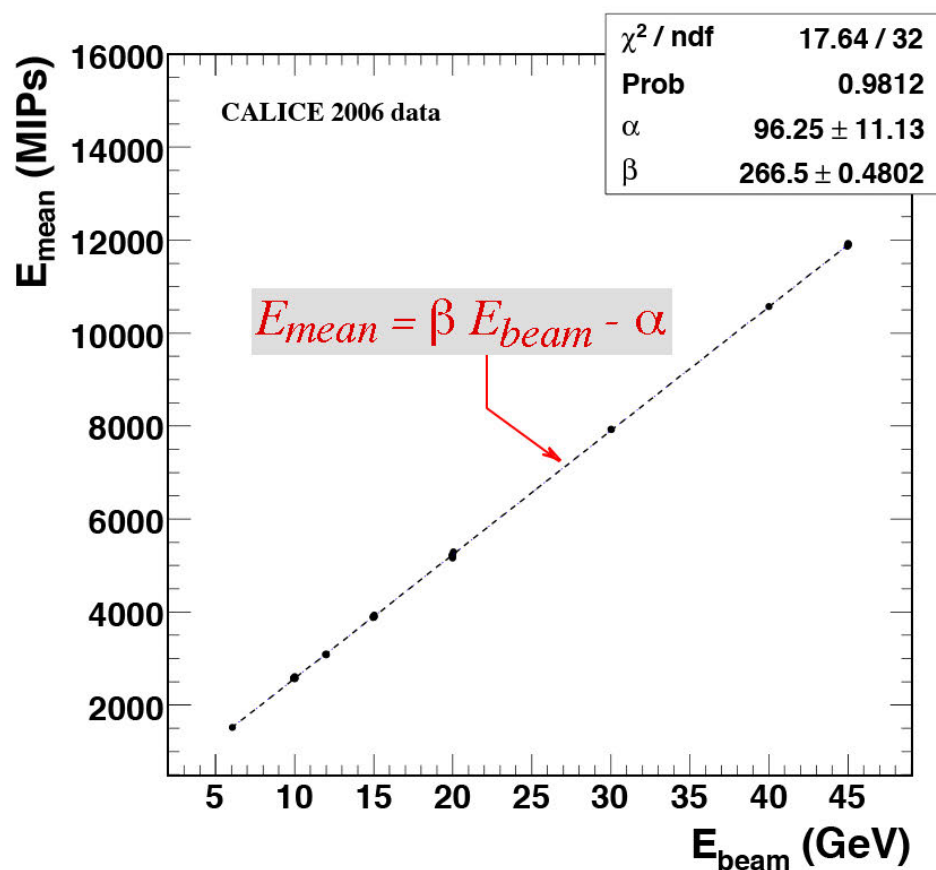


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Response non-linearity in CALICE W/Si ECAL

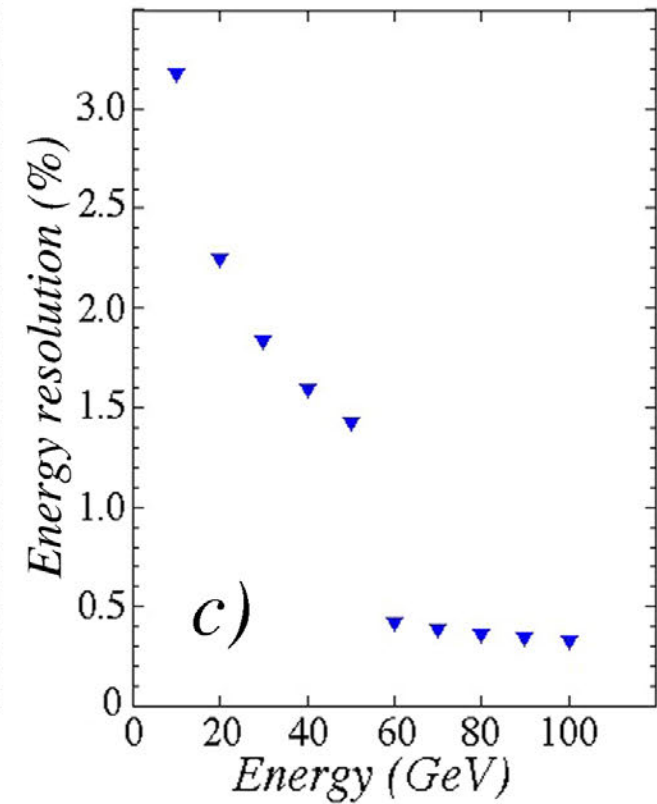
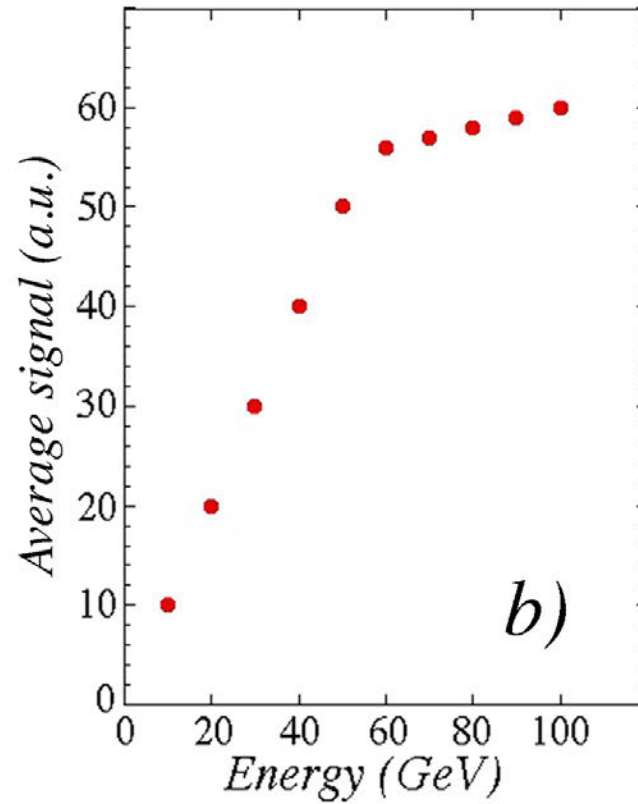
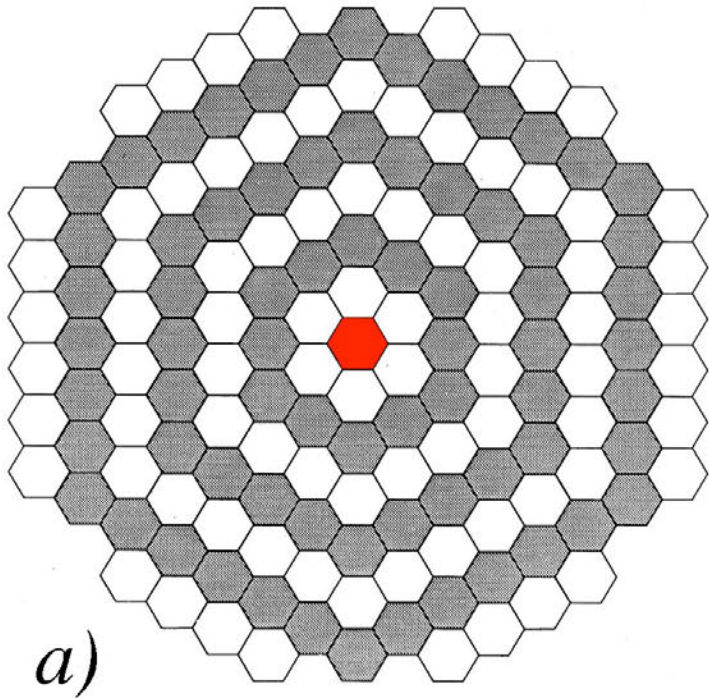
NIM A608 (2009) 372



Misconceptions about calorimetry

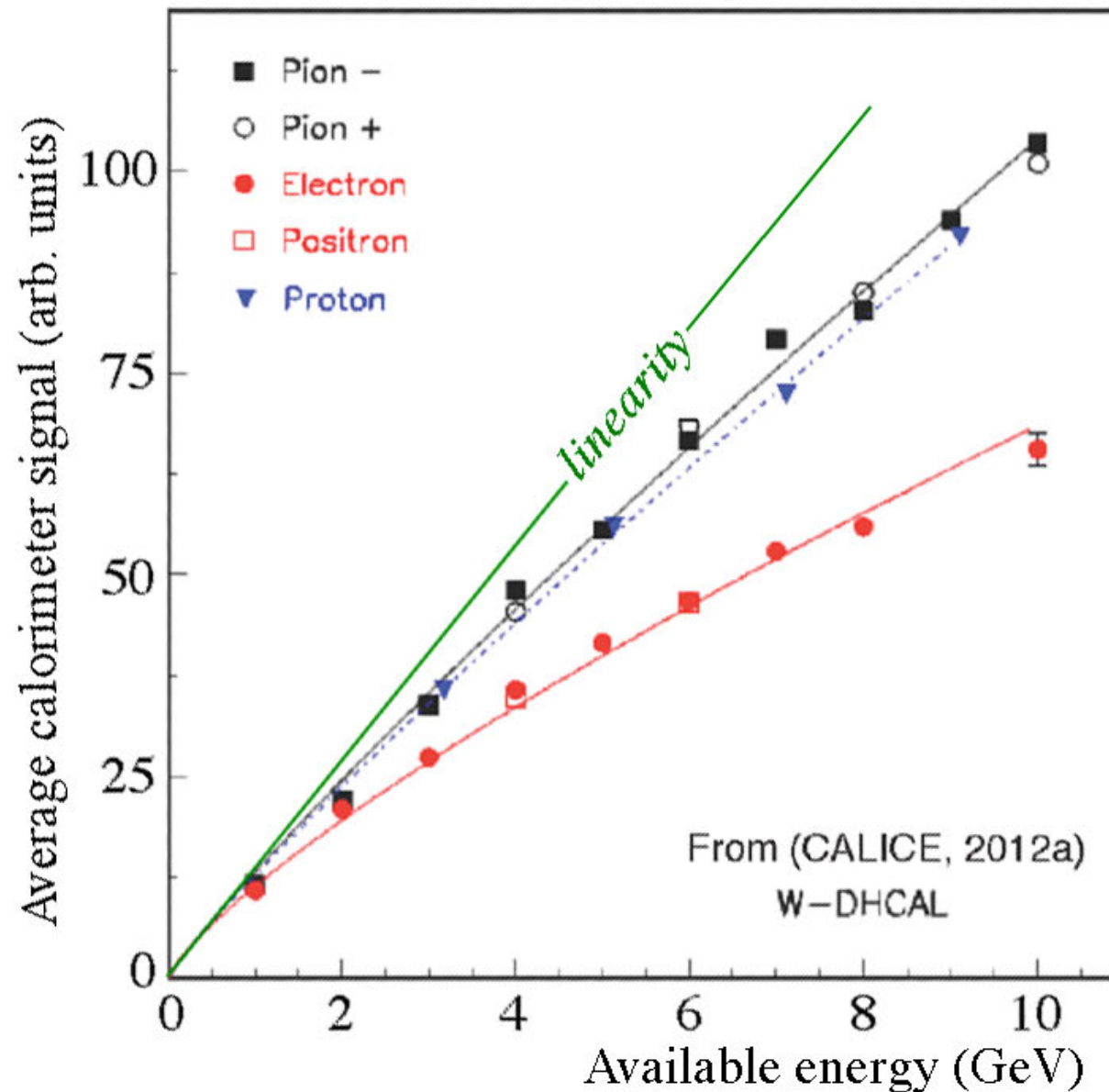
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- *Signal saturation does not matter*

Effects of signal saturation (SPACAL)



Signal saturation in the CALICE DHCAL (overcompensating @ < 10 GeV)

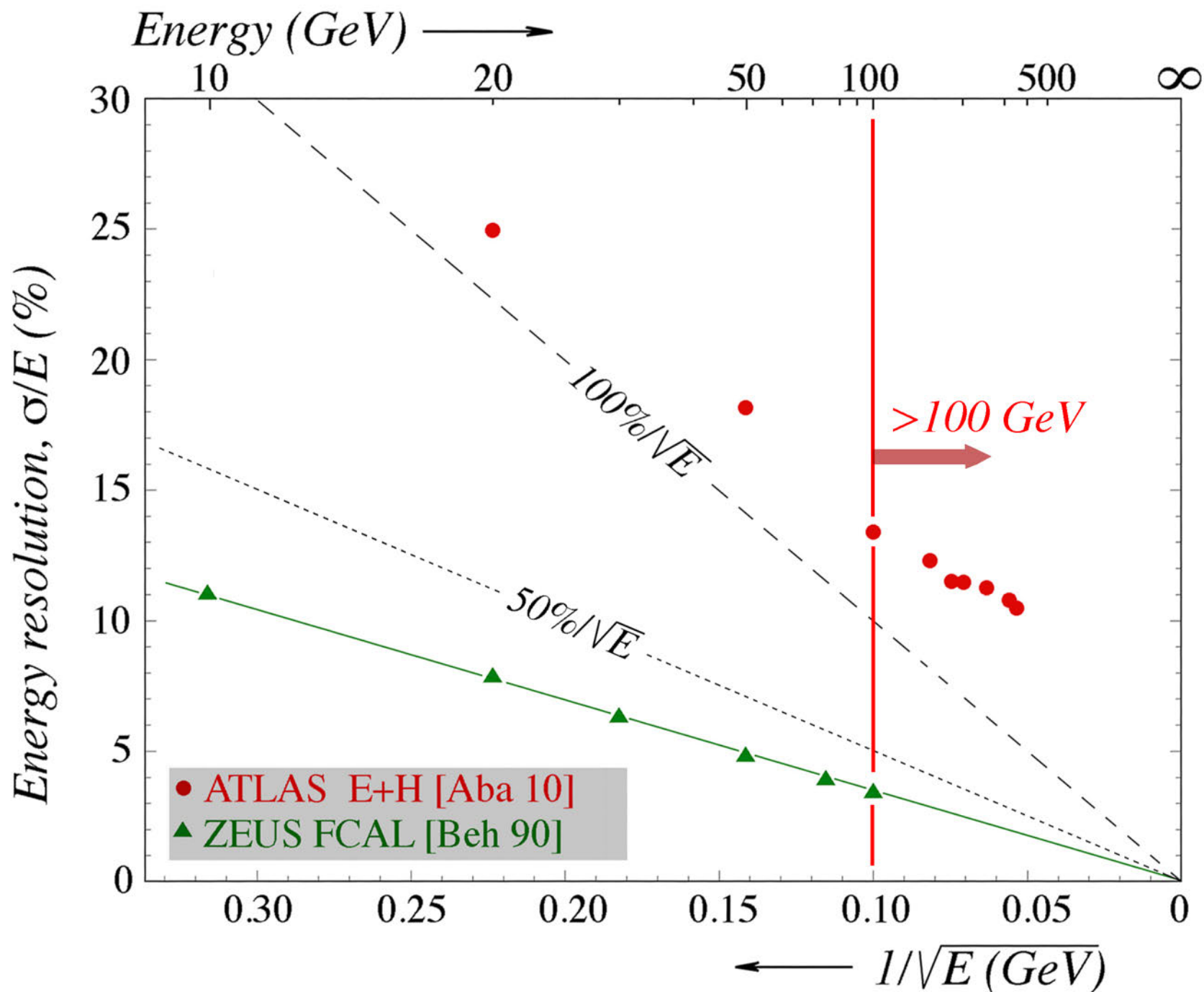
Rev. Mod. Phys. 88 (2015) 15003



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- *Energy resolution scales like $E^{-1/2}$*
- *Linearity \equiv you can fit a straight line through some data points*
- *Signal saturation does not matter*
- *Compensation would be nice, but is not really important*

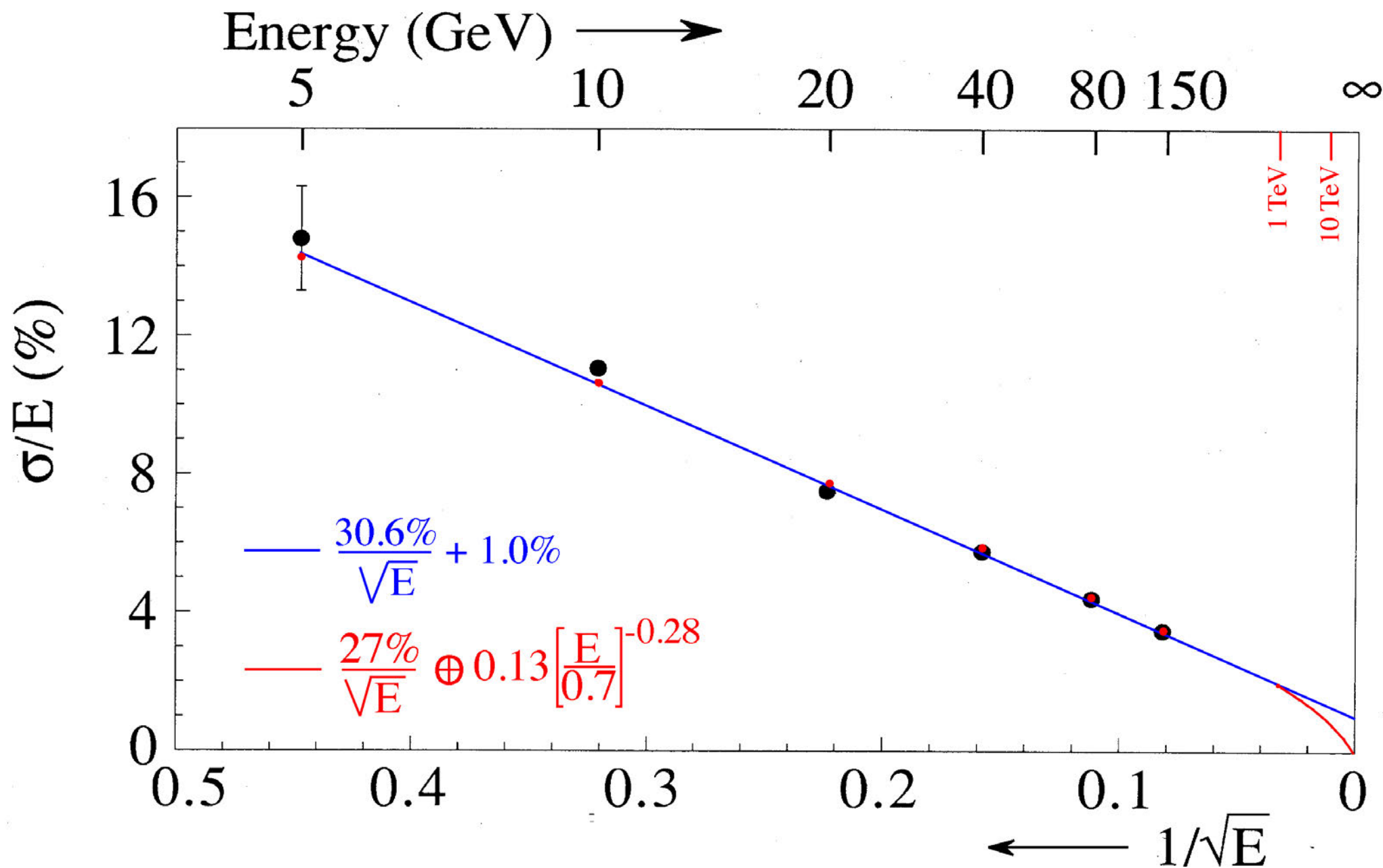
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Misconceptions about calorimetry

- *A shower is a collection of mips*
- *Energy resolution \equiv width of signal distribution*
- *Energy resolution scales like $E^{-1/2}$*
- *Linearity \equiv you can fit a straight line through some data points*
- *Signal saturation does not matter*
- *Compensation would be nice, but is not really important*
- *The only effect of non-compensation is a constant term in the energy resolution*

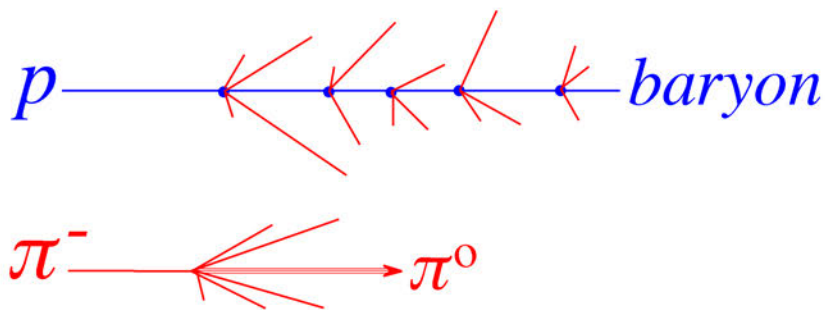
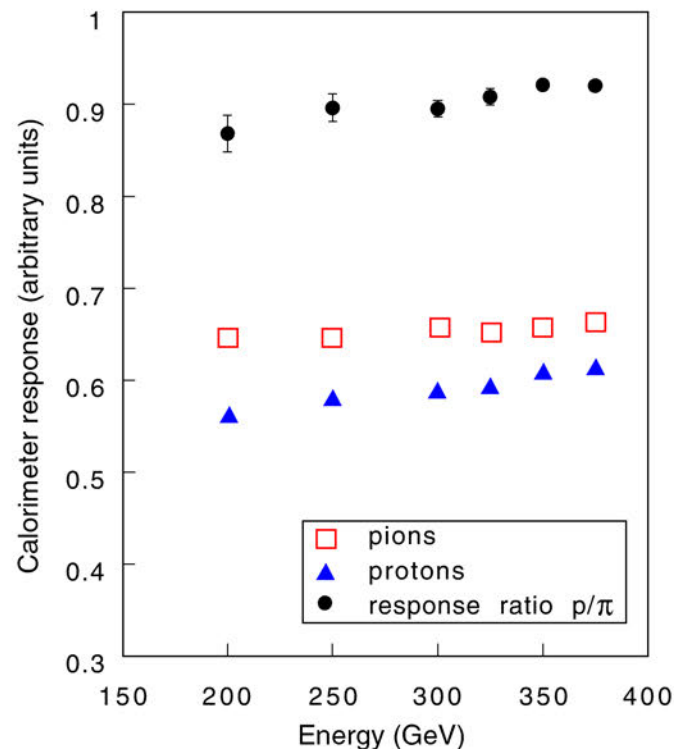
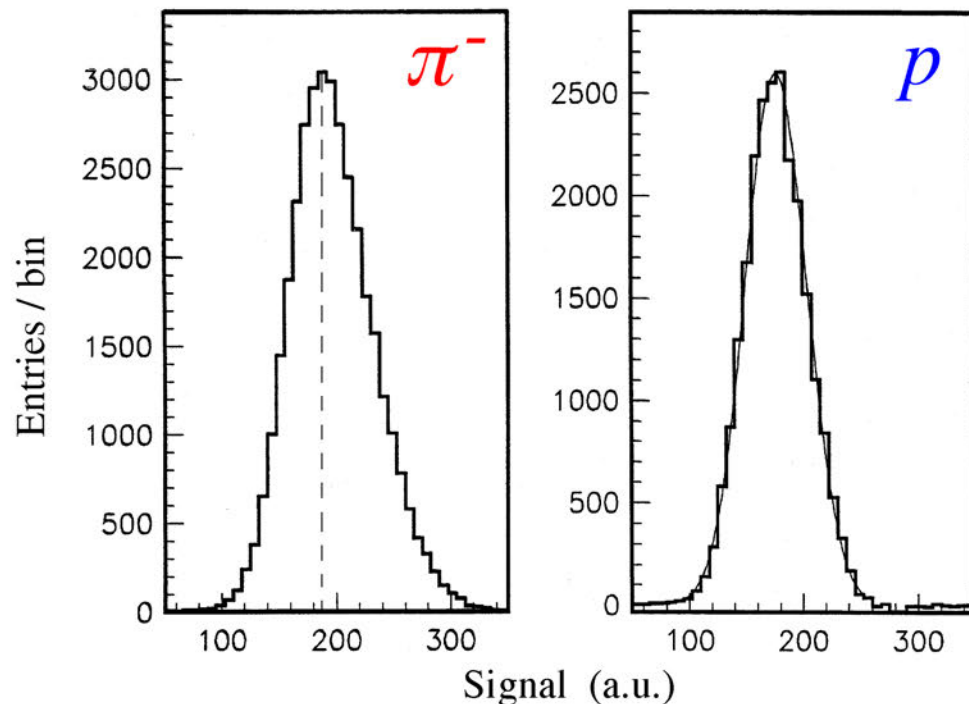
Difference only noticeable for $E > 1000 \text{ GeV}$



Misconceptions about calorimetry

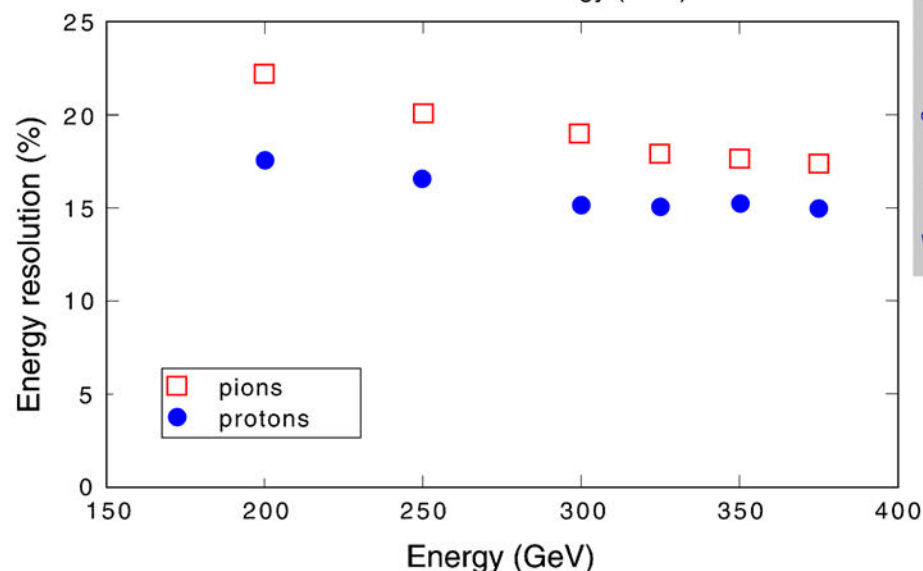
- *The only effect of non-compensation is a constant term in the energy resolution*
 - *Hadronic signal non-linearity*
 - *Non-Gaussian response functions*
 - *Different average signal for p , π , K*
 - *Calibration problems, especially if e/h (em) \neq e/h (had)*

Proton / pion differences in calorimeter signals caused by differences in em shower fraction characteristics



em fraction in p showers:

- smaller
- less fluctuations
- more symmetric
- less concentrated near axis



data from NIM A408 (1998) 380

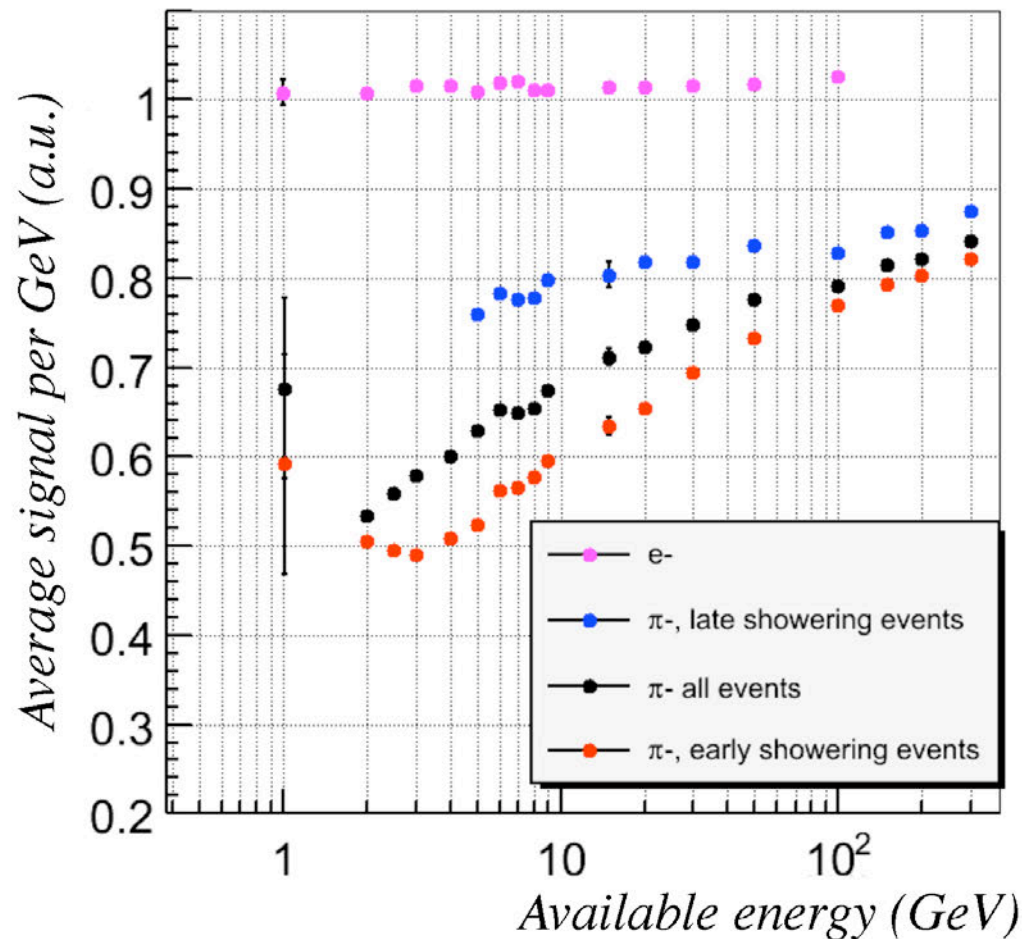
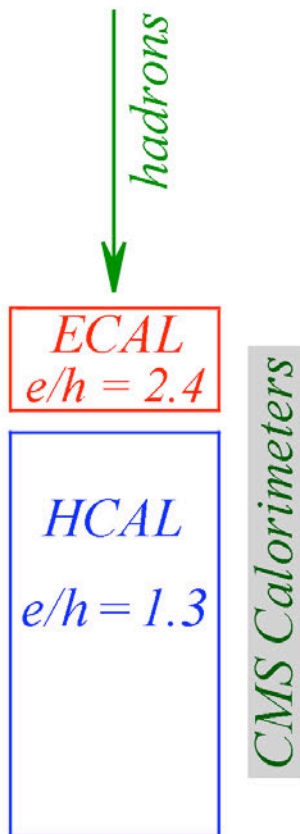
Consequences for LHC calorimeters

Hadronic response and signal linearity (CMS)

CMS pays a price for its focus on em energy resolution
ECAL has $e/h = 2.4$, while HCAL has $e/h = 1.3$

→ Response depends strongly on starting point shower

Data from: CMS note 2007/012



Misconceptions about calorimetry

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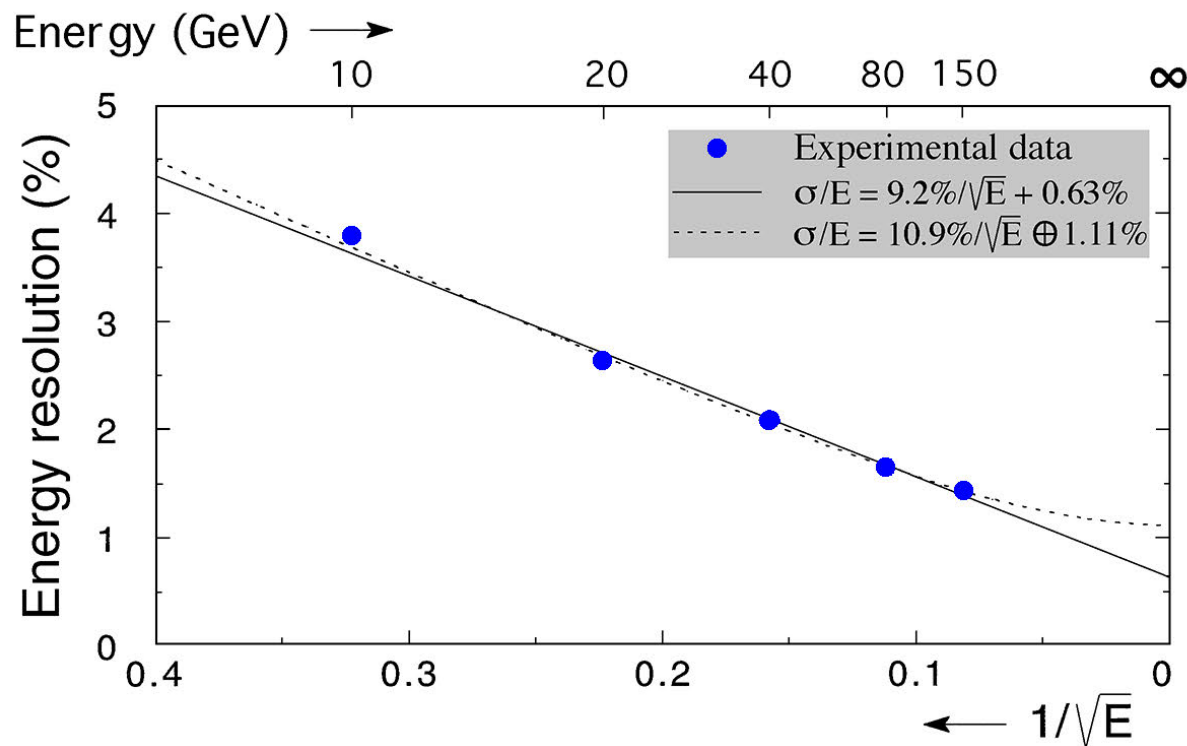
Options for the future

- *Intrinsically compensating calorimeters*
- *Dual-readout calorimeters*
- *Particle Flow Analysis systems*

A good alternative for future collider experiments (compensating em and had segments)

ECAL

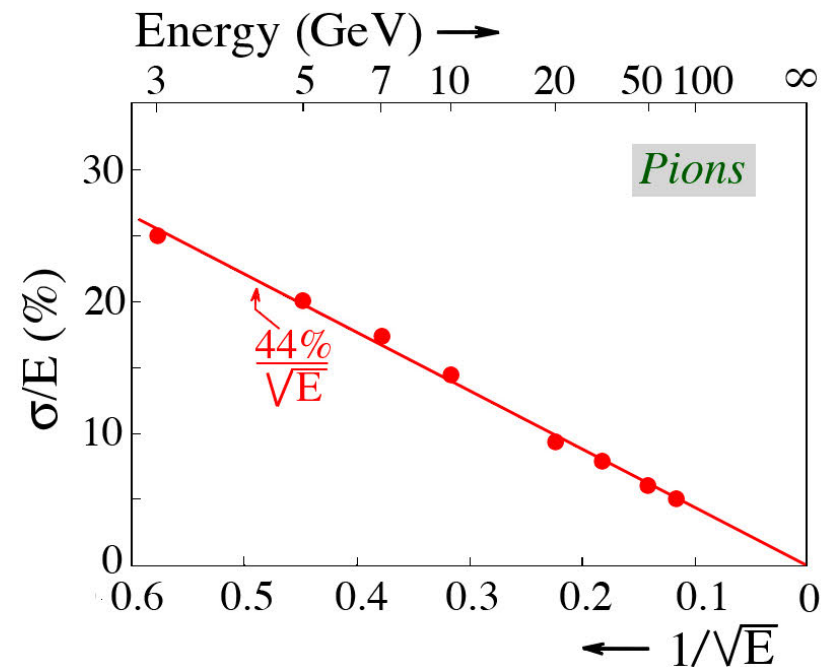
● Pb/fiber 4:1, 0.5 mm fibers (RD1)



NIM A337 (1994) 314

HCAL

● 10mm Pb/2.5mm scint [Bern87]



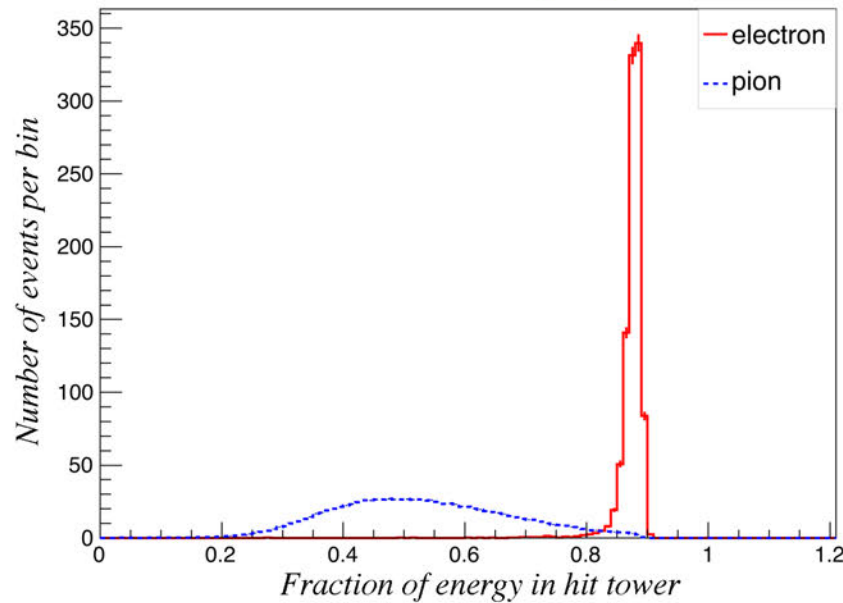
NIM A262 (1987) 229

Cu/fiber dual-readout calorimetry

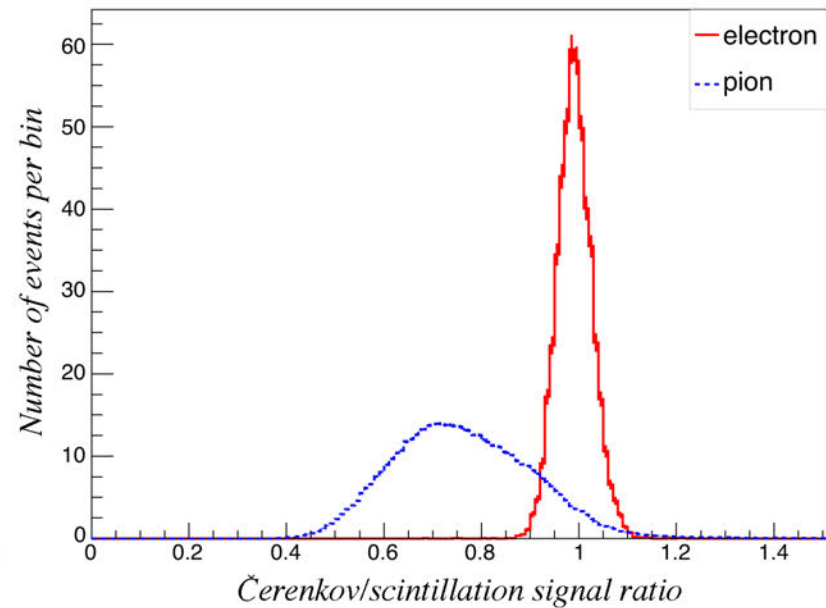
- *Excellent em and hadronic energy resolution*
- *Calibration is trivial*
- *Excellent particle-id in longitudinally unsegmented detector*
- *Ultrafast Cherenkov signals give unique timing options*

Methods to distinguish e/π in longitudinally unsegmented calorimeter

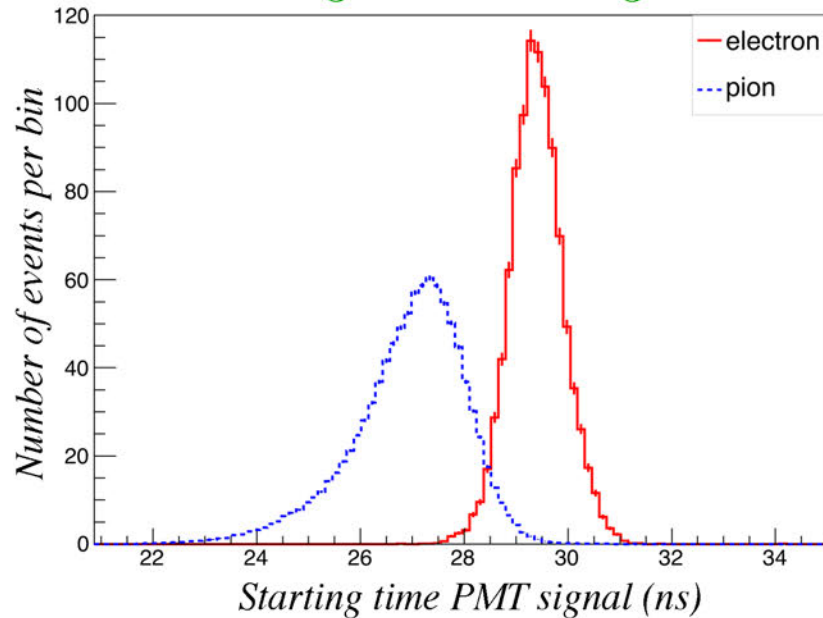
Lateral shower profile



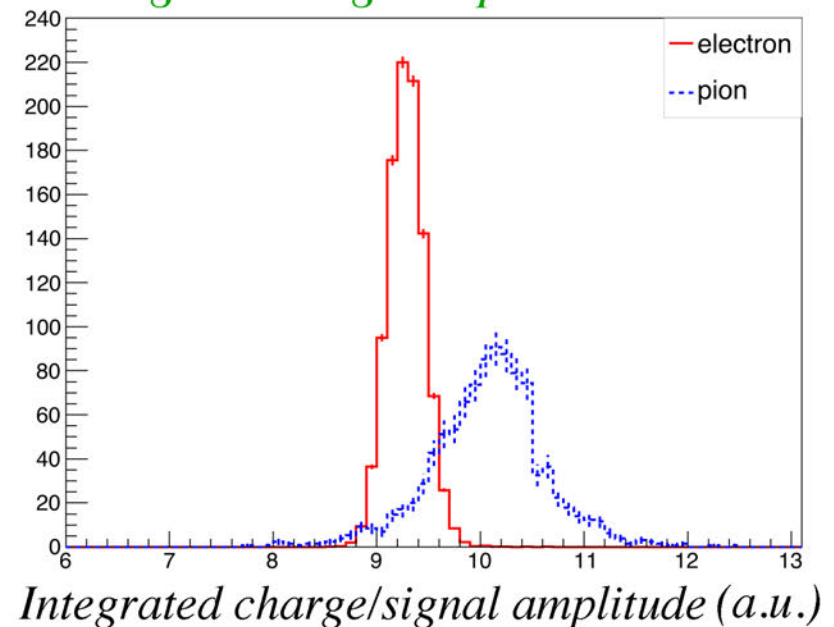
Difference C/S signals



Starting time PMT signal



Signal charge/amplitude ratio



NIM A735 (2014) 120

Combination of cuts: $>99\%$ electron efficiency, $<0.2\%$ pion mis-ID

Particle Flow Analysis

Particle Flow Analysis

- *The basic idea*

Combine the information of the tracker and the calorimeter system to determine the jet energy

Momenta of charged jet fragments are determined with the tracker

Energies of the neutral jet fragments come from the calorimeter

- *This principle has been used successfully to improve the hadronic performance of experiments with poor hadronic calorimetry*

However, the improvements are fundamentally limited

In particular, no one has ever come close to separating W/Z this way

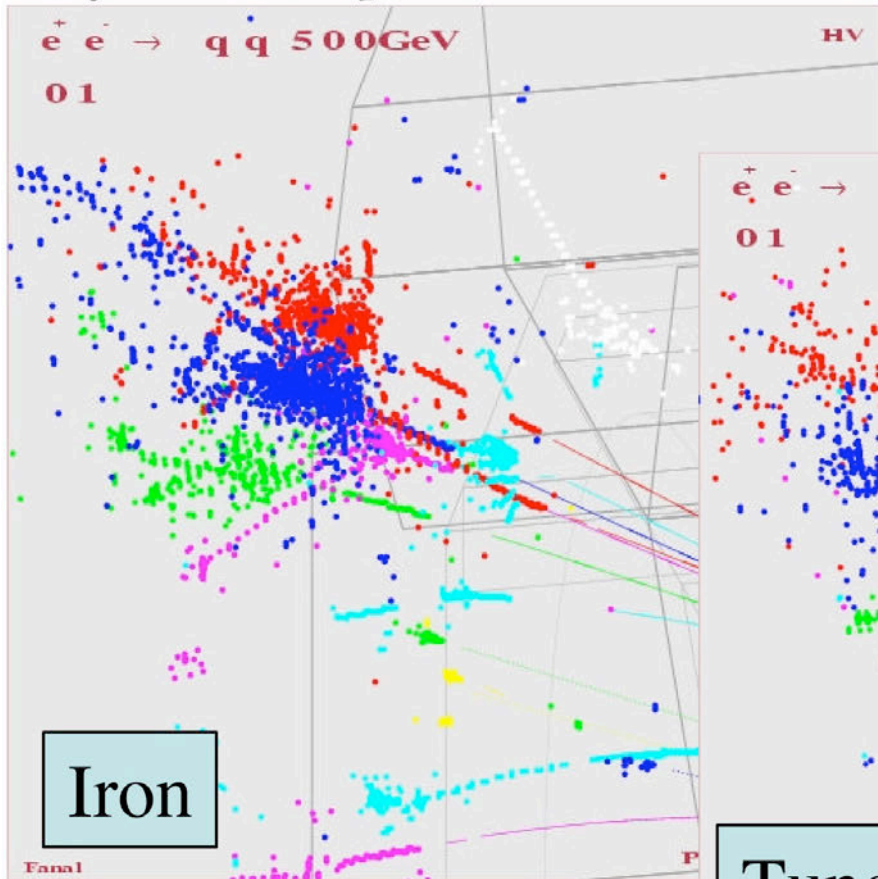
- *The problem*

The calorimeters do not know that the charged jet fragments have already been measured by the tracker. These fragments are also absorbed in the calorimeter. Confusion: Which part of the calorimeter signals comes from the neutral jet fragments?

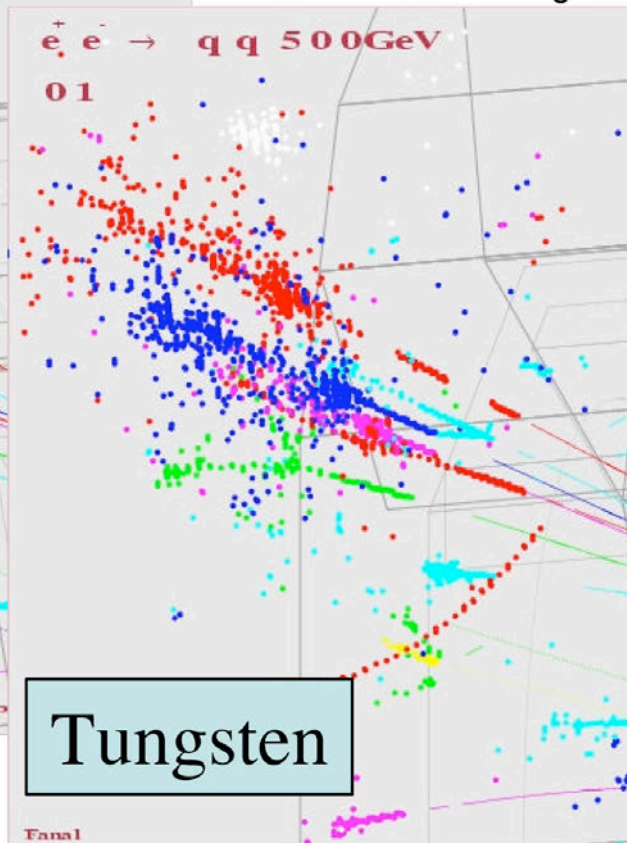
- *Advocates of this method claim that a fine detector granularity will help solve this problem. Others believe it would only create more confusion. Like with all other issues in calorimetry, this issue has to be settled by means of experiments, NOT by Monte Carlo simulations!!*

Pink Pion Physics

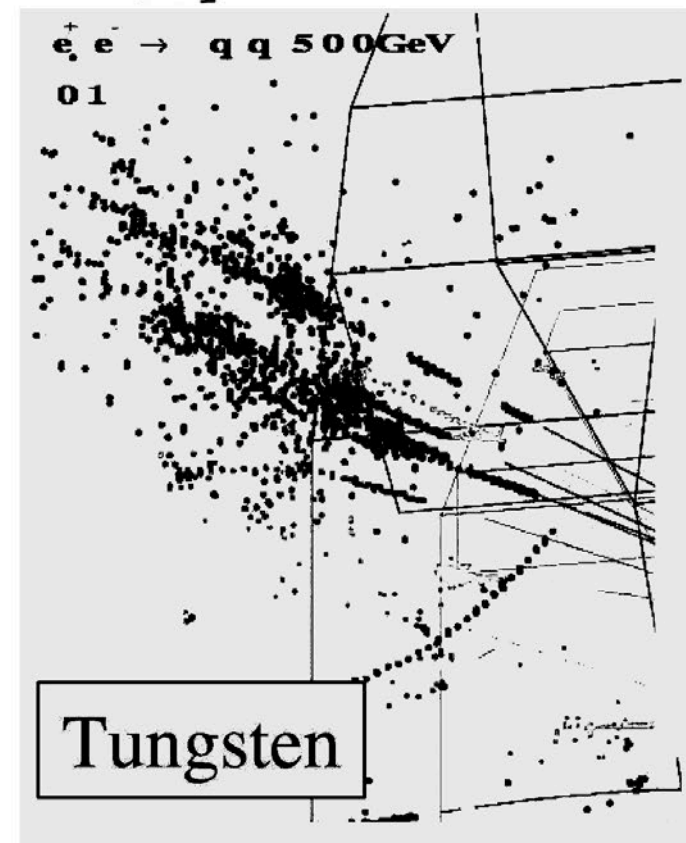
$$X_0 = 1.8\text{cm}, \lambda_I = 17\text{cm}$$



(images courtesy H.Videau)



$$X_0 = 0.35\text{cm}, \lambda_I = 9.6\text{cm}$$



A frequently used, but misleading argument

- The fact that 65% of the jet energy is measured with excellent precision in the tracker is **irrelevant***

In our detectors, the charged tracks are better measured than photon(s)
which are themselves better measured than neutral hadron(s)

Resolution on the charged track(s)	$\Delta p/p \sim \text{qq } 10^{-5}$
Resolution on the photon(s)	$\Delta E/E \sim 12\%$
Resolution on the h^0	$\Delta E/E \sim 45\%$

$$\begin{array}{l} E_{\text{jet}} = E_{\text{charged tracks}} + E_{\gamma} + E_{h^0} \\ \text{fraction} \quad 65\% \quad 26\% \quad 9\% \end{array}$$

From:
J.C. Brient
CALOR 08

*What matters for the jet energy resolution are the **fluctuations** in this 65%.*

In the absence of a calorimeter, one should therefore not expect to be able to measure jet energy resolutions better than 25–30% on the basis of tracker information alone, *at any energy*. And

From: NIM A495 (2002) 107

Hadronic calorimeter prototype

Vienna Conference on Instrumentation
NIM A732 (2013) 466



Absorber: Tungsten or Steel

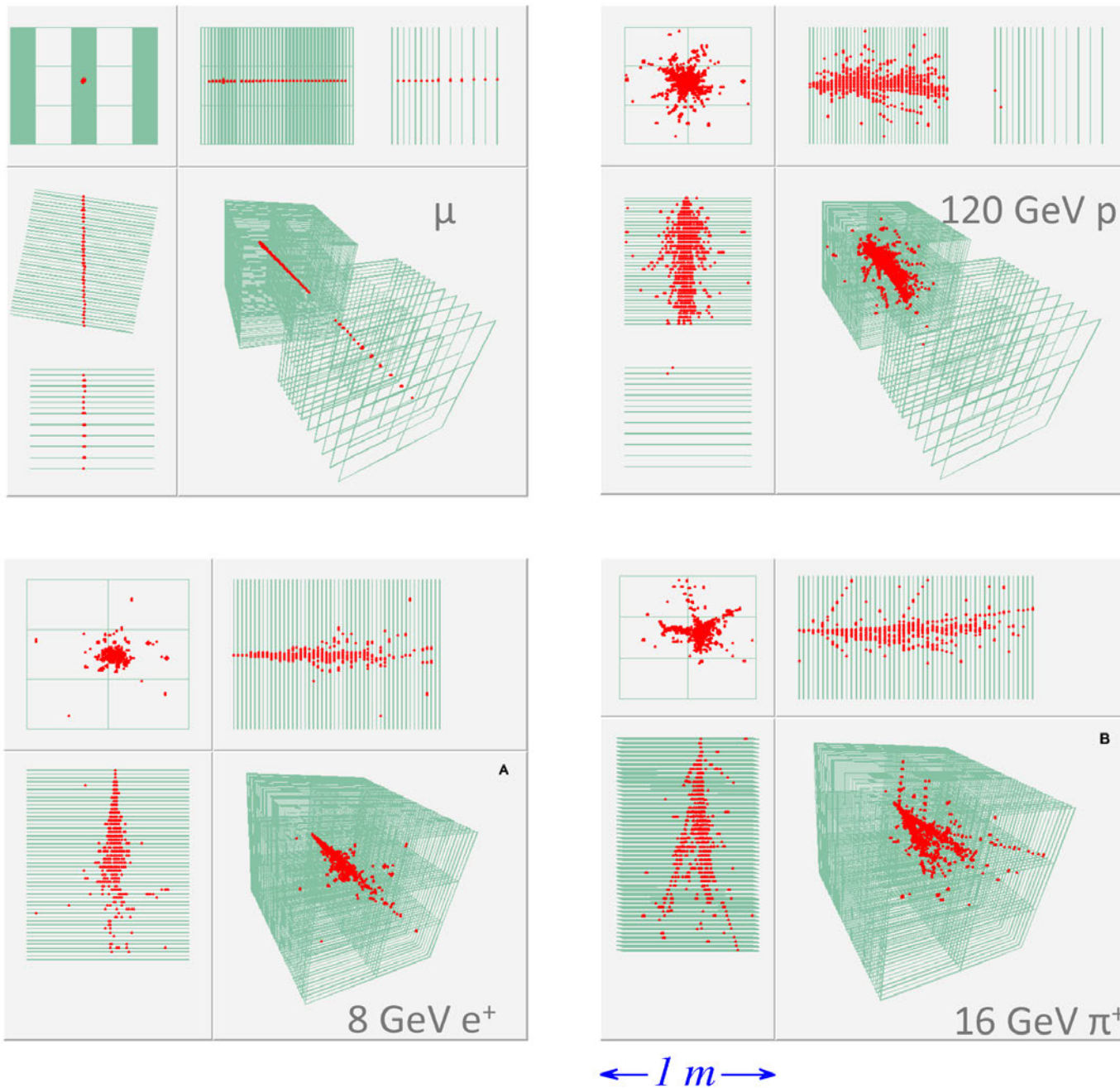
Digital readout: RPCs ($1 \times 1 \text{ cm}^2$)

Dimensions: 54 layers, $1 \times 1 \text{ m}^2$

$\sim 500,000$ readout channels !!

Tested at CERN/FNAL, e/π 10 - 300 GeV

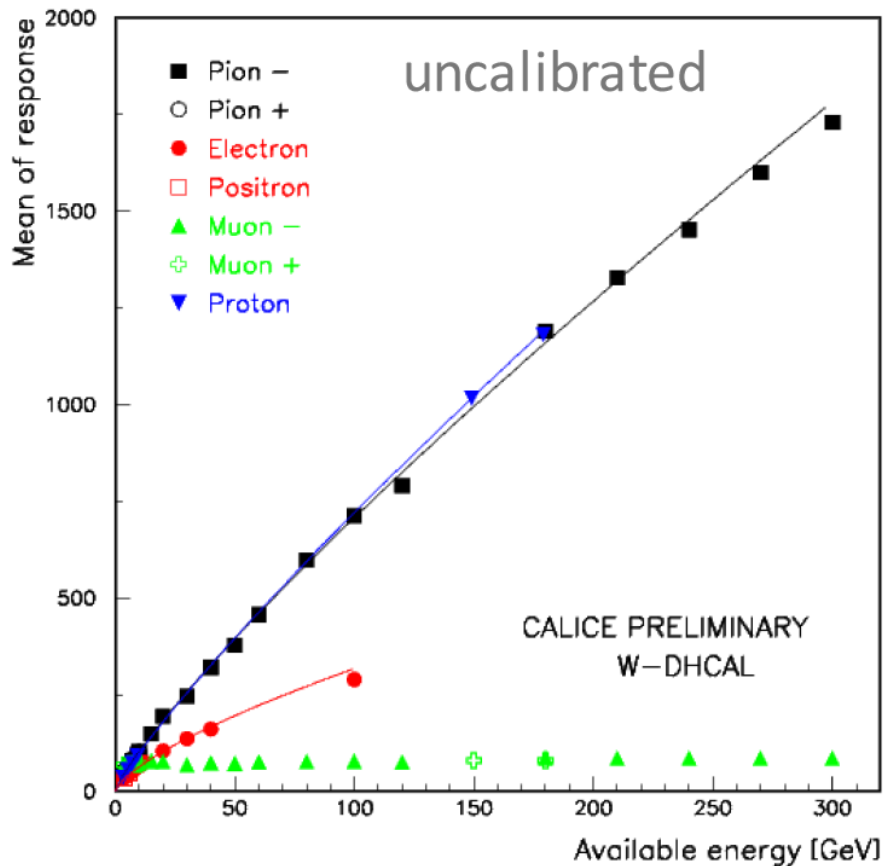
Some events displays of the CALICE DHCAL



There exists no such thing as a TYPICAL event profile

Test results digital hadron calorimeter CALICE

Tungsten – DHCAL



Non-linear response
to both e^\pm and hadrons

Both well described by
power law $\propto E^\beta$

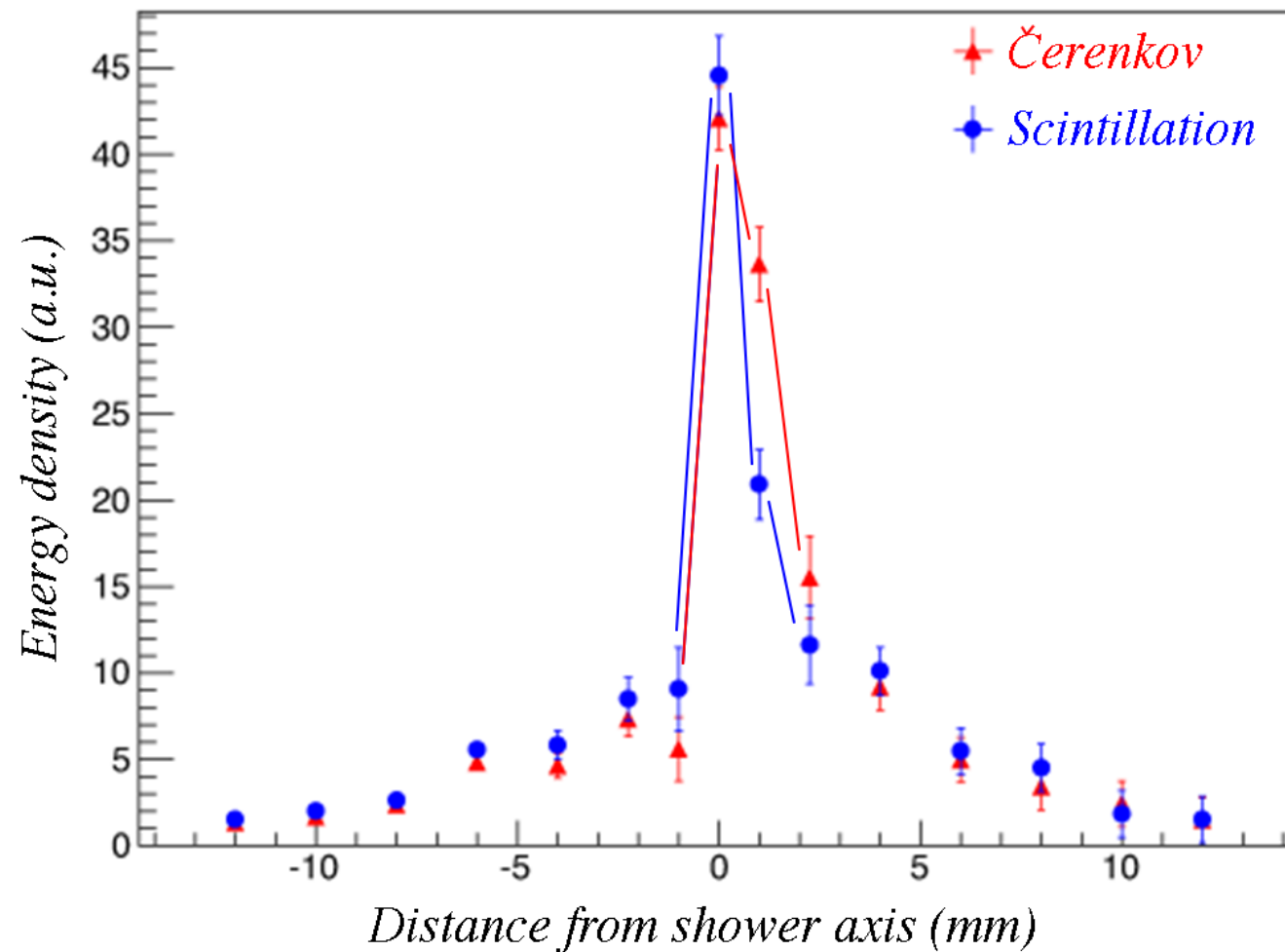
Badly over-compensating

$e/h \sim 0.9 - 0.5$

→ need smaller readout pads **!!!!**

The extremely narrow electromagnetic shower profile

Lateral shower profile



Fundamental problems with PFA

- *Calibration?!*
- *Non-linearity (saturation effects)*
- *Texas towers*

Unfortunately, the proponents of PFA are not interested in these issues, and only study engineering problems

Misconceptions about calorimetry

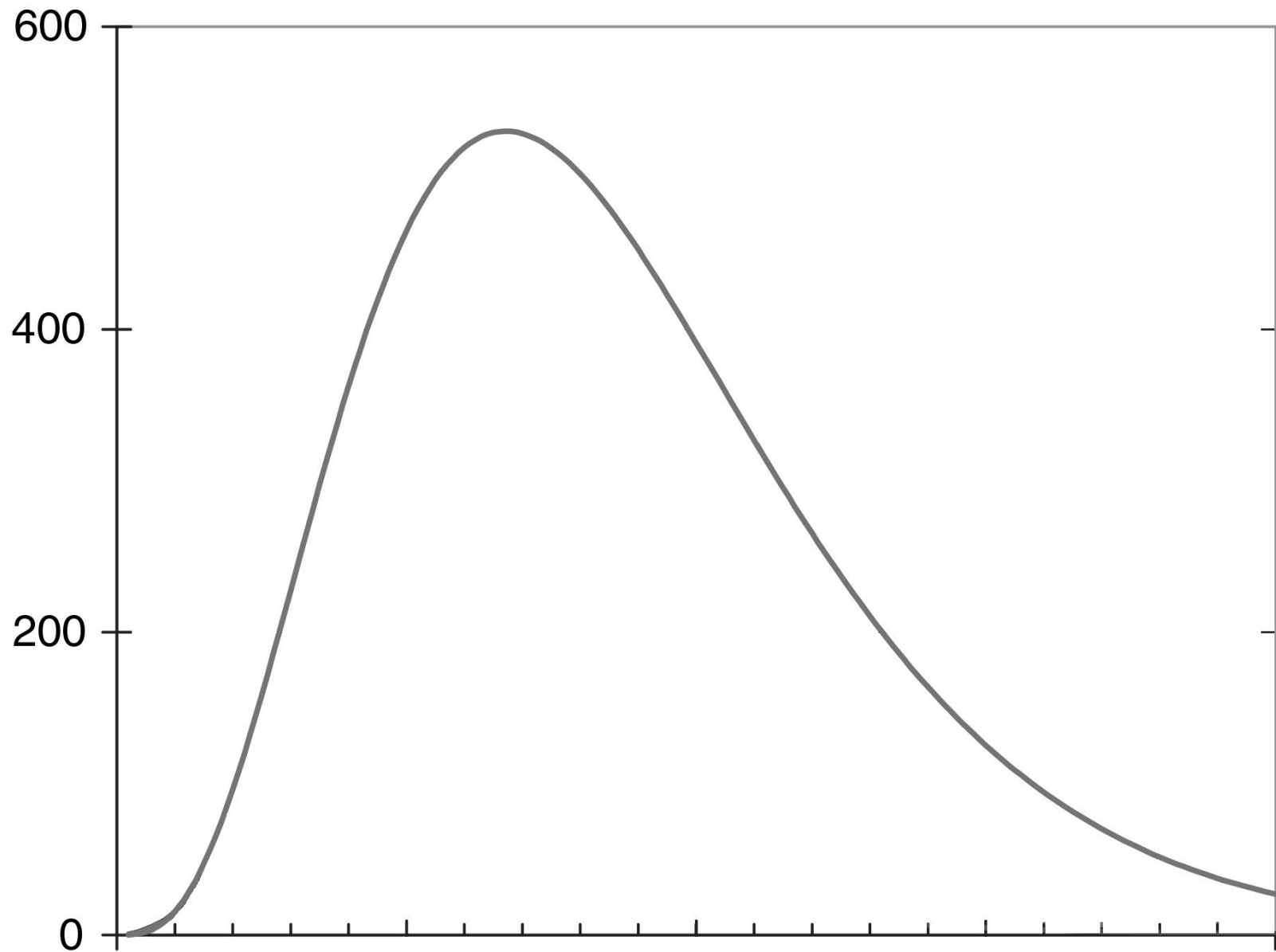
- *A shower is a collection of mips*
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 - *Signal saturation does not matter*
 - *Compensation would be nice, but is not really important*
 - *The only effect of non-compensation is a constant term in the energy resolution*
 - *ALL CALORIMETER PROBLEMS CAN BE SOLVED OFFLINE*
- *Pretend everything is OK*
Build those calorimeter systems with 10^8 channels
Leave it to future generations to solve the mess

The future of calorimetry in high energy physics

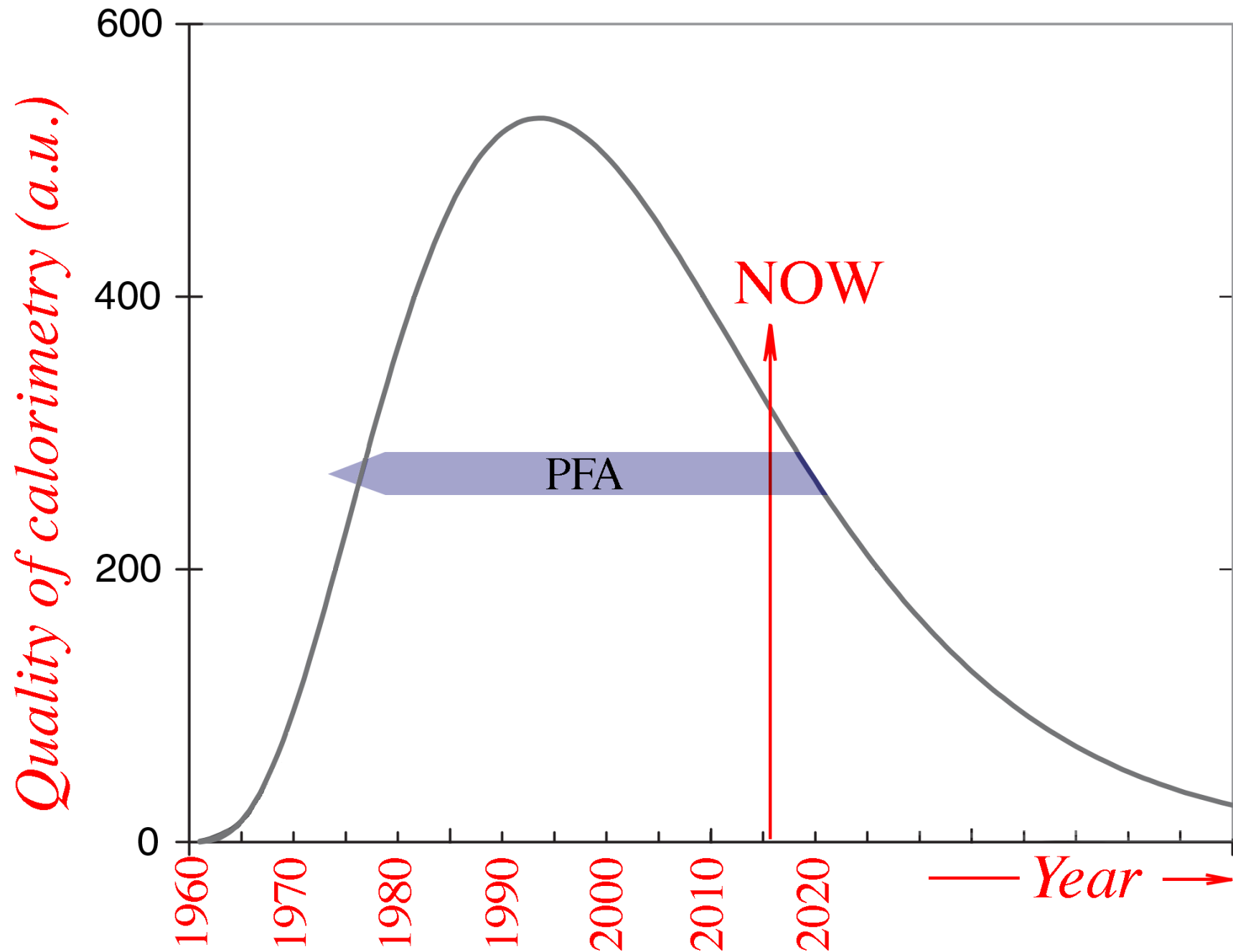
- *No funding available for generic R&D*
- *Ignorance, misconceptions + lack of interest for crucial issues*
- *Belief that all problems can be solved with technology (W, Si, RPC)*

⇒ The future looks bleak (imho)

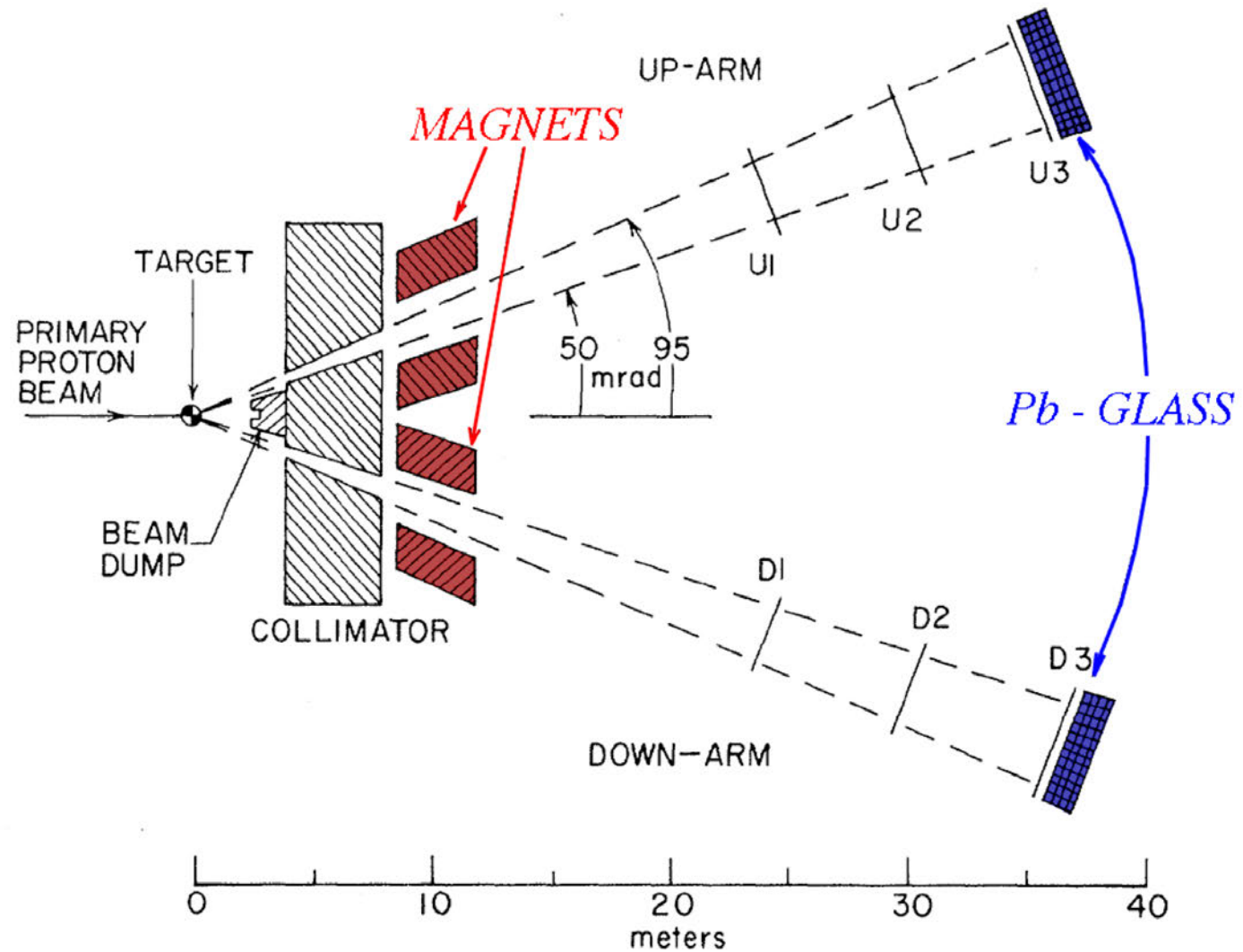
Where do we go from here?



The future of calorimetry in HEP experiments



1970s - Shower counters in magnetic spectrometers

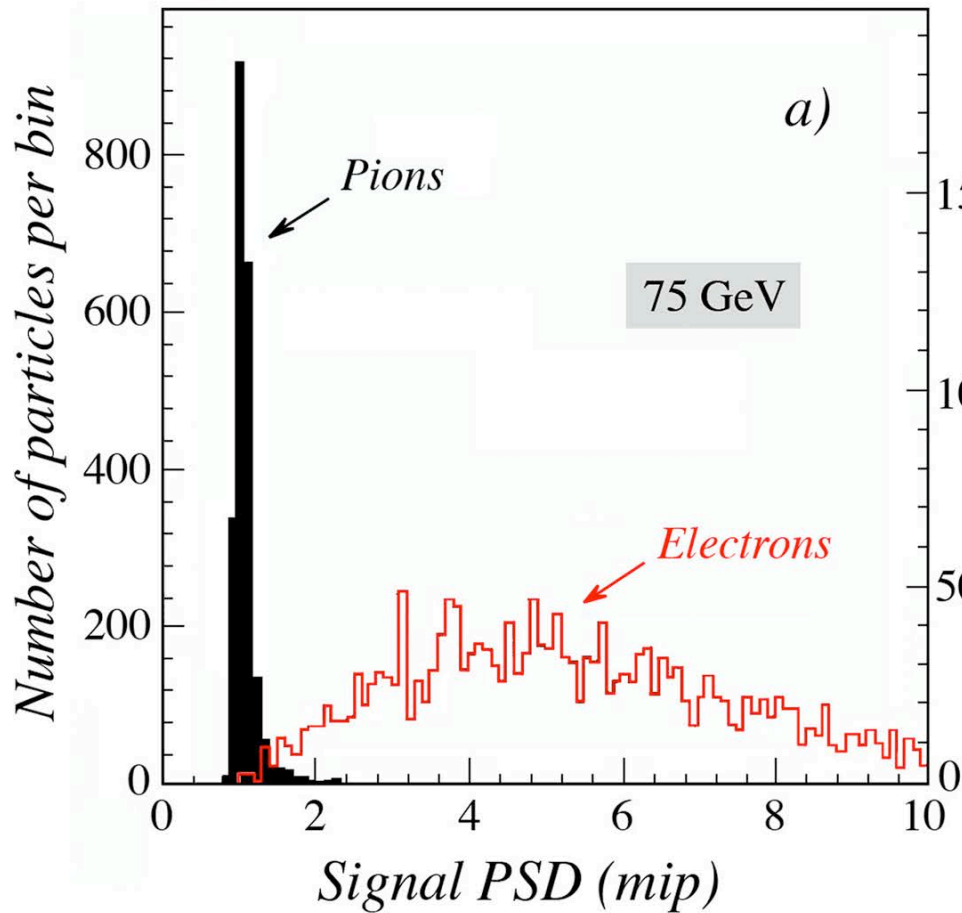


However, in modern 4π experiments the showers start after $< 2\text{m}$, instead of 40m

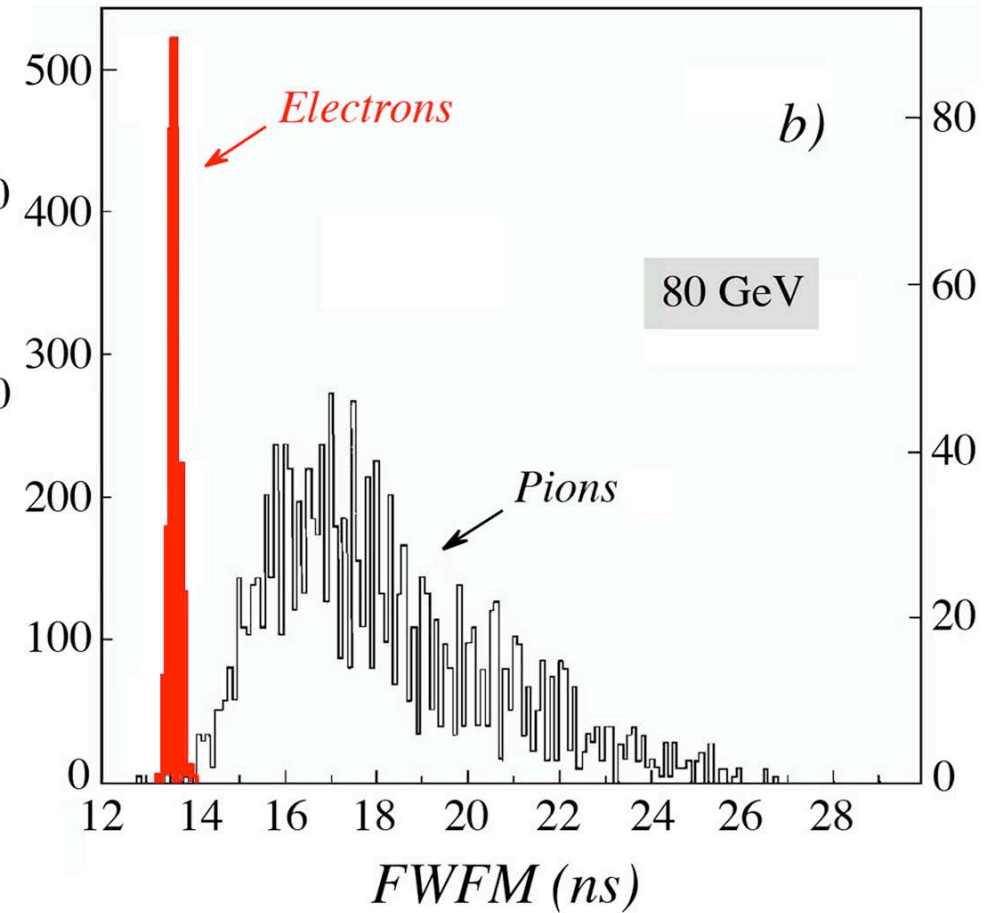
Backup slides

Particle identification with calorimeters

*Using shower profile
(pre-shower detector)*



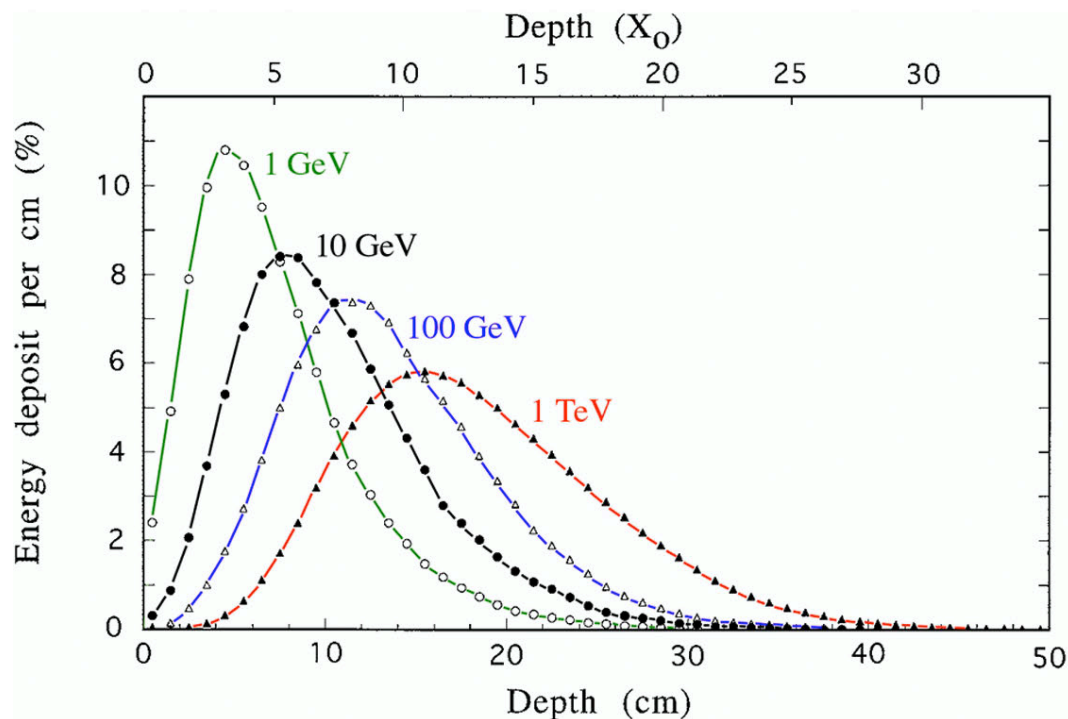
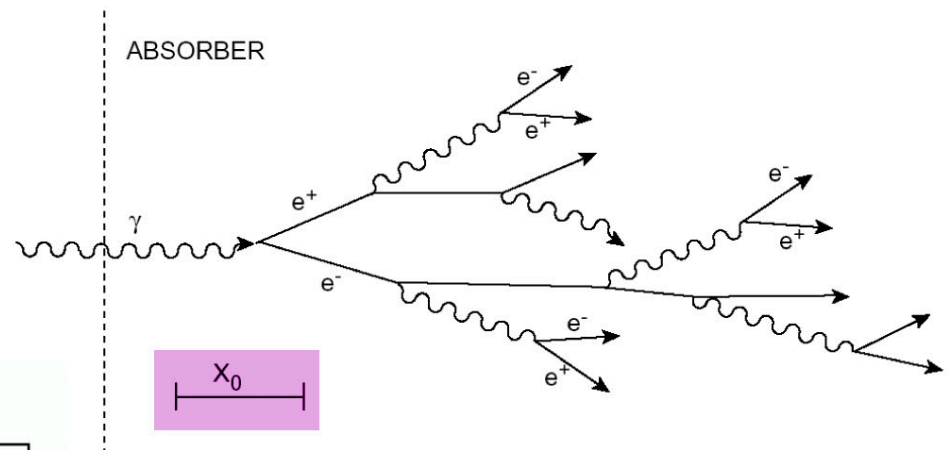
*Using time structure
of the signals*



Calorimeters

Electromagnetic shower development

When a high-energy electron or photon enters a calorimeter, its energy is absorbed in a cascade of processes in which many different “shower” particles are produced.



The shower development is governed by the “radiation length” X_0 , which is typically ~ 1 cm

Even very-high-energy particles are absorbed in relatively small detectors (99% of 100 GeV e^- in 10 kg)

The physics of hadronic shower development

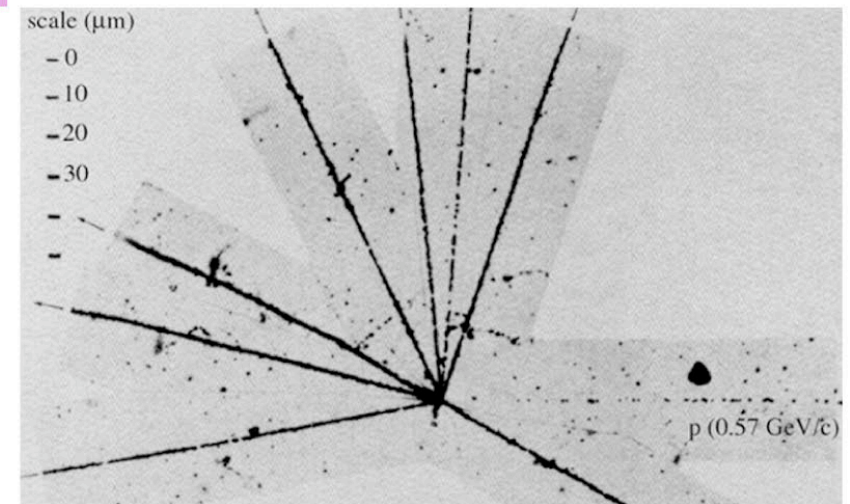
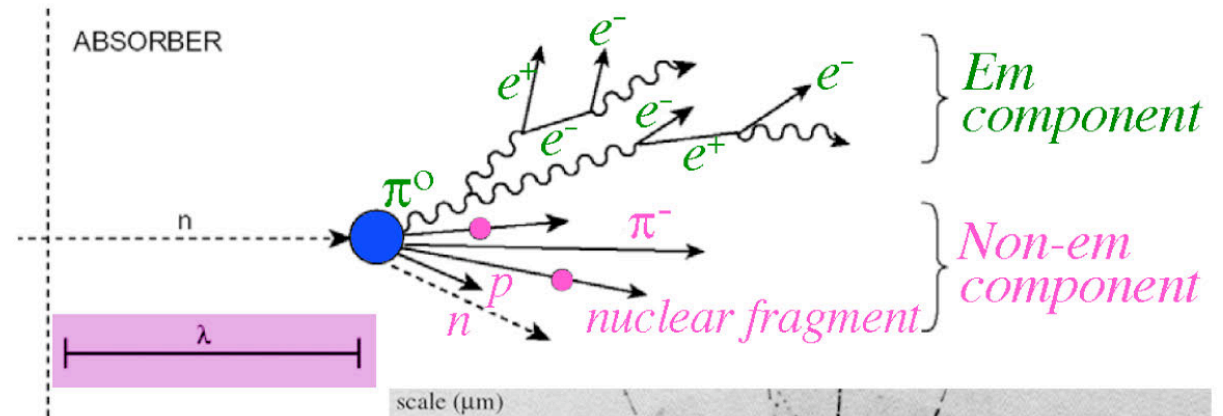
- A hadronic shower consists of two components

- **Electromagnetic component**

- electrons, photons
- neutral pions $\rightarrow 2 \gamma$

- **Hadronic (non-em) component**

- charged hadrons π^\pm, K^\pm (20%)
- nuclear fragments, p (25%)
- neutrons, soft γ 's (15%)
- break-up of nuclei (“invisible”) (40%)

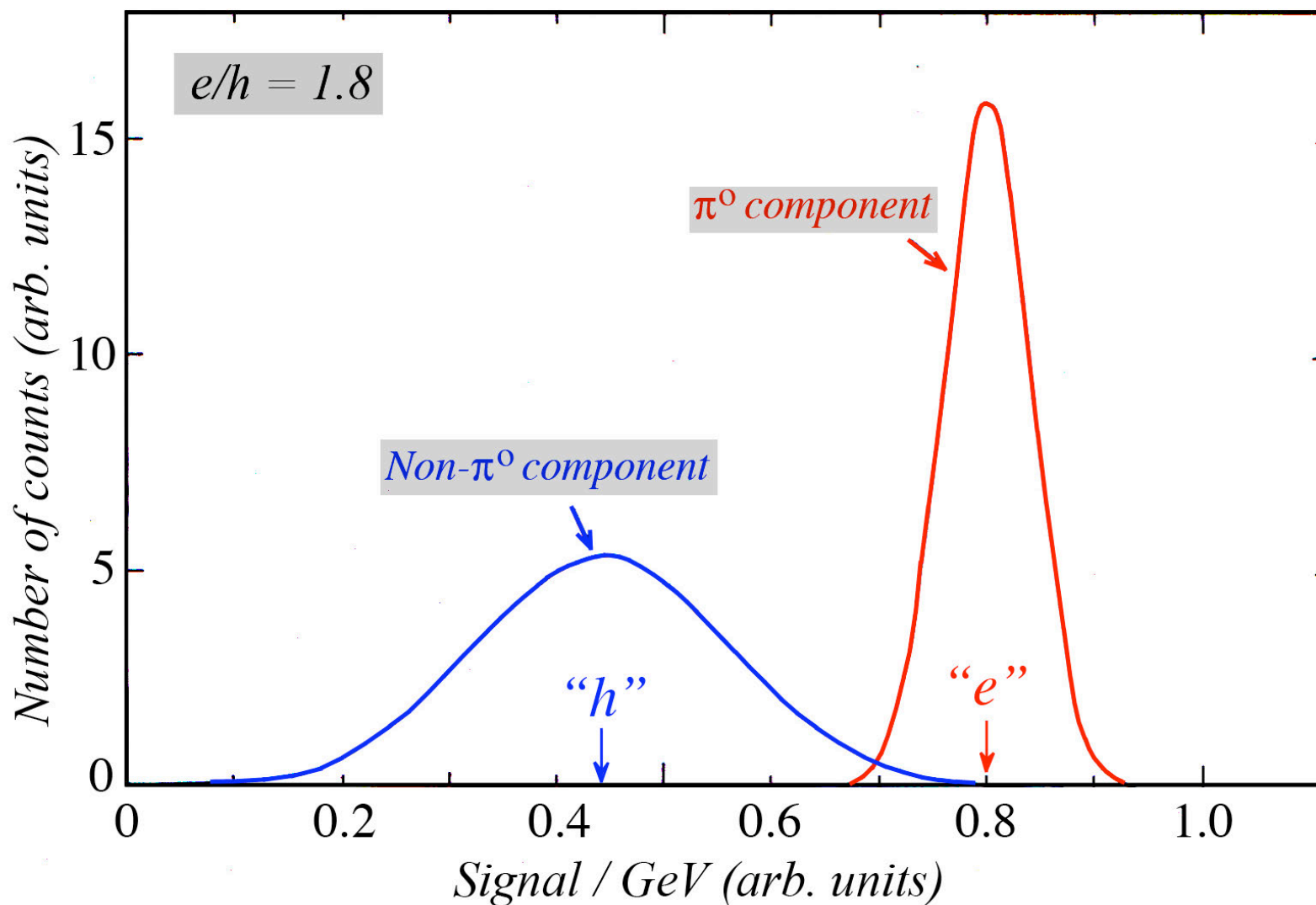


- Important characteristics for hadron calorimetry:

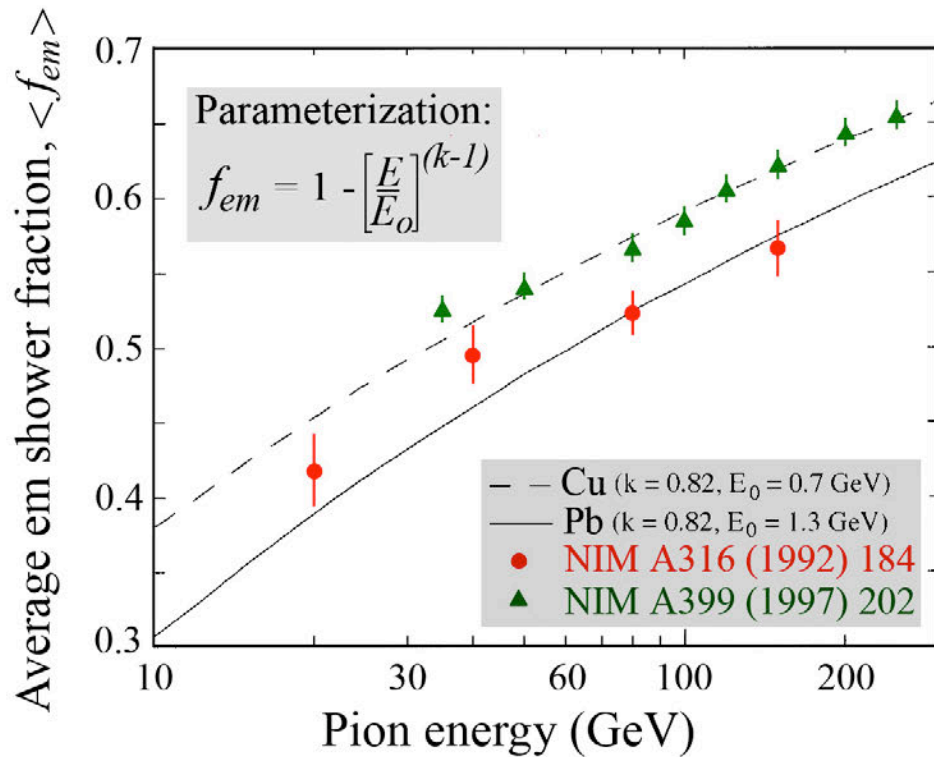
- Large, non-Gaussian fluctuations in energy sharing em/non-em
- Large, non-Gaussian fluctuations in “invisible” energy losses

*The calorimeter response to the two shower components
is NOT the same*

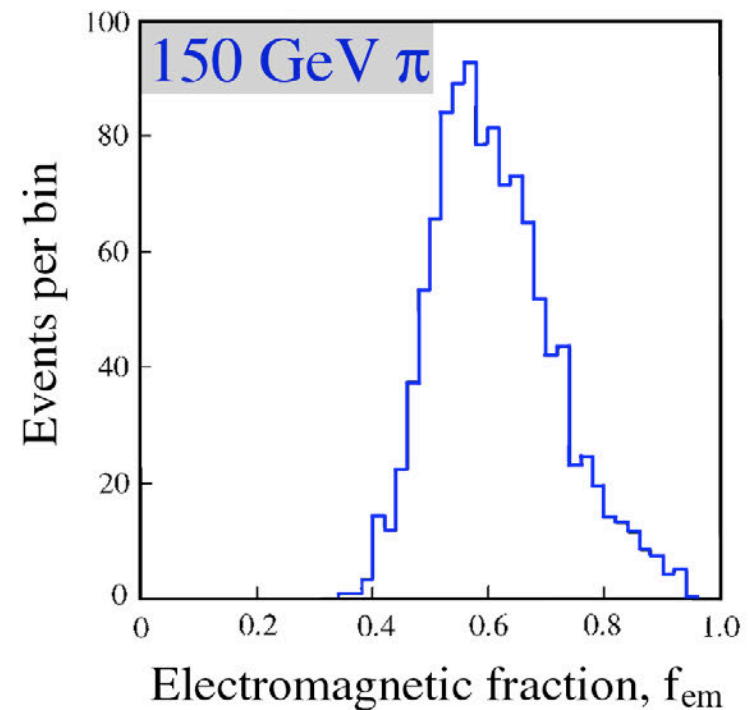
(mainly because of nuclear breakup energy losses in non- π^0 component)



(Fluctuations in) the electromagnetic shower fraction, f_{em}
i.e. the fraction of the shower energy deposited by π^0 s



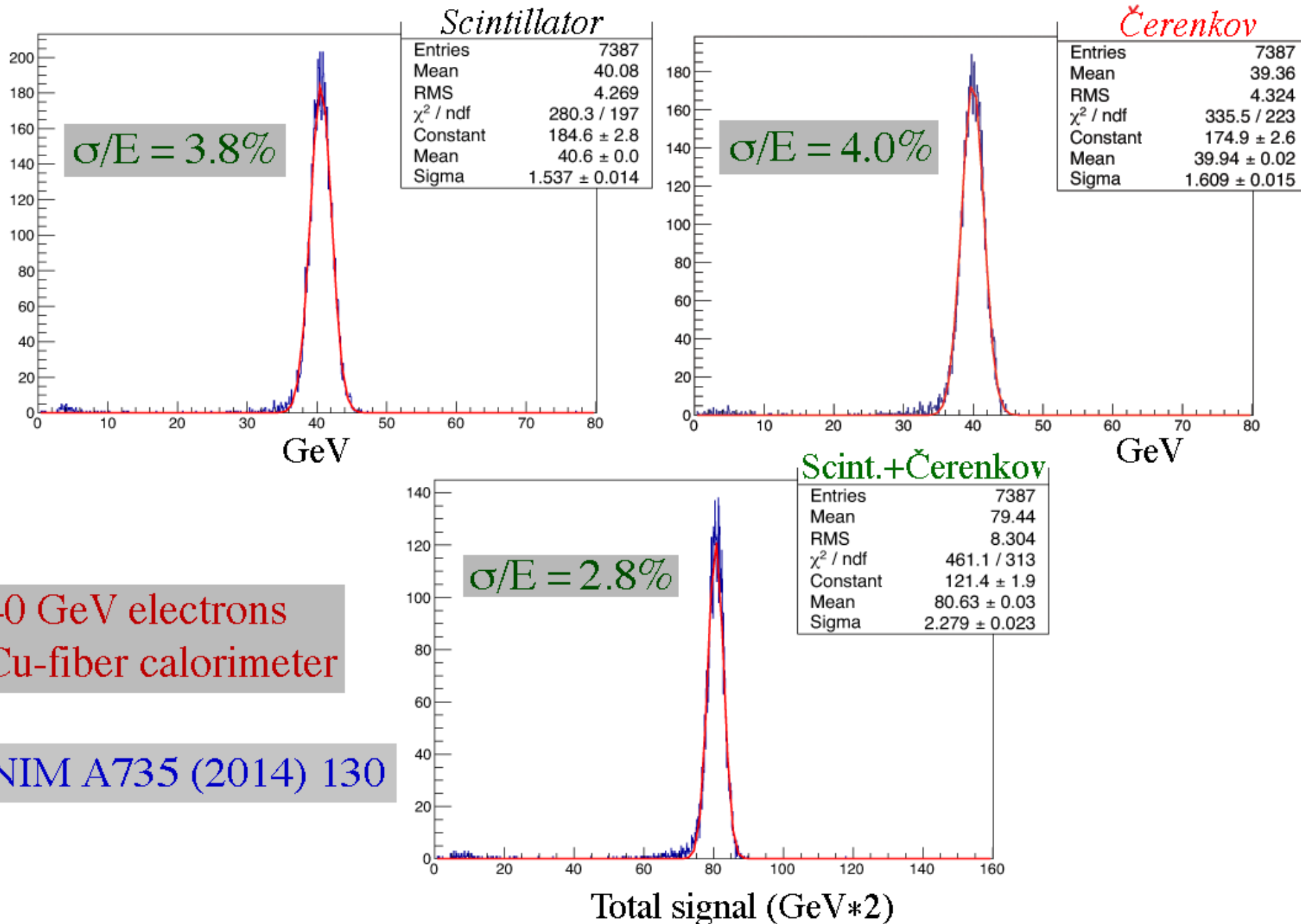
The em fraction is, on average,
large and energy dependent



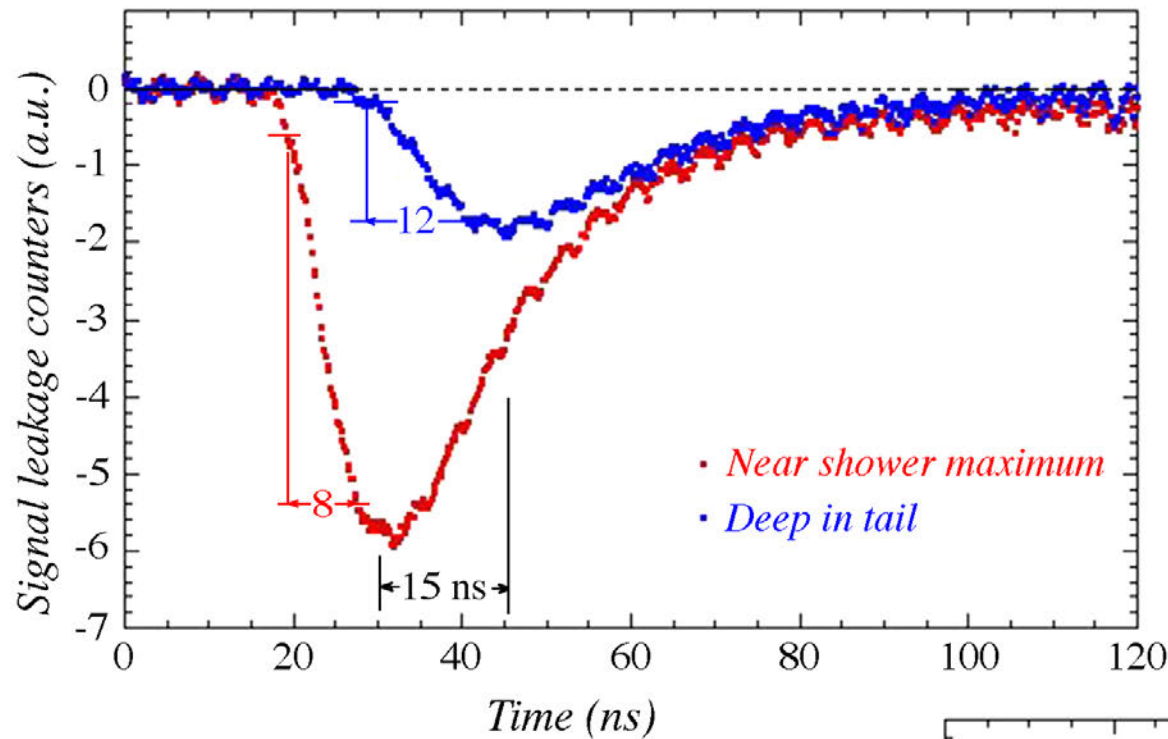
Fluctuations in f_{em} are
large and non-Poissonian

S and Č signals sample the showers independently

Resolution improves by combining



Comparison signal shapes leakage counters

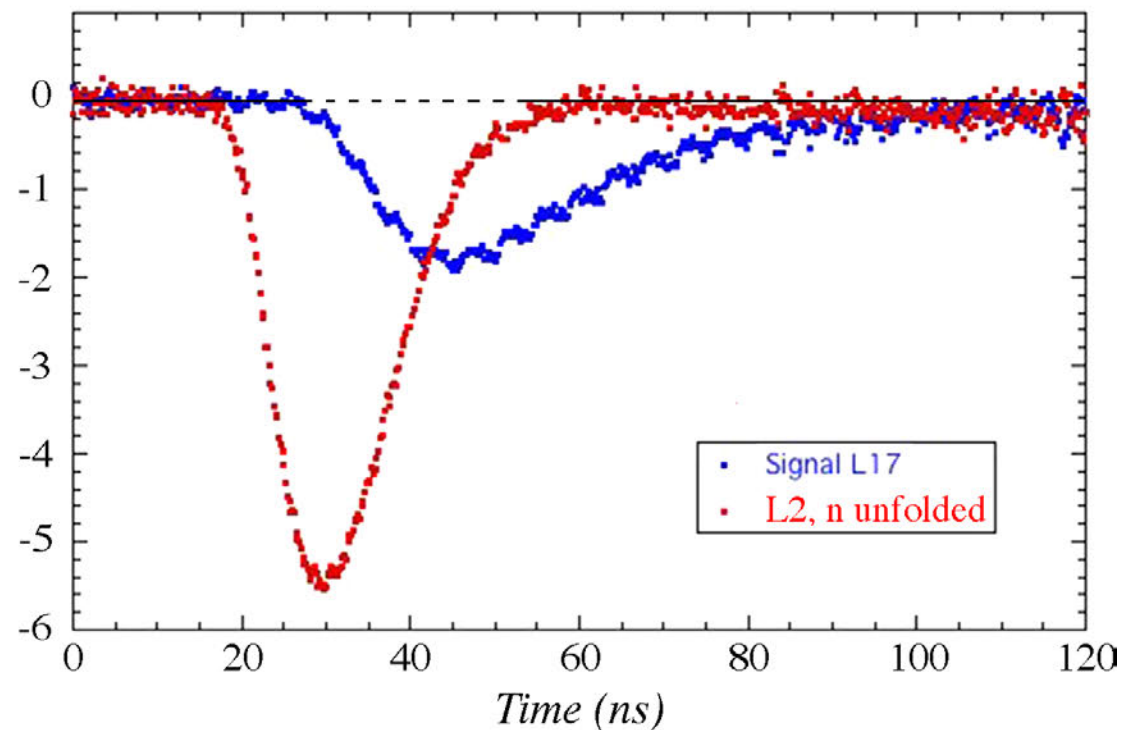


Expected signal contributions:

- prompt charged shower particles

- $n + p \rightarrow n + p$
(time constant 10 - 20 ns)




n contribution unfolded



*The energy resolution of compensating calorimeters is dominated by **sampling fluctuations***

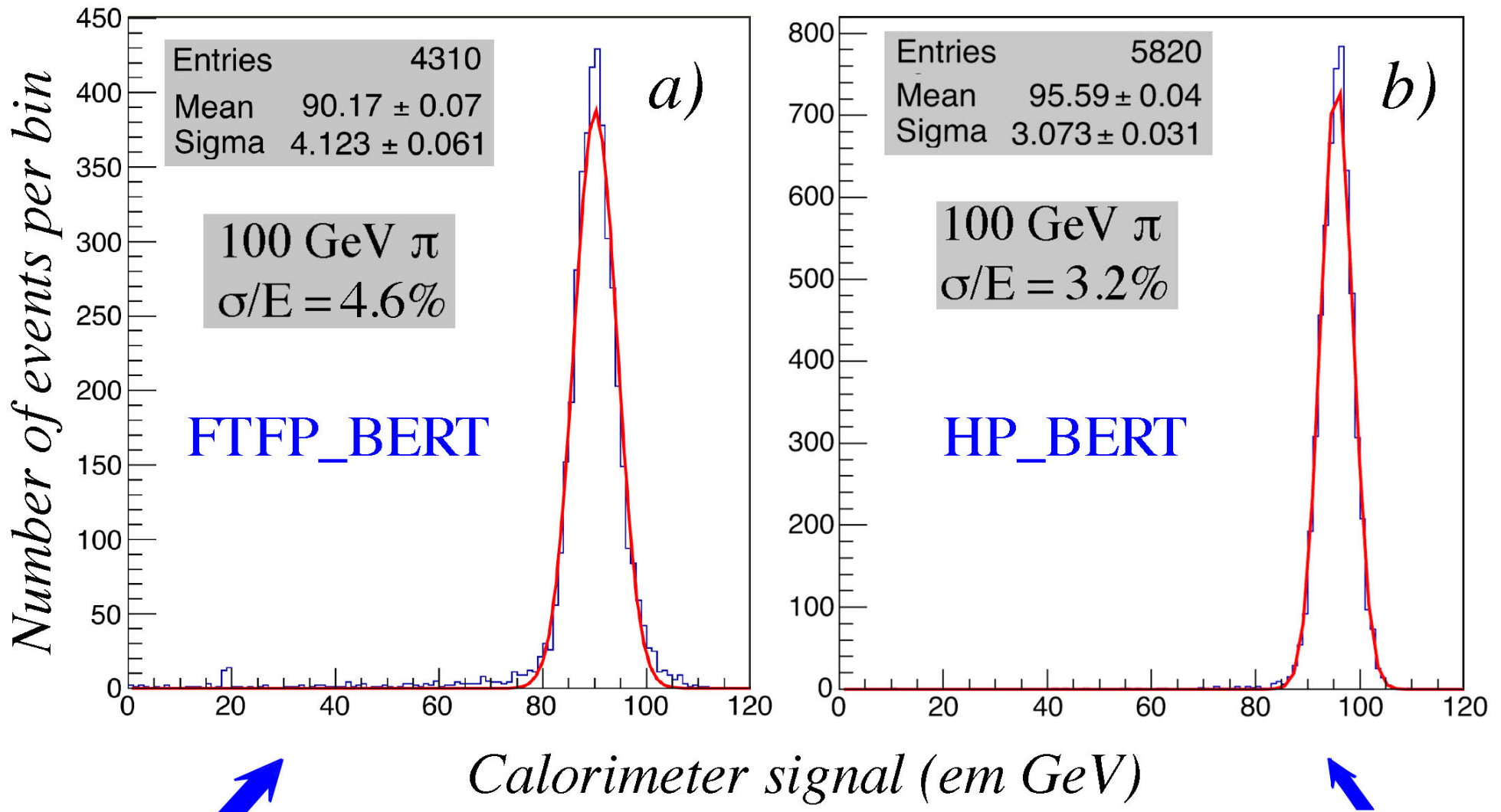
$$\sigma/E = a_{\text{samp}}/\sqrt{E}$$

Published results a_{samp} (%):

<i>Experiment</i>	<i>Structure</i>	<i>em resolution</i>	<i>hadr. resolution</i>
<i>HELIOS</i>	<i>U/plastic plates</i>	<i>19 - 22</i>	<i>34 - 39</i>
<i>ZEUS</i>	<i>U/plastic plates</i>	<i>16.5</i>	<i>31.1</i>
<i>SPACAL</i>	<i>Pb/fibers</i>	<i>12.9</i>	<i>30.6</i>
<i>ZEUS</i>	<i>Pb/plastic plates</i>	<i>23.5</i>	<i>41.2</i>
<i>RD52</i>	<i>Cu/fibers</i>	<i>8.9 (13.9)</i>	<i>?</i>
		<i>sampling</i>  <i>total</i>  (incl Č p.e.)	<i>GEANT: 32</i> 

GEANT4 simulations of 100 GeV π

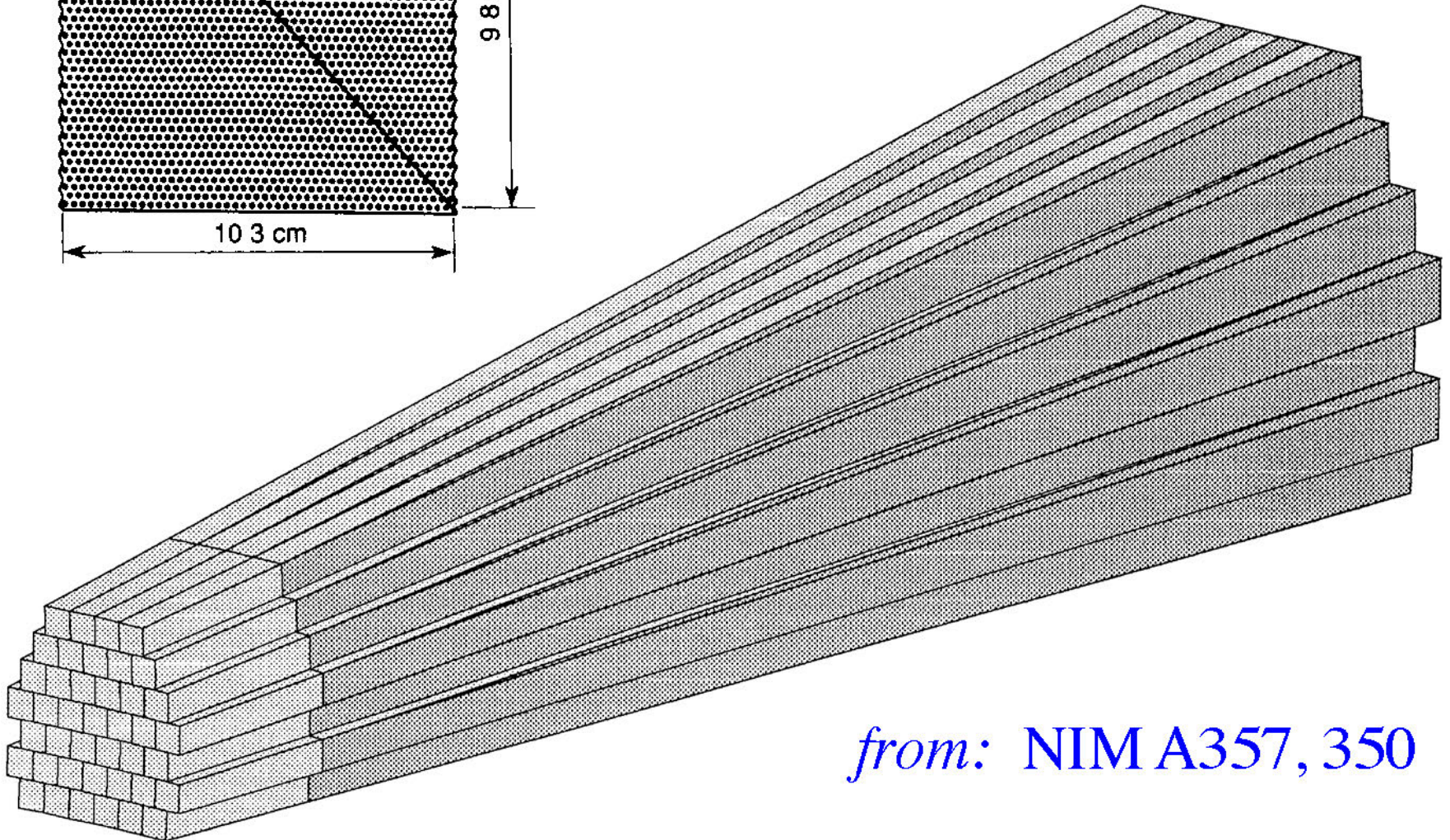
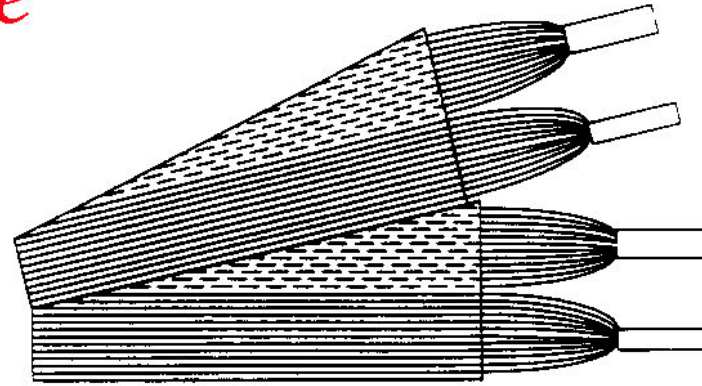
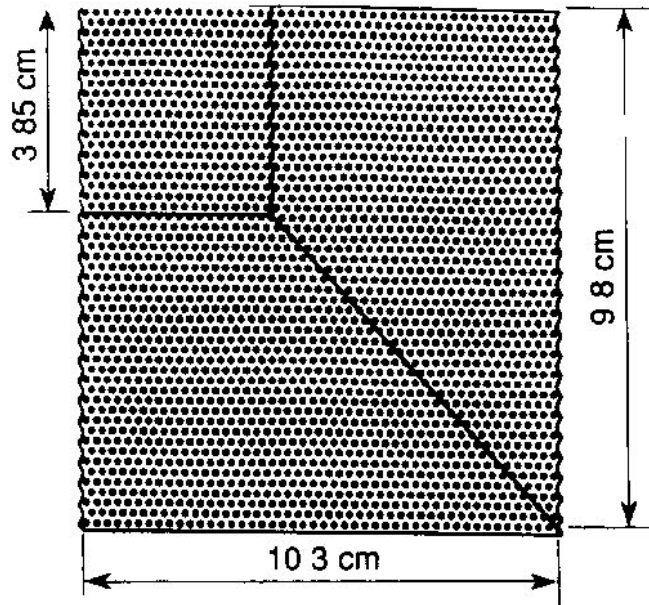
RD52_Cu 65 x 65 cm²



Standard hadronic
shower simulation
package

High precision
simulation package
(neutrons!!)

Projective structure



from: NIM A357, 350