Status and prospects of inclusive b \rightarrow ulv theory

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Why precision CKM studies?

- The SM accomodates flavour & CP violation, but we have no theory of flavour
- We expect New Physics at the EW scale, and most models predict additional flavour and CP violation.
- The CKM mechanism is very successful **flavour** and CP problem (NP must preserve agreement with data)
- To uncover small signals of physics beyond CKM, we need precision tests, in many ways a challenge for our QCD understanding

Outline

- Inclusive decays, inputs, pert corrections
- Shape Function(s)
- High q^2 tail and WA
- Existing approaches
- A trial comparison
- Conclusions

Inclusive semileptonic B decays: basic features

- Simple idea: inclusive decay do not depend on final state, factorize long distance dynamics of the meson. OPE allows to express it in terms of matrix elements of local operators
- The Wilson coefficients are perturbative, matrix elements of local ops parameterize non-pert physics: **double series in** α_s, Λ/m_b
- Lowest order: decay of a free *b*, linear Λ/m_b absent. Depends on $m_{b,c}$, 2 parameters at O(1/m_b²), 2 more at O(1/m_b³)...

$$\mu_{\pi}^{2}(\mu) = \frac{1}{2M_{B}} \left\langle B \left| \overline{b} (i \overline{D})^{2} b \right| B \right\rangle_{\mu} \qquad \mu_{G}^{2}(\mu) = \frac{1}{2M_{B}} \left\langle B \left| \overline{b} \frac{i}{2} \sigma_{\mu\nu} G^{\mu\nu} b \right| B \right\rangle_{\mu}$$

The total s.l. width in the OPE

$$\Gamma[\bar{B} \to X_{u}e\bar{\nu}] = \frac{G_{F}^{2} m_{b}^{5}}{192\pi^{3}} |V_{ub}|^{2} \left[1 + \frac{\alpha_{s}}{\pi} p_{u}^{(1)}(\mu) + \frac{\alpha_{s}^{2}}{\pi^{2}} p_{u}^{(2)}(r,\mu) - \frac{\mu_{\pi}^{2}}{2m_{b}^{2}} - \frac{3\mu_{G}^{2}}{2m_{b}^{2}} \right] \\ + \left(\frac{77}{6} + 8\ln\frac{\mu_{\rm WA}^{2}}{m_{b}^{2}} \right) \frac{\rho_{D}^{3}}{m_{b}^{3}} + \frac{3\rho_{LS}^{3}}{2m_{b}^{3}} + \frac{32\pi^{2}}{m_{b}^{3}} B_{\rm WA}(\mu_{\rm WA}) \right] \\ + O(\alpha_{s}/m_{b}^{2}...)$$

OPE valid for inclusive enough measurements, away from perturbative singularities.

 m_b dependence is up to twice stronger in the cut rate

Most OPE parameters (quark masses etc) from sl decays into charm

Fitting OPE parameters to the moments



Total **rate** gives $|V_{cb}|$, global **shape** parameters (moments of the distributions) tell us about B structure

OPE parameters describe universal properties of the B meson and of the quarks

Global fit (kinetic scheme)



Fits & Quark Masses



Fits & Quark Masses

Fitted |V_{cb}| stable, but 2.4σ from latest lattice exclusive determination.

Mass determinations not so stable

OPE fails for $bs\gamma$, but only at $O(\alpha_s)$ with operators $\neq O_7$. Unlikely to be relevant for normalized moments, but it must be studied

At the moment the role of radiative moments in the fits is similar to using PDG bound on m_b.

Inclusion of additional constraints?



Constant values

Perturbative calculations

Partial rate for $P_+ < \Delta = M_D^2/M_B$



▶ NNLO result is smaller and less dependent on μ_h than NLO

• would lead to higher $|V_{ub}|$ compared to NLO (preliminary)

Some of the shift is due to different *S* at LO, NLO, NNLO

Ben Pecjak, ICHEP08

Complete $O(\alpha_s)$ implemented by all groups De Fazio-Neubert

Running coupling NNLO $O(\alpha_s^2\beta_0)$ in GGOU & DGE lead to -5% & +2%, resp. in $|V_{ub}|$ Gardi,Ridolfi, PG

2008

Asatrian, Greub, Pecjak Bonciani, Ferroglia, Beneke, Huber, Li G. Bell in SCET-HQET corresponds to fixed order $O(\alpha_s^2)$ in the SF region

The problems with cuts

 $|V_{ub}|$ from total BR(b \rightarrow ul ν) like incl $|V_{cb}|$ but we need kinematic cuts to avoid the ~100x larger b \rightarrow cl ν background:

$$m_X < M_D \qquad E_l > (M_B^2 - M_D^2)/2M_B \qquad q^2 > (M_B - M_D)^2 ...$$

or combined (m_X,q²) cuts

The cuts destroy convergence of the OPE that works so well in $b \rightarrow c$. OPE expected to work only away from pert singularities 0.8

Rate becomes sensitive to "local" b-quark wave function properties like Fermi motion Dominant nonpert contributions can be resummed into a SHAPE FUNCTION f(k+)



How to access the SF?



How to access the SF?

Prediction based on resummed pQCD

OPE constraints + parameterization



SF from perturbation theory

Resummed perturbation theory is qualitatively different: Support properties; stability! (E. Gardi)

b quark SF emerges from resummed pQCD but needs an IR prescription and power corrections for $b \rightarrow B$

Dress Gluon Exponentiation (DGE) by Gardi et al employs renormalon resummation to define Fermi motion. Power corrections can be partly accomodated.

Aglietti et al (ADFR) use Analytic Coupling in the IR



The SF in the OPE

Local OPE has also threshold singularities and SF can be equivalently introduced resumming dominant singularities Bigi et al, Neubert

Fermi motion can be parameterized within the OPE like PDFs in DIS. At leading order in m_b only a single universal function of one parameter enters (SF).

Unlike resummed pQCD, the OPE does not predict the SF, only its first few moments. One then needs an ansatz for its functional form.

 $\int dk_+ k_+^n F_i(k_+, q^2) = \text{local OPE prediction} \Leftarrow \text{moments fits}$

Two very different implementations: PG,Giordano,Ossola,Uraltsev (GGOU) Bosch,Lampe,Neubert,Paz (BLNP)

Functional forms



(I-2%) on V_{ub}

Recent more systematic method by Ligeti et al. arXiv:0807.1926 Plot shows 9 SFs that satisfy all the first three moments

0.8

k [GeV]

1

0.2

0.4

0.6

 $= c_4 = 0$

 $c_3 = \pm 0.15, c_4 = 0$

 $c_3 = 0, c_4 = \pm 0.15$

 $c_3 = \pm 0.1, c_4 = \pm 0.1^{-1}$

1.2 1.4

1.6

The high q² tail

At high q² higher dimensional operators are not suppressed leading to pathological features. Origin in the non-analytic square root

WA matrix element B_{WA} parameterizes global properties of the tail, affects V_{ub} determinations depending on cuts, tends to decrease V_{ub}

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Constraining Weak Annihilations



Comparing the existing approaches at common mb (HFAG ichep08, CKM08)

V_{ub} from DGE

Gardi & Andersen see Gardi talk

Main features of the spectra are reproduced $|||||||V_{ub}||$ stable, small errors and good χ^2

NNLL and $O(\alpha_s^2\beta_0)$ implemented

Power corrections in the SF region are included here only in theor. err. No subleading SF. WA error equal for all cuts. Matches to local OPE.

Only input other than α_s m_b(m_b)=4.24(4) from global fit

5-6% total error, mostly mb





Worse consistency here.

NNLO resummation, NLO constants

Consider E_I cuts higher than 2.3GeV because their E_I apparently does not reproduce data (see later)

employs M_B in on-shell calculation of spectra: no renormalon cancellation, no convergence to OPE. no model error

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~7% total error, mostly mc
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Vubfrom ADFR
Aglietti, Di Lodovico, Ferrera, Ricciardi



ub in BLNP Bosch, Lange, Neubert, Paz

$$\tilde{W}_{1}^{(0)}(P_{+}, y) = U_{y}(\mu_{h}, \mu_{i}) H(y, \mu_{h}) \int_{0}^{P_{+}} \int_{0}^{P_{+}} U_{y}(\mu_{h}, \mu_{i}) H(y, \mu_{h}) \int_{0}^{P_{+}} U_{y}(\mu_{h}, \mu_{h}) H(y, \mu_{h}) \int_{0}^{P_{+}} U_{y}(\mu_{h}, \mu_{h}) H(y, \mu_{h}) H(y, \mu_{h}) \int_{0}^{P_{+}} U_{y}(\mu_{h}, \mu_{h}) H(y, \mu_{h}) H(y$$

 $d\Gamma = HJ \otimes \hat{S} + \frac{1}{m_i} H'_i J'_i \otimes \hat{S}'_i + \dots$

Good consistency. Uses elegant multiscale OPE that resums soft-collinear logs, but many largely unconstrained subleading SFs

NNLL resummation, only $O(\alpha_s, \Lambda^2/m_b^2)$ matching to OPE, 3 ffs for leading SF, extensive modelling of SSF.

 m_b and μ_{π^2} in SF scheme obtained from global fit in the kin scheme

~7-8% total error, main error HQE parameters

$$d\hat{\omega} \ m_b J(y, m_b(P_+ - \hat{\omega}), \mu_i) \ \hat{S}(\hat{\omega}, \mu_i)$$

CLEO (E.) $3.94 \pm 0.46 \pm 0.37 - 0.33$ BELLE sim. ann. (m_v, q^2) 4.33 ± 0.46 + 0.35 - 0.30 BELLE (E) $4.74 \pm 0.44 + 0.35 - 0.30$ BABAR (E_a) $4.29 \pm 0.24 \pm 0.35 - 0.30$ BABAR (E_a, s_b^{max}) $4.41 \pm 0.30 \pm 0.42 - 0.37$ BELLE (m_x) $3.99 \pm 0.26 \pm 0.30 - 0.25$ BABAR (m_v) $4.13 \pm 0.20 \pm 0.32 - 0.27$ BABAR $(m_{y}-q^{2})$ $4.41 \pm 0.29 \pm 0.36 - 0.31$ BABAR (P⁺) $3.76 \pm 0.24 + 0.31 - 0.25$ Average +/- exp + theory - heory $4.32 \pm 0.16 \pm 0.32 - 0.27$ $\chi^2/dof = 8.5/8$ (CL = 39 %) Bosch, Lange, Neubert and Paz (BLNP) HFAG Phys.Rev.D72:073006,2005 ICHEP08 2 4 $|V_{nh}| [\times]$

SF in GGOU



$$\int dk_{+} k_{+}^{n} F_{i}(k_{+}, q^{2}) = \text{local OPE} \text{Importance of subleading effects}$$

$|V_{ub}|$ in the kinetic scheme -GGOU

PG,Giordano,Ossola,Uraltsev

Good consistency & small th error. OPE in a scheme with Wilsonian IR cutoff ~IGeV, all subleading I/m_b and O($\alpha_s^2\beta_0$) terms consistently included, careful treatment of high q² tail.

Inputs from global fit to the moments

+6.3-7.0% total error



A global comparison



Why do central values differ up to 9-10%?

The lepton spectrum



Babar E₁ determination

Belle E₁ determination

Common inputs, m_b^{kin} =4.60GeV or $m_b(m_b)$ =4.24GeV. Exp analyses depend strongly on generator (slight inconsistency here...)

The lepton spectrum





The spectrum does provide information: OPE based methods close to each other up to 2.2GeV, resummed methods show larger slope, seem to behave in same way

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The lepton spectrum

DGE slope vs mb



In DGE the slope depends on m_b, while ADFR have it fixed The leptonic spectrum is not sensitive to the SF except quite close to the endpoint. At I.5GeV all methods should agree (it's pQCD after all)

2.4

2.6

The M_X spectrum



- Not all observables are equally clean. eg high q² tail is sensitive to WA
- Need spectra: only way to test frameworks (see E₁ spectrum).
- More inclusive measurements, less dependence on mb
- Theory errors are partly parametric: mb dependence is crucial

	Average V _{ub} x10 ³
DGE	$4.26(14)_{ex}^{+19}_{-13}$
BLNP	$4.31(16)_{ex}^{+32}$ -27
GGOU	$3.96(15)_{ex}^{+20}_{-23}$
2.1, 1.9, 1.3σ from B→πl∨	
(MILC-FNAL) 3.1, 2.4, 1.5 σ from UTFit	
(because of sin2 β)	

NEW preliminary Belle Multivariate analysis only $E_l > I \text{ GeV}$ $|V_{ub}| = (4.45 \pm 0.26^{+0.13}_{-0.22}) \times 10^{-3}_{GGOU}$ 2.1 σ from excl, 2.5 σ from UTFit This includes about 90% of the rate really inclusive measurement, no need for SF. Only crucial input mb needs to be confirmed!

> **NEW PHYSICS?** eg LR models Chen,Nam





Recent lattice results for B_K and previously neglected contributions lead to 15% smaller ε_K , in ~1.8-2 σ conflict with exp sin2 β . **Perhaps sin2\beta is simply too low...**

....or incl Vub and latest BK both wrong

Conclusions

- → MAIN ISSUE for V_{ub} : bottom mass. Can we include additional constraints on m_b in the fit? which ones?
- → Not all observables are equivalent, some are cleaner. For ex high q² tail is sensitive to WA: it decreases V_{ub}. Can we drop it? how much do the exp analyses depend on the high q² tail?
- ➡ Need spectra and/or analysis with varying cuts: only way to test current frameworks (see trial exercise on E_I spectrum). M_X cuts?
- More inclusive measurements are welcome: they decrease the dependence of |V_{ub}| on both SF and m_b
- ➡ Frameworks fairly compatible within non-par th errors. Convergence to OPE (normalization) to be checked. Use mb uncertainty as exp error?
- The primary goal is the precise determination of |V_{ub}|. All frameworks are interesting, but they are **not all equivalent**. After |V_{ub}| is measured we can go back and study models of QCD dynamics.