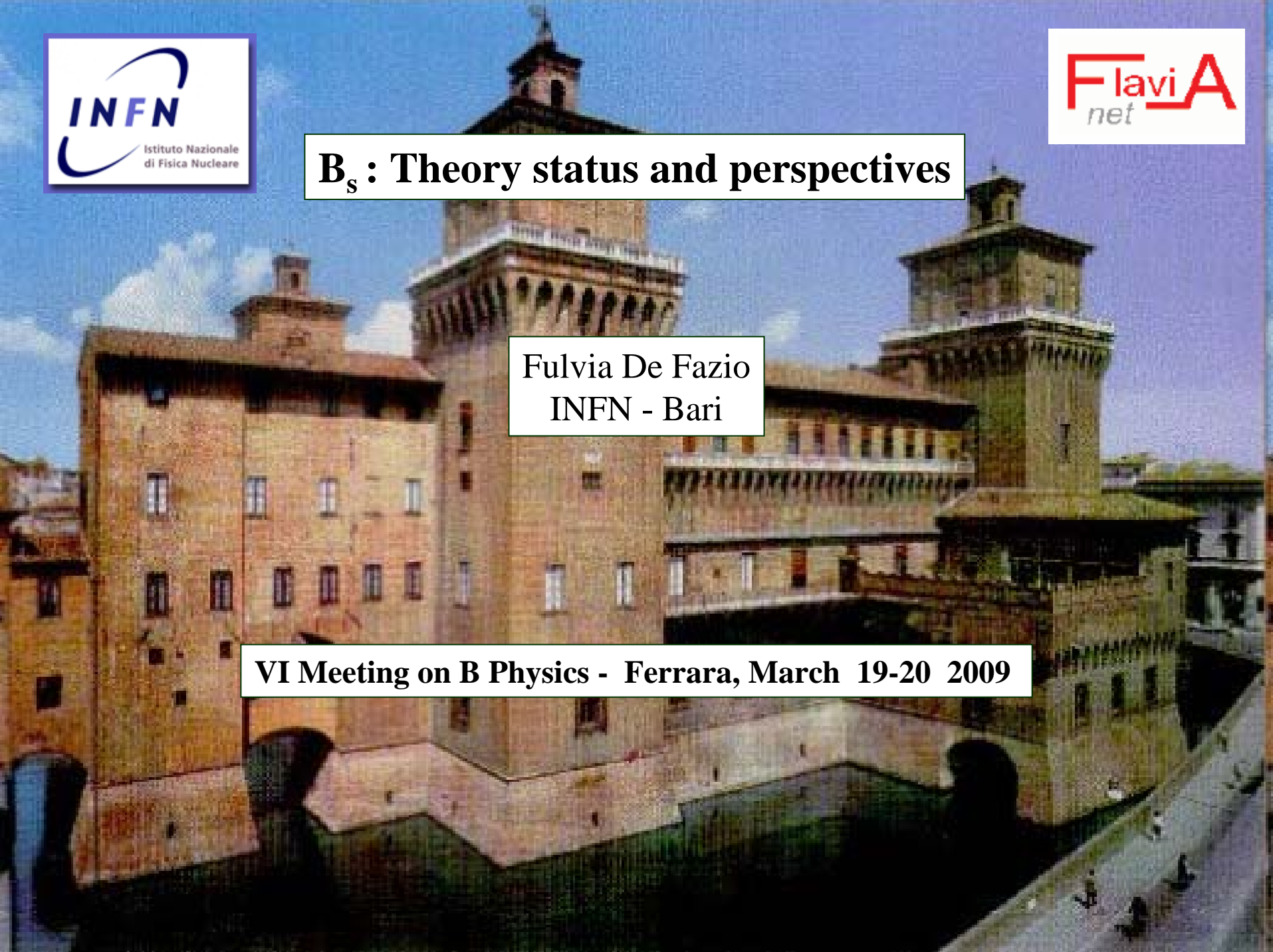





**$B_s$  : Theory status and perspectives**

Fulvia De Fazio  
INFN - Bari

**VI Meeting on B Physics - Ferrara, March 19-20 2009**



# Outline

- Notations & known facts about mixing of neutral B mesons
- Determination of  $\Delta m$ ,  $\Delta \Gamma$ ,  $\phi$  – theory predictions
  - (some) proposed strategies
  - experimentally adopted strategies
- $B_s \rightarrow J/\psi \phi$  : discussion of some theoretical uncertainties – role of 
  - SU(3) for strong phases
- Other channels:
  - $f_0(980)$  as a S-wave background to  $\phi$
  - $B_s \rightarrow J/\psi f_0(980)$  as an alternative mode
  - other interesting modes
- New Physics:
  - $\Delta m_s$
  - $\phi$
- $B_s$  Physics not related to CP violation: some interesting decay modes
- Conclusions

# $B_s - \bar{B}_s$ mixing

governed by Schroedinger-like eq.

$$i \frac{d}{dt} \begin{pmatrix} |B_s(t)\rangle \\ |\bar{B}_s(t)\rangle \end{pmatrix} = \left( \hat{M} - i \frac{\hat{\Gamma}}{2} \right) \begin{pmatrix} |B_s(t)\rangle \\ |\bar{B}_s(t)\rangle \end{pmatrix}$$

$$\begin{aligned} \hat{M}, \hat{\Gamma} \quad 2 \times 2 \quad \text{hermitian matrices} &\Rightarrow M_{21} = M_{12}^* \quad \Gamma_{21} = \Gamma_{12}^* \\ \text{CPT} &\Rightarrow M_{11} = M_{22} \quad \Gamma_{11} = \Gamma_{22} \end{aligned}$$

mass eigenstates

$$\begin{aligned} |B_{s,L}\rangle &= p |B_s\rangle + q |\bar{B}_s\rangle \\ |B_{s,H}\rangle &= p |B_s\rangle - q |\bar{B}_s\rangle \end{aligned}$$

with

$$\begin{aligned} M_L, \Gamma_L \\ M_H, \Gamma_H \end{aligned}$$

Usual notations:

$$\begin{aligned} \Delta m &= M_H - M_L & \Delta \Gamma &= \Gamma_L - \Gamma_H \\ \phi &= \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) & \phi_M &= \arg(M_{12}) \end{aligned}$$

## $B_s - \bar{B}_s$ mixing

Exact results:

$$(\Delta m)^2 - \frac{1}{4}(\Delta\Gamma)^2 = 4|M_{12}|^2 - |\Gamma_{12}|^2$$

$$(\Delta m)(\Delta\Gamma) = 4 \operatorname{Re}(M_{12}\Gamma_{12}^*)$$

$$\frac{q}{p} = -\frac{\Delta m - i\frac{\Delta\Gamma}{2}}{2\left(M_{12} - i\frac{\Gamma_{12}}{2}\right)}$$

but using:  $|\Gamma_{12}| \ll |M_{12}|$

$$\Delta m = 2|M_{12}|$$

$$\Delta\Gamma = 2|\Gamma_{12}|\cos\phi$$

If CP were conserved...

$$CP|B_{s,L}\rangle = -|B_{s,L}\rangle$$

$$CP|B_{s,H}\rangle = |B_{s,H}\rangle$$

$$M_{12} = M_{21} = M_{12}^* \Rightarrow \phi_M = 0$$

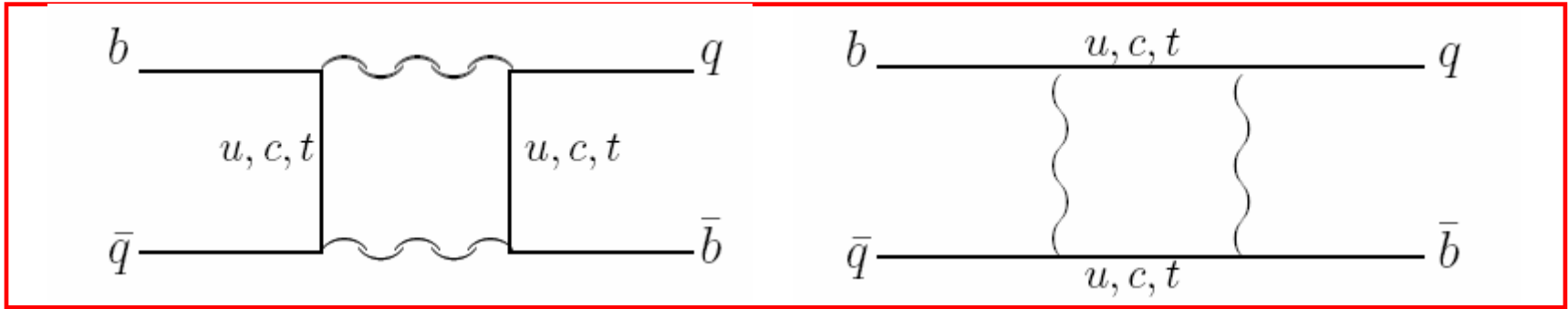
$$\Gamma_{12} = \Gamma_{21} = \Gamma_{12}^* \Rightarrow \phi = 0$$

(in the phase convention  $CP|B_s\rangle = -|\bar{B}_s\rangle$  )

# $B_s - \bar{B}_s$ mixing

$|M_{12}|$ ,  $|\Gamma_{12}|$ ,  $\phi = \arg(-M_{12}/\Gamma_{12})$  are related to observables

$\Delta m$  and  $\Delta\Gamma$  come from real and Im parts of box diagrams:



●  $\Delta m = 2|M_{12}| \rightarrow |M_{12}|$  takes contribution from **heavy** internal particles:  $t$ , NP

●  $\Delta\Gamma = 2|\Gamma_{12}|\cos\phi \rightarrow |\Gamma_{12}|$  sensible to **light** internal particles  $u, c$

Any NP would also affect tree level decays  $\Rightarrow$  assume no NP in  $\Gamma_{12}$

NP would change instead  $|M_{12}|$

$B_q - \bar{B}_q$  mixing

$$\phi_M = \arg(M_{12})$$

Takes contribution from internal top exchange

$$\phi_{M,q} = 2 \arg(V_{tb} V_{tq}^*)$$

$$\phi = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) = \phi_M - \arg(-\Gamma_{12})$$

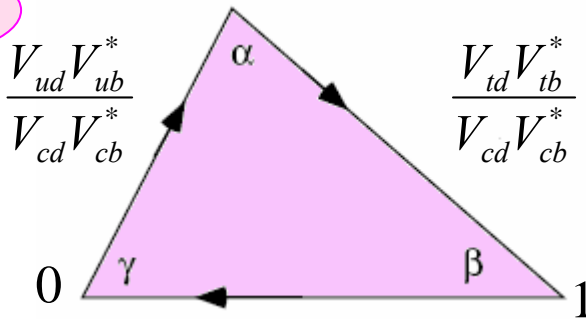
$\Gamma_{12}$  takes contribution from internal u,c exchange

$$\arg(\Gamma_{12}) \approx 2 \arg(V_{cb} V_{cq}^*), 2 \arg(V_{cb} V_{cq}^*) \arg(V_{ub} V_{uq}^*), 2 \arg(V_{ub} V_{uq}^*)$$

Only neglecting these contributions leads to

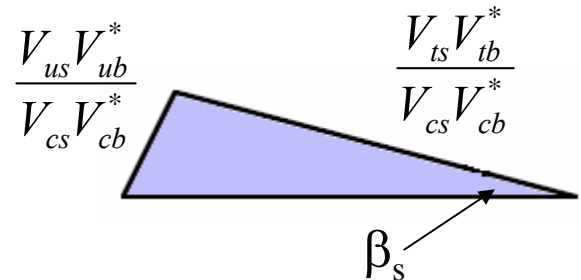
$$2\beta_q = 2 \arg\left(-\frac{V_{tb} V_{tq}^*}{V_{cb} V_{cq}^*}\right)$$

$B_d - \bar{B}_d$



$$\beta_d = \arg\left(-\frac{V_{tb} V_{td}^*}{V_{cb} V_{cd}^*}\right) = 0.38 \pm 0.02 \text{ rad}$$

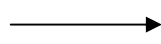
$B_s - \bar{B}_s$



$$\beta_s = \arg\left(-\frac{V_{tb} V_{ts}^*}{V_{cb} V_{cs}^*}\right) \approx 0.02 \text{ rad}$$

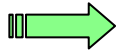
$B_s - \bar{B}_s$  mixing

$$\phi = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right)$$



In the SM it turns out to be tiny

$$\Delta\Gamma = 2|\Gamma_{12}|\cos\phi$$



Since NP should not affect  $\Gamma_{12}$   
it can only modify  $\cos\phi$



NP can only decrease the value of  $\Delta\Gamma$  with respect to SM

# Theory predictions: $\Delta m$

Calculation of the box diagram with internal top quarks gives rise to an effective hamiltonian composed by a single operator

$$Q = \bar{s}_L \gamma_\nu b_L \bar{s}_L \gamma^\nu b_L$$

with:

$$\langle \bar{B}_s | Q | B_s \rangle = \frac{2}{3} f_{B_s}^2 M_{B_s} \frac{B_{B_s}}{b(\mu)}$$

renorm. group invariant

$$b(\mu) = [\alpha_s(\mu)]^{-6/23}$$

at LO

The Wilson coefficient of  $Q$  is

$$C(m_t, M_W, \mu =) = M_W^2 S(x_t) \hat{\eta}_b b(\mu)$$

Perturbative quantities:

$$S_0(x_t) \quad x_t = \frac{m_t^2}{M_W^2}$$

Inami , Lim

$$\hat{\eta}_B$$

Buras et al.

**Result:**

$$\Delta m_s = 2M_{12} = \frac{G_F^2}{6\pi^2} |V_{tb} V_{ts}^*|^2 M_W^2 S_0(x_t) \hat{\eta}_B B_{B_s} f_{B_s}^2 M_{B_s}$$



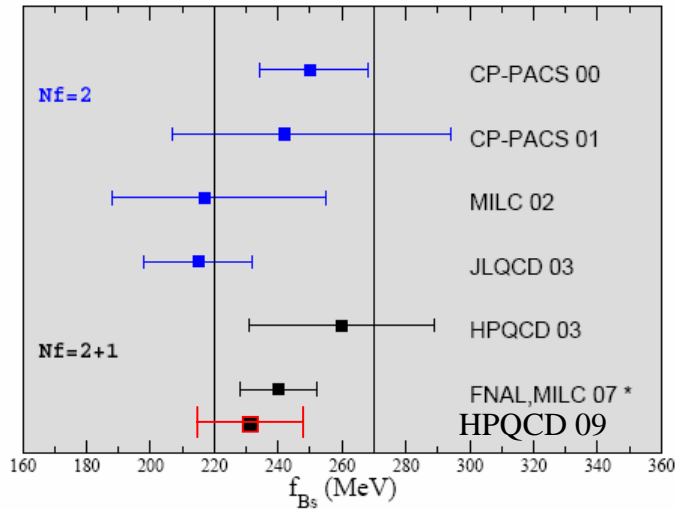
$$\frac{\Delta m_s}{\Delta m_d} = \frac{M_{B_s}}{M_{B_d}} \left| \frac{V_{ts}^2}{V_{td}^2} \right| \xi^2 \quad \xi = \frac{f_{B_s} \sqrt{B_{B_s}}}{f_{B_d} \sqrt{B_{B_d}}}$$



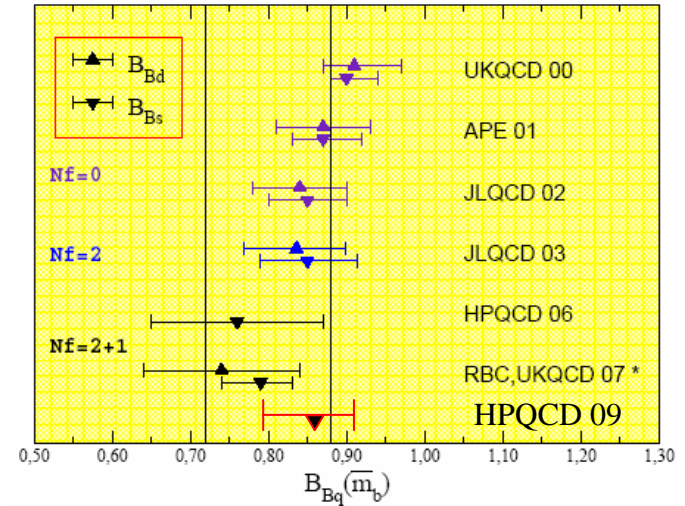
# Theory predictions: $\Delta m$

Plots from Lubicz and Tarantino, 0807.4605

$f_{B_s}$



$B_{B_s}$



Very recent HPQCD results, with  $n_f=2+1$

$$f_{B_s} = 231 \pm 15 \text{ MeV}$$

$$B_{B_s} = 0.86 \pm 0.06$$

Sum rules give results in the same ballpark

$\xi$

$$\xi = 1.258 \pm 0.033$$

HPQCD 09 - 0902.1815

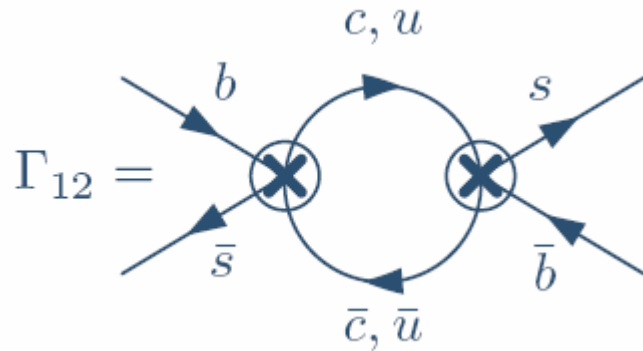
**Final result:**

$$\Delta m^{SM} = (19.30 \pm 6.68) \text{ ps}^{-1}$$

Lenz & Nierste,  
JHEP 06 (07) 072

# Theory predictions: $\Delta\Gamma$

Exploiting that  $m_t, M_W \gg m_b$  heavy particles can be integrated out  
 The effective hamiltonian stems from:



The imaginary part is obtained using the optical theorem



$\Gamma_{12}$  is written as an expansion in  $\Lambda/m_b$  and  $\alpha_s$

At leading order two operators contribute:

$$Q = \bar{q}_\alpha \gamma_\mu (1 - \gamma_5) b_\alpha \bar{q}_\beta \gamma_\mu (1 - \gamma_5) b_\beta$$

$$Q_S = \bar{q}_\alpha (1 + \gamma_5) b_\alpha \bar{q}_\beta (1 + \gamma_5) b_\beta$$

However:

- almost complete cancellation of the coefficient of  $Q$
- too large  $1/m_b$  and  $\alpha_s$  corrections

**Enters also in  $\Delta m$**



A different basis can be used, with a better behaved expansion

# Theory predictions: $\Delta\Gamma$

Define:  $\tilde{Q}_S = \bar{q}_\alpha (1 + \gamma_5) b_\beta \bar{q}_\beta (1 + \gamma_5) b_\alpha$

$$\langle B_s | \tilde{Q}_S | \bar{B}_s \rangle = \frac{1}{3} M_{B_s}^2 f_{B_s}^2 \tilde{B}'_s$$

Using the fact that

$$R_0 = Q_s + \alpha_1 \tilde{Q}_S + \frac{\alpha_2}{2} Q = O\left(\frac{1}{m_b}\right)$$

one can trade the old basis  $\{Q, Q_s\}$  for the new basis  $\{Q, \tilde{Q}_S\}$

Result:

$$\Delta\Gamma_s^{SM} = \left(\frac{f_{B_s}}{240\text{MeV}}\right)^2 \left[ (0.105 \pm 0.016) B + (0.024 \pm 0.004) \tilde{B}'_s + O\left(\frac{1}{m_b}\right) \right] \text{ps}^{-1}$$

$$\left(\frac{\Delta\Gamma_s}{\Delta m_s}\right)^{SM} = [49.7 \pm 9.4] \times 10^{-4}$$

Using  $B = 0.85 \pm 0.06$   
 $\tilde{B}'_s = 1.41 \pm 0.12 \rightarrow$  (lattice)

Precisely predicts

$$\frac{\Delta\Gamma_s}{\Delta m_s}$$

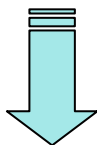
$$\left(\frac{\Delta\Gamma_s}{\Delta m_s}\right)^{SM} = [49.7 \pm 9.4] \times 10^{-4}$$

Using the CDF result:

$$\Delta m_s = 17.77 \pm 0.10 \pm 0.07 \text{ ps}^{-1}$$



$$\begin{aligned}\Delta\Gamma_s^{SM} &= 0.088 \pm 0.017 \text{ ps}^{-1} \\ \frac{\Delta\Gamma_s^{SM}}{\Gamma_s} &= 0.127 \pm 0.024\end{aligned}$$



Experimental violation of these results would signal NP in  $\Delta m_s$  or  $\Delta\Gamma_s$

# Time evolution

was pure  $B^0$  at  $t=0$

$$\begin{aligned}
 |B^0(t)\rangle &= \frac{e^{-imt}}{2} \left\{ |B^0\rangle \left[ e^{-\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_H t}{2}} + e^{\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_L t}{2}} \right] + \frac{q}{p} |\bar{B}^0\rangle \left[ e^{\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_L t}{2}} - e^{-\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_H t}{2}} \right] \right\} \\
 |\bar{B}^0(t)\rangle &= \frac{e^{-imt}}{2} \left\{ \frac{p}{q} |B^0\rangle \left[ -e^{-\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_H t}{2}} + e^{\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_L t}{2}} \right] + |\bar{B}^0\rangle \left[ e^{-\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_H t}{2}} + e^{\frac{i\Delta mt}{2}} e^{-\frac{\Gamma_L t}{2}} \right] \right\}
 \end{aligned}$$

was pure  $\bar{B}^0$  at  $t=0$

Definitions:

$$\begin{aligned}
 A_f &= \langle f | B^0 \rangle & \bar{A}_f &= \langle f | \bar{B}^0 \rangle & |\bar{f}\rangle &= CP|f\rangle \\
 A_{\bar{f}} &= \langle \bar{f} | B^0 \rangle & \bar{A}_{\bar{f}} &= \langle \bar{f} | \bar{B}^0 \rangle
 \end{aligned}$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

$$A_{CP}^{dir} = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \quad A_{CP}^{mix} = -2 \frac{\text{Im}(\lambda_f)}{1 + |\lambda_f|^2} \quad A_{\Delta\Gamma} = -2 \frac{\text{Re}(\lambda_f)}{1 + |\lambda_f|^2}$$

## Time dependent decay rates

$$\Gamma(B^0(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 e^{-\Gamma t} \left\{ \frac{1 + |\lambda_f|^2}{2} \cosh \frac{\Delta\Gamma t}{2} + \frac{1 - |\lambda_f|^2}{2} \cos(\Delta m t) \right. \\ \left. - \operatorname{Re} \lambda_f \sinh \frac{\Delta\Gamma t}{2} - \operatorname{Im} \lambda_f \sin(\Delta m t) \right\}$$

$$\Gamma(\bar{B}^0(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 (1 + a) e^{-\Gamma t} \left\{ \frac{1 + |\lambda_f|^2}{2} \cosh \frac{\Delta\Gamma t}{2} - \frac{1 - |\lambda_f|^2}{2} \cos(\Delta m t) \right. \\ \left. - \operatorname{Re} \lambda_f \sinh \frac{\Delta\Gamma t}{2} + \operatorname{Im} \lambda_f \sin(\Delta m t) \right\}$$

$$\Gamma(B^0(t) \rightarrow \bar{f}) = \mathcal{N}_f |\bar{A}_f|^2 e^{-\Gamma t} (1 - a) \left\{ \frac{1 + |\lambda_{\bar{f}}|^{-2}}{2} \cosh \frac{\Delta\Gamma t}{2} - \frac{1 - |\lambda_{\bar{f}}|^{-2}}{2} \cos(\Delta m t) \right. \\ \left. - \operatorname{Re} \frac{1}{\lambda_{\bar{f}}} \sinh \frac{\Delta\Gamma t}{2} + \operatorname{Im} \frac{1}{\lambda_{\bar{f}}} \sin(\Delta m t) \right\}$$

$$\Gamma(\bar{B}^0(t) \rightarrow \bar{f}) = \mathcal{N}_f |\bar{A}_f|^2 e^{-\Gamma t} \left\{ \frac{1 + |\lambda_{\bar{f}}|^{-2}}{2} \cosh \frac{\Delta\Gamma t}{2} + \frac{1 - |\lambda_{\bar{f}}|^{-2}}{2} \cos(\Delta m t) \right. \\ \left. - \operatorname{Re} \frac{1}{\lambda_{\bar{f}}} \sinh \frac{\Delta\Gamma t}{2} - \operatorname{Im} \frac{1}{\lambda_{\bar{f}}} \sin(\Delta m t) \right\}$$

Determination of  $\Delta m$ ,  $\Delta\Gamma$ ,  $\phi$ :

Strategies, experimental methods, theoretical uncertainties

Measured quantity: mixing amplitude

$$A_{mix}(t) = \frac{N_{mixed}(t) - N_{unmixed}(t)}{N_{mixed}(t) + N_{unmixed}(t)} = -D \cos(\Delta m t)$$

Dilution factor  $D=2P_{tag}-1$

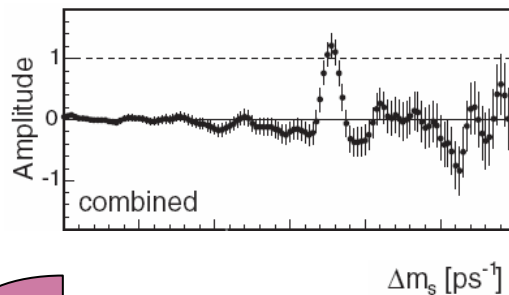
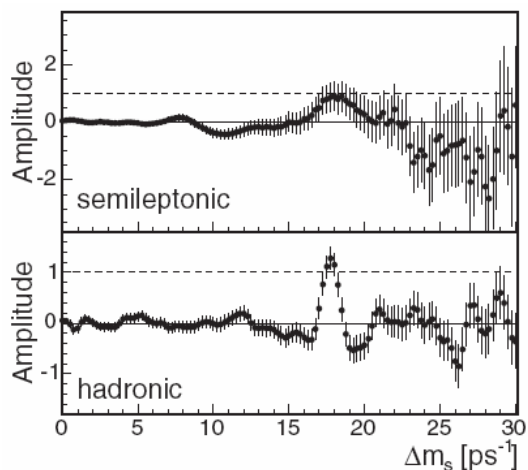
Number of particles decaying after mixing happened

$$N_{mixed}(t) \propto \frac{1}{2}(1 - \cos(\Delta m t))$$

Number of particles decaying – no mixing happened

$$N_{unmixed}(t) \propto \frac{1}{2}(1 + \cos(\Delta m t))$$

- tagging of flavour at production
- final state flavour determined reconstructing flavour specific final states



$$\Delta m_s = 17.7 \pm 0.10(stat) \pm 0.07(syst) \text{ ps}^{-1}$$

← CDF

**D0** →

$$\Delta m_s = 18.53 \pm 0.98(stat + syst) \text{ ps}^{-1}$$



# Asymmetries

- Asymmetries in flavour specific final states ( $f$ s)
- Asymmetries in final CP eigenstates
- CP asymmetries in flavour specific final states

Flavour specific final state  $f$ :

$$\begin{array}{l} B^0 \rightarrow f \quad \text{but} \quad \bar{B}^0 \not\rightarrow f \quad \Rightarrow \quad \bar{A}_f = 0 \quad \Rightarrow \quad \lambda_f = 0 \\ \bar{B}^0 \rightarrow \bar{f} \quad \text{but} \quad B^0 \not\rightarrow \bar{f} \quad \Rightarrow \quad A_{\bar{f}} = 0 \quad \Rightarrow \quad \frac{1}{\lambda_{\bar{f}}} = 0 \end{array}$$

CP eigenstate final state  $f_{CP}$ :

$$f = f_{CP} = \eta_f \bar{f} \quad \eta_f = \pm 1$$

# Asymmetries in CP eigenstate final state

$$\begin{aligned}
 a_f(t) &= \frac{\Gamma(\bar{B}^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow f)}{\Gamma(\bar{B}^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow f)} = \\
 &= -\frac{A_{CP}^{dir} \cos(\Delta mt) + A_{CP}^{mix} \sin(\Delta mt)}{\cosh\left(\frac{\Delta\Gamma t}{2}\right) + A_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma t}{2}\right)}
 \end{aligned}$$

(putting  $a = \frac{\Delta\Gamma}{\Delta m} \tan\phi = 0$ )

If there is only one amplitude contributing to the decay:

$$\left| \frac{\bar{A}_f}{A_f} \right| = 1 \Rightarrow |\lambda_f| = 1 \Rightarrow A_{CP}^{dir} = 0 \quad A_{CP}^{mix} = \eta_f \sin\phi \quad A_{\Delta\Gamma} = -\eta_f \cos\phi$$

CP parity of the final state



$$a_f(t) = -\frac{\eta_f \sin\phi \sin(\Delta mt)}{\cosh\left(\frac{\Delta\Gamma t}{2}\right) - \eta_f \cos\phi \sinh\left(\frac{\Delta\Gamma t}{2}\right)}$$

## CP Asymmetries in $fs$ final state

Assuming no direct CP violation:  $A_f = \bar{A}_{\bar{f}}$

$$a_{fs}^{CP} = \frac{\Gamma(\bar{B}^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow \bar{f})}{\Gamma(\bar{B}^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow \bar{f})} = \frac{|\Gamma_{12}|}{|M_{12}|} \sin \phi$$
$$= a = \frac{\Delta\Gamma}{\Delta m} \operatorname{tg} \phi$$

Related to an untagged quantity:

$$A_{fs}^{untagged} = \frac{\int_0^{\infty} dt [\Gamma(f, t) - \Gamma(\bar{f}, t)]}{\int_0^{\infty} dt [\Gamma(f, t) + \Gamma(\bar{f}, t)]} =$$
$$= \frac{a_{fs}}{2} \frac{x_s^2 + y_s^2}{1 + x_s^2}$$

$$x_s = \frac{\Delta m}{\Gamma} \quad y_s = \frac{\Delta\Gamma}{2\Gamma}$$

Untagged analysis of semileptonic decays

$$B_s^0 \rightarrow D_s^- \mu^+ \nu X$$

$$\bar{B}_s^0 \rightarrow D_s^+ \mu^- \nu X$$

Results obtained using:

$$A_{fs}^{untagged} = \frac{a_{fs} x_s^2 + y_s^2}{2(1+x_s^2)}$$

$$A_{fs}^{untagged} = [1.23 \pm 0.97 (stat) \pm 0.35 (syst)] \times 10^{-2}$$

$$a_{fs} = \frac{\Delta\Gamma_s}{\Delta m_s} \text{tg}\phi = [2.45 \pm 1.93 (stat) \pm 0.35 (syst)] \times 10^{-2}$$



Can be used to determine  $\Delta\Gamma_s$  and  $\phi$

Another possibility is to use the relation to the analogous asymmetry in  $B_d$  decays and B factories results

Combined result

$$a_{fs} = 0.001 \pm 0.0090$$

$$\Delta\Gamma_s = 0.13 \pm 0.09 \text{ ps}^{-1}$$

$$\phi = -0.70 \pm_{0.39}^{0.47}$$

—————> large uncertainties

$$B_s \rightarrow J/\psi \phi$$

The final state is an admixture of different CP eigenstates

—→ can be disentangled considering the angular distribution of the decay products:

$$J/\psi \rightarrow l^+ l^- \quad \phi \rightarrow K^+ K^-$$

Three independent polarization amplitudes:

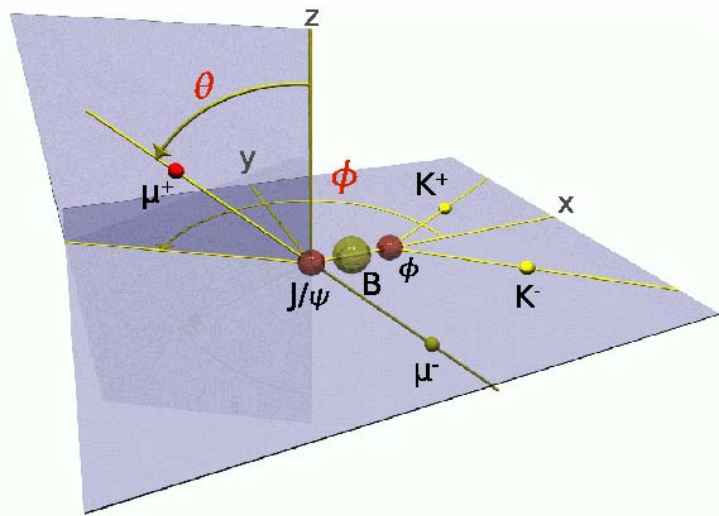
$$A_0(t), \quad A_{\parallel}(t), \quad A_{\perp}(t)$$

with

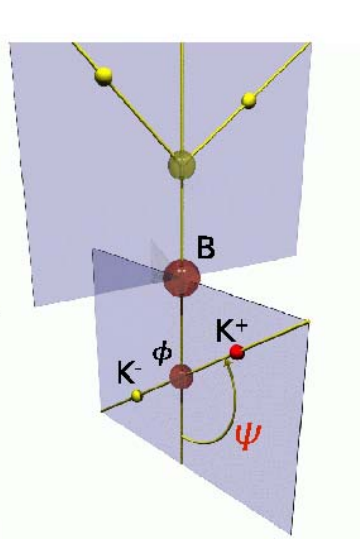
$$|A|^2 = |A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2$$

CP even

CP odd



J/ψ rest frame



φ rest frame

$\theta, \phi, \psi$ , transversity angles

$$B_s \rightarrow J / \psi \phi$$

Simple example: time-dependent one-angle distribution:

$$\frac{d\Gamma(t)}{d \cos \theta} \propto \underbrace{\left( |A_0(t)|^2 + |A_{\parallel}(t)|^2 \right)}_{\text{CP even}} \frac{3}{8} (1 + \cos^2 \theta) + \underbrace{|A_{\perp}(t)|^2}_{\text{CP odd}} \frac{3}{4} \sin^2 \theta$$

The full three angle distribution contains more information.

However:

- it is more involved

- depends also on the strong phases  $\delta_1 = \arg\{A_{\parallel}(0)^* A_{\perp}(0)\}$   $\delta_2 = \arg\{A_0(0)^* A_{\perp}(0)\}$



Method exploited by D0 and CDF

$$B_s \rightarrow J / \psi \phi$$

D0 analysis of the angular distribution in **flavour untagged**  $B_s^0$  mesons

Fitting:

$$\frac{d^3\Gamma}{d \cos \theta d\phi d\psi}$$

The result has a **four-fold ambiguity**  $\pm \phi, \pm(\pi-\phi)$  due to the invariance under simultaneous exchange of the sign of  $\sin \phi, \cos \delta_1, \cos \delta_2$

Two sets of solutions:

$$|\phi| = 0.79 \pm 0.56 (stat) \pm_{0.14}^{0.01} (syst)$$

$$\Delta\Gamma_s = 0.17 \pm 0.08 (stat) \pm 0.02 (syst)$$

$$|\phi| = 2.35 \pm 0.56 (stat) \pm_{0.14}^{0.01} (syst)$$

$$\Delta\Gamma_s = -0.17 \pm 0.08 (stat) \pm 0.02 (syst)$$



set consistent with SM

$$B_s \rightarrow J / \psi \phi$$

CDF Collab., PRL 100 (08) 161802

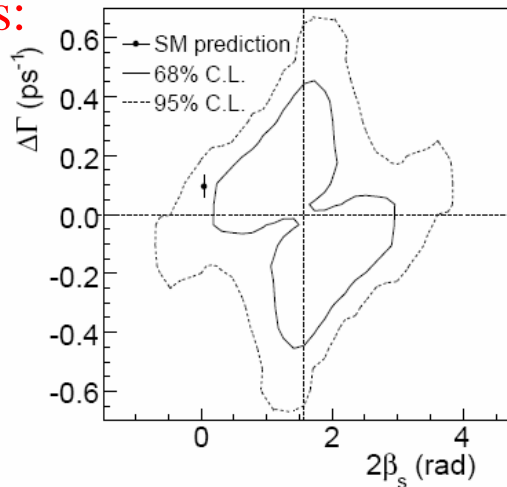
D0 Collab., PRL 101 (08) 241801

## CDF and D0 analysis of **flavour tagged** decay



- combines information obtained from both the time dependence  
both the angular distributions to disentangle the various CP components
- allows to reduce the four-fold ambiguity in a twofold ambiguity

### CDF Results:



at 68% C.L.

$$2\beta_s \in [0.32, 2.82]$$

while imposing the SM prediction for  $\Gamma_{12}$ :

$$2\beta_s \in [0.24, 1.36] \cup [1.78, 2.90]$$

Assuming SM predictions for  $2\beta_s$  and  $\Delta\Gamma$ , CDF finds that the probability of a deviation as large as the level of the observed data is 15%



$$B_s \rightarrow J/\psi\phi$$

Allowed ranges at 90% C.L.

$$-1.22 < \phi < -0.08$$

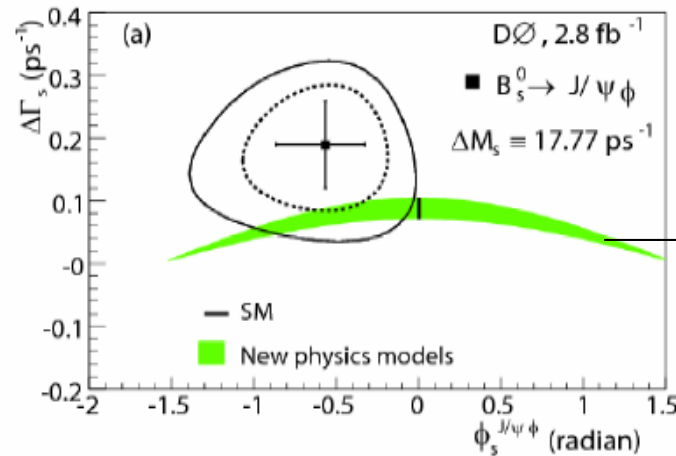
$$-3.06 < \phi < -1.92$$

$$0.05 < \Delta\Gamma < 0.33 \text{ ps}^{-1}$$

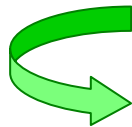
$$-0.33 < \Delta\Gamma < -0.05 \text{ ps}^{-1}$$

the SM hypothesis for  $\phi$  has a probability of 8.5 %

D0 performs also a fit with constrained  $\delta_i$ , taken from  $B_d \rightarrow J/\psi K^*$



$$\Delta\Gamma_s = \Delta\Gamma_s^{SM} |\cos\phi_s|$$



$$\Delta\Gamma_s = 0.19 \pm 0.07 (stat) \pm_{0.01}^{0.02} (syst) \text{ ps}^{-1}$$

$$\phi = -0.57 \pm_{0.30}^{0.24} (stat) \pm_{0.02}^{0.08} (syst)$$

$$B_s \rightarrow J / \psi \phi$$

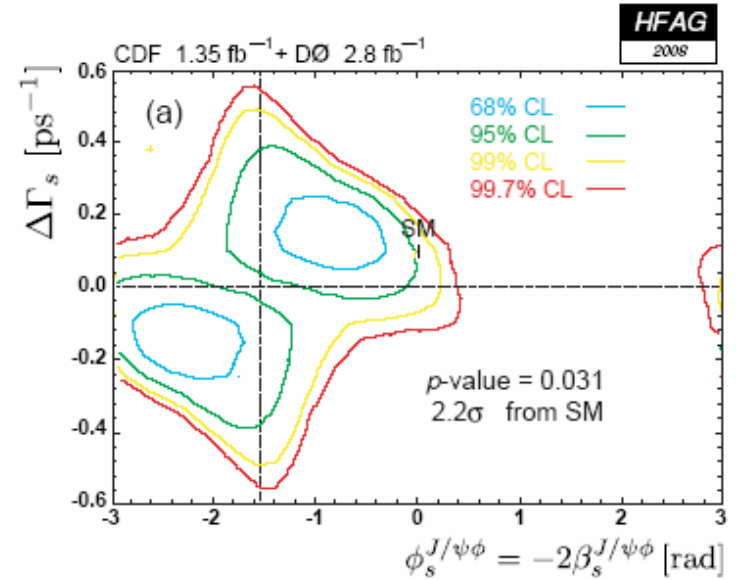
**Combined result (HFAG)**  
(no assumption on the strong phases)

HFAG, 0808.1297

Numerical results for the two solutions:

$$\begin{aligned} \Delta\Gamma_s &= 0.154^{+0.054}_{-0.070} \text{ ps}^{-1}, \\ &\in [+0.036, +0.264] \text{ at 90\% CL} \\ \phi_s^{J/\psi\phi} = -2\beta_s^{J/\psi\phi} &= -0.77^{+0.29}_{-0.37} \text{ rad}, \\ &\in [-1.47, -0.29] \text{ at 90\% CL}, \end{aligned}$$

$$\begin{aligned} \Delta\Gamma_s &= -0.154^{+0.070}_{-0.054} \text{ ps}^{-1}, \\ &\in [-0.264, -0.036] \text{ at 90\% CL} \\ \phi_s^{J/\psi\phi} = -2\beta_s^{J/\psi\phi} &= -2.36^{+0.37}_{-0.29} \text{ rad}, \\ &\in [-2.85, -1.65] \text{ at 90\% CL}. \end{aligned}$$

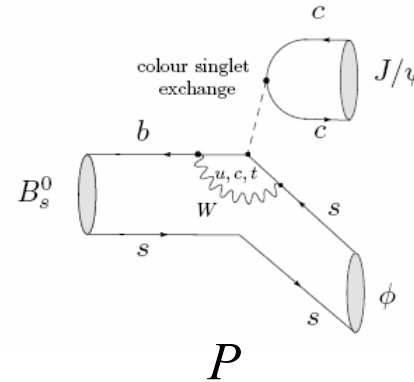
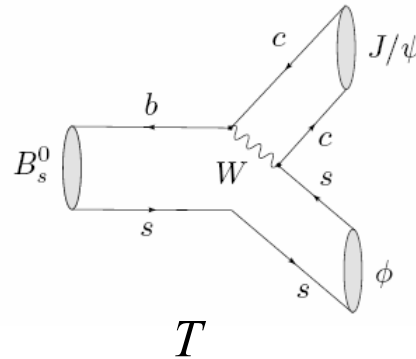


HFAG: consistency of SM predictions is at level of  $2.2 \sigma$

# $B_s \rightarrow J/\psi\phi$ : Role of penguins

Faller, Fleischer, Mannel  
PRD 79 (09) 014005

Tree and penguin topologies contribute:



$$A(B_s^0 \rightarrow (J/\psi\phi)_f) = \lambda_c (T + P^c) + \lambda_u P^u + \lambda_t P^t$$

$f = 0, \parallel, \perp$

$$\lambda_q = V_{qs} V_{qb}^*$$

$$\lambda_t = -\lambda_u - \lambda_c$$

Defining:

$$Q_f = \lambda^2 A(T + P_c - P_t) \quad R_b = \left(1 - \frac{\lambda^2}{2}\right) \frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right| \quad \varepsilon = \frac{\lambda^2}{1 - \lambda^2}$$

$$a_f e^{i\theta_f} = R_b \left[ \frac{P_u - P_t}{T + P_c - P_t} \right] \longrightarrow \theta_f \text{ strong CP-invariant phase}$$



$$A(B_s^0 \rightarrow (J/\psi\phi)_f) = \left(1 - \frac{\lambda^2}{2}\right) Q_f \left[1 + \varepsilon a_f e^{i\theta_f} e^{i\gamma}\right]$$

$$A(\bar{B}_s^0 \rightarrow (J/\psi\phi)_f) = \eta_f \left(1 - \frac{\lambda^2}{2}\right) Q_f \left[1 + \varepsilon a_f e^{i\theta_f} e^{-i\gamma}\right]$$

Doubly ( $\varepsilon$ )  
Cabibbo-suppressed  
contributions:  
Negligible?

# $B_s \rightarrow J / \psi \phi$ : Role of penguins

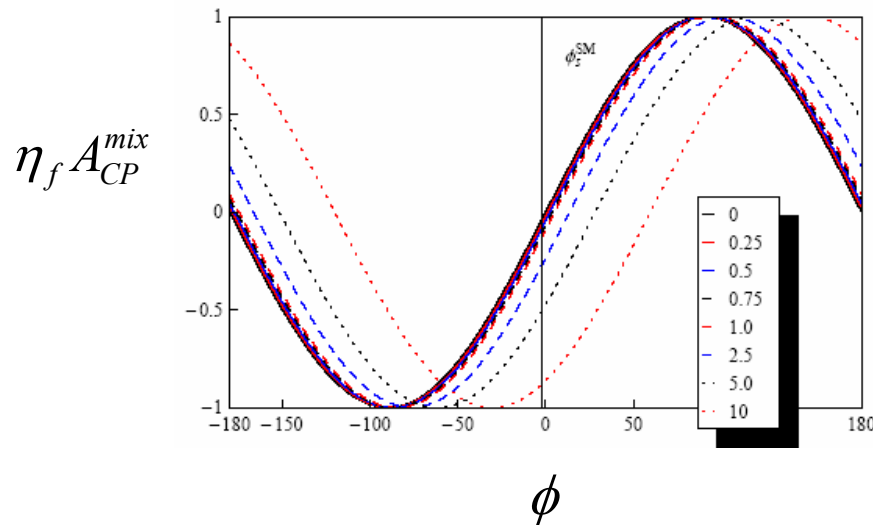
Reliable estimates of  $a_f, \theta_f$  are missing.

Factorization would predict  $\theta_f = 180^\circ$ .

Putting  $a_f = 0$  would give:  $A_{CP}^{mix} = \eta_f \sin \phi$



Now depends also on  $a_f, \theta_f$



→ obtained for  $\theta_f = 180^\circ$

Values of  $a_f \approx 1$   
could lead to  $\eta_f A_{CP}^{mix} \approx O(-10\%)$

$B_s \rightarrow J / \psi \phi$  : Role of penguins

Control channel:  $B_s^0 \rightarrow J / \psi K^{*0}$

Two quantities to be exploited:

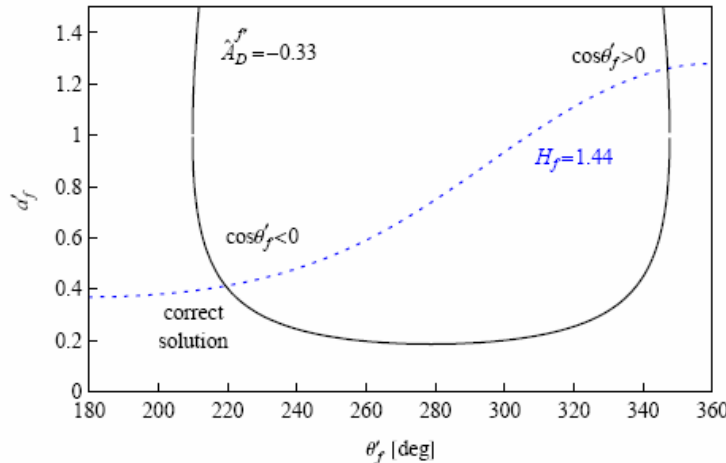
$$H_f = \frac{1}{\varepsilon} \left| \frac{Q_f}{Q'_f} \right|^2 \frac{\Gamma'(f, t=0)}{\Gamma(f, t=0)} = \frac{1 - 2a'_f \cos \theta'_f \cos \gamma + a'^2_f}{1 + 2\varepsilon a_f \cos \theta_f \cos \gamma + \varepsilon^2 a^2_f}$$

$$A_{CP}^{dir} = \frac{2a'_f \sin \theta'_f \sin \gamma}{1 - 2a'_f \cos \theta'_f \cos \gamma + a'^2_f}$$

Primed quantities refer to  $B_s^0 \rightarrow J / \psi K^{*0}$

Measuring  $H_f, A_{CP}^{dir}$  would fix  $a'_f \approx a_f \quad \theta'_f \approx \theta_f$

Example:



The twofold ambiguity may be solved by comparison with  $B_d \rightarrow J / \psi \rho$

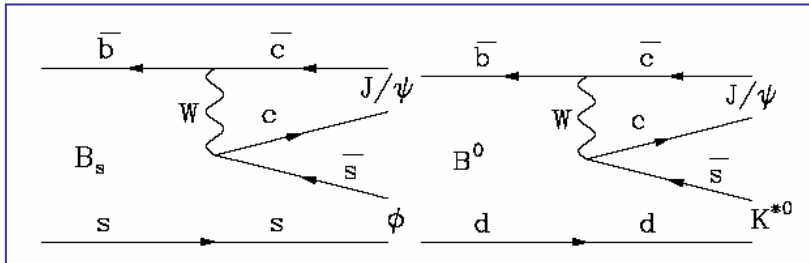
However notice that theoretical estimates provide  $\left| \frac{Q'_f}{Q_f} \right| \approx 0.2 - 1.0$

# SU(3) accuracy: The case of the strong phases

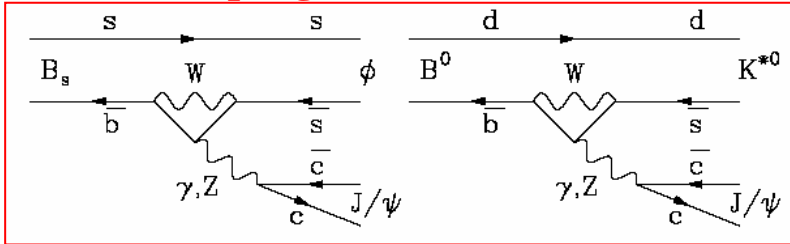
Extracting strong phases from  $B_d \rightarrow J/\psi K^{*0}$  (as already used by D0) would solve the discrete ambiguity in the determination of  $\phi$

Analogous topologies:

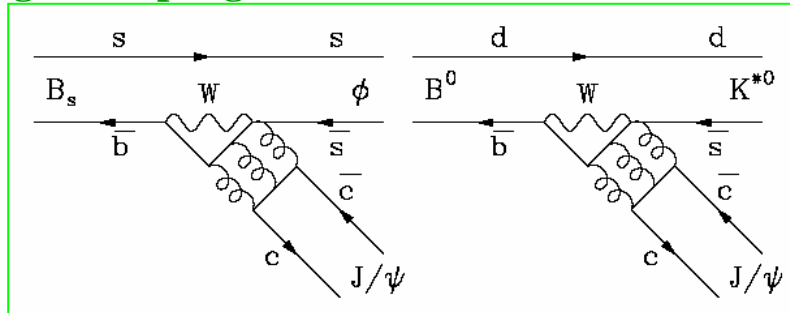
tree



electroweak penguins



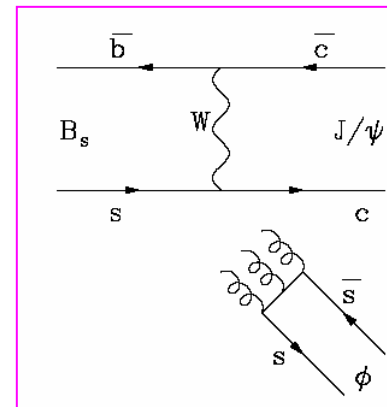
gluonic penguins



**Problem:**  $\phi$  has also a singlet component



extra diagrams



→ OZI suppressed

+ others

doubly OZI supp.

This has a counterpart in  $B_d \rightarrow J/\psi \phi$  where it has been estimated to be negligible

The similarity of amplitudes and strong phases in  $B_s \rightarrow J/\psi \phi$  and  $B_d \rightarrow J/\psi K^{*0}$  seems a well-founded assumption

# Other channels induced by $\bar{b} \rightarrow \bar{c}c\bar{s}$

M.V. Carlucci, P. Colangelo, FDF  
in preparation

☀ A different charmonium state:

$$B_s \rightarrow \psi(2S)\phi, \quad B_s \rightarrow \chi_{c0}\phi, \quad B_s \rightarrow \eta_c\phi$$

☀  $\psi$  + a different light meson:

$$\begin{array}{ll} B_s \rightarrow \psi\eta & \eta_f = +1 \\ B_s \rightarrow \psi\eta' & \eta_f = +1 \end{array}$$

$$B(B_s \rightarrow \psi\eta) = 9.3 \times 10^{-5}$$

$$B(B_s \rightarrow \psi\eta') = 1.3 \times 10^{-4}$$

Necessity to detect  
photons in the final state

$$B_s \rightarrow \psi f_0(980) \quad \eta_f = -1$$

Improving theoretical prediction

- comparing different form factor sets
- exploiting results of SCET-based sum rules
- describing  $\eta$ - $\eta'$  mixing in the flavour basis

Twofold role of  $f_0$ : - background to  $B_s \rightarrow J/\psi\phi$   
- interesting final state with  $f_0(980) \rightarrow \pi^+\pi^-$

## Contribution of S-wave to $B_s \rightarrow J/\psi\phi$

There might be an S-wave contribution to the  $K^+K^-$  system in the region of the  $\phi$

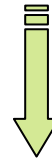


- it would bias the result
- neglecting this contribution makes the error smaller

In the case of  $B_d \rightarrow J/\psi K^{*0}$  BaBar finds that the S-wave component  $K\pi$  is  $\sim 8\%$

BaBar PRD 76 (07) 031102

It may be argued that due to the narrowness of  $\phi$  ( $\Gamma=4.3$  MeV )  
with respect to  $K^*$  ( $\Gamma=51$  MeV ) the S-wave component under the  $\phi$  is smaller



True?



Hints on the role of S-wave contribution from other channels

$$D_s \rightarrow K^+ K^- \pi^+$$

$$\frac{\Gamma(D_s^+ \rightarrow f_0(980)\pi^+ \rightarrow K^+ K^- \pi^+)}{\Gamma(D_s^+ \rightarrow \phi\pi^+ \rightarrow K^+ K^- \pi^+)} = 0.3 \pm 0.1$$

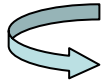
→ Analysis done over all of phase space  
What about the low mass region?

Recent analysis performed by CLEO in the low mass region fitting data with a BW for the  $\phi$  plus a linear S-wave component

Conclusion: **The fraction of S-wave depends on the mass interval considered but is  $O(10\%)$  in the region around  $\phi$**

# Contribution of S-wave to $B_s \rightarrow J/\psi\phi$

How to get rid of this contribution?



Partial wave analysis

□ BaBar:  $D_s^+ \rightarrow \pi^+ K^+ K^-$

□ Spherical harmonics moments  $Y_l^0$

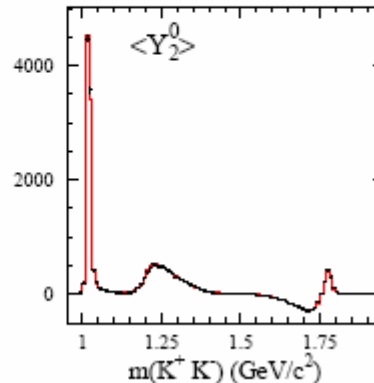
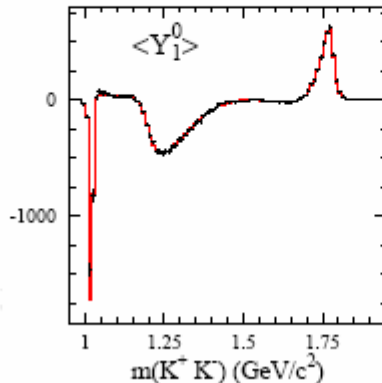
□ S, P waves and relative phase can be extracted using:

$$\sqrt{4\pi}Y_0^0 = S^2 + P^2$$

$$\sqrt{4\pi}Y_1^0 = 2SP\cos\phi$$

$$\sqrt{4\pi}Y_2^0 = 0.894P^2$$

$K^+ K^-$



Large interference between S-wave ( $f_0(980)$ ) and P-wave ( $\phi(1020)$ ) in  $Y_1^0$

$Y_2^0$  takes contribution only from P-wave

A. Palano, talk at LHC-b meeting  
Bologna, January 09

[www.ba.infn.it/~palano/antimo\\_f0.pdf](http://www.ba.infn.it/~palano/antimo_f0.pdf)

$$B_s \rightarrow J/\psi f_0 \quad f_0 \rightarrow \pi^+ \pi^-$$

- No angular analysis required
- No photons to detect

From analysis of BaBar data about the modes  $D_s^+ \rightarrow \pi^+ \pi^- \pi^+$   $D_s^+ \rightarrow K^+ K^- \pi^+$   
It is expected that

$$\frac{B(B_s \rightarrow J/\psi f_0, f_0 \rightarrow \pi^+ \pi^-)}{B(B_s \rightarrow J/\psi \phi, \phi \rightarrow K^+ K^-)} = (19 \pm 2)\%$$



New Physics or not New Physics....

$$\Delta m_s$$

Experimental weighted average (HFAG)

$$\Delta m_s = 17.78 \pm 0.12 \text{ ps}^{-1}$$

To be compared to (Lenz & Nierste 07) :

$$\Delta m_s^{SM} = (19.30 \pm 6.68) \text{ ps}^{-1}$$

What happens in other NP scenarios?

$\Delta m_s > (\Delta m_s)^{SM}$  is favoured in

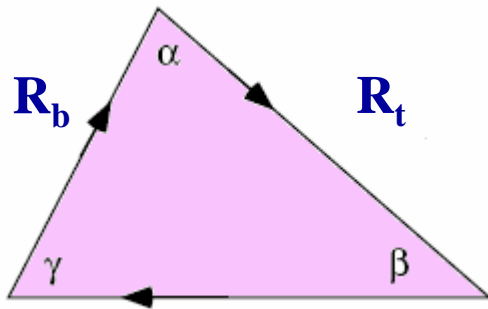
- Two Higgs Doublet Model type II
- MSSM with low  $\tan \beta$
- Littlest Higgs model without T-parity
- Universal Extra dimensions

$\Delta m_s < (\Delta m_s)^{SM}$  is favoured in

- MSSM with MFV and large  $\tan \beta$

$$\Delta m_s$$

Relations between  $\Delta m_s$  and other observables hold either in SM or in MFV. Violation of such relations would imply new low energy operators and/or new sources of flavour/CP violation



$$R_b = \sqrt{1 + R_t^2 - 2R_t \cos \beta}$$
$$\cot \gamma = \frac{1 - R_t \cos \beta}{R_t \sin \beta}$$

$R_b$  and  $\gamma$  can be determined from tree level decays

$R_t$  and  $\beta$  from loop-induced processes and are therefore sensitive to NP

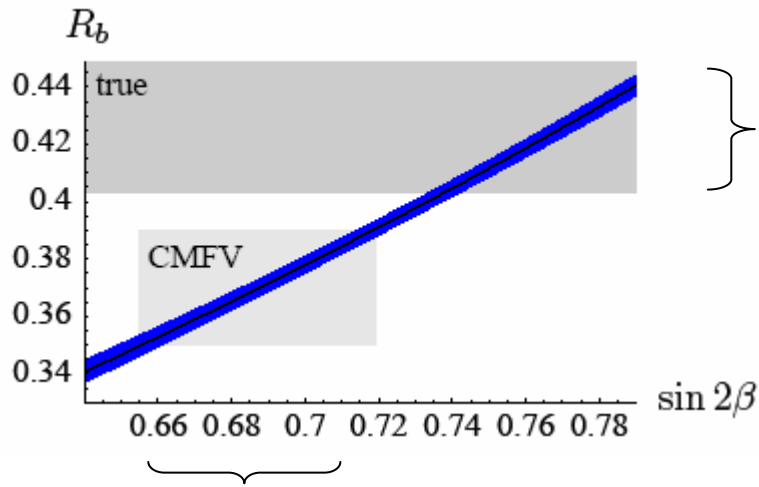


testing the previous relations may reveal NP effects

Recall that

$$R_t \Leftrightarrow \Delta m_s$$
$$\sin 2\beta \Leftrightarrow A_{CP}^{mix}(B_d \rightarrow J/\psi K_s)$$

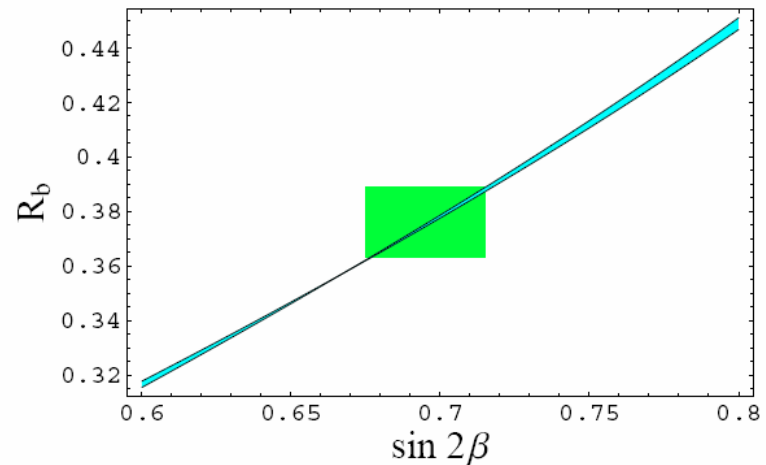
$$\Delta m_s$$



Value of  $R_b$  from tree level processes

Measured value of  $\sin 2\beta$

Updated values of  $\xi$  and of  $\Delta m_s$  seem to give a better agreement

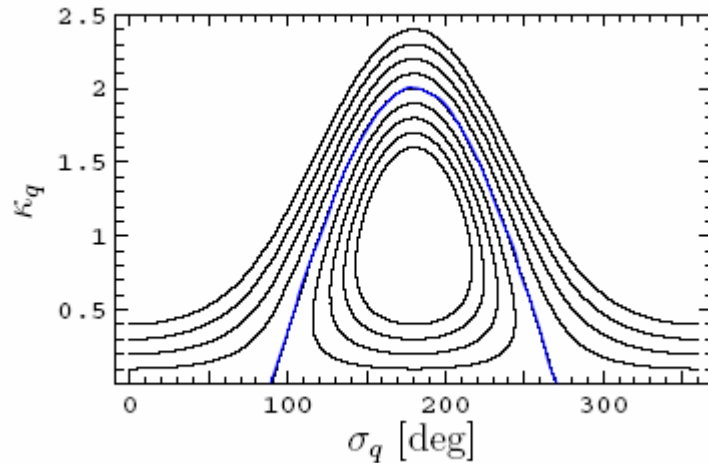


$$\Delta m_s$$

Effect of possible new physics on  $\Delta m_s \rightarrow \Delta m_s = \Delta m_s^{SM} \left[ 1 + k_s e^{i\sigma_d} \right]$

Quantify the deviation from the SM  $\rightarrow$

$$\rho_s = \left| \frac{\Delta m_s^{\text{exp}}}{\Delta m_s^{SM}} \right| = \sqrt{1 + 2k_s \cos \sigma_s + k_s^2}$$



The blue line is  $\rho_s=1$



Even the perfect coincidence of  $\Delta m_s^{\text{exp}}$  with  $\Delta m_s^{SM}$  would not exclude NP in  $B_s$  mixing: There are anyway allowed regions in the  $(\sigma_s, k_s)$  plane





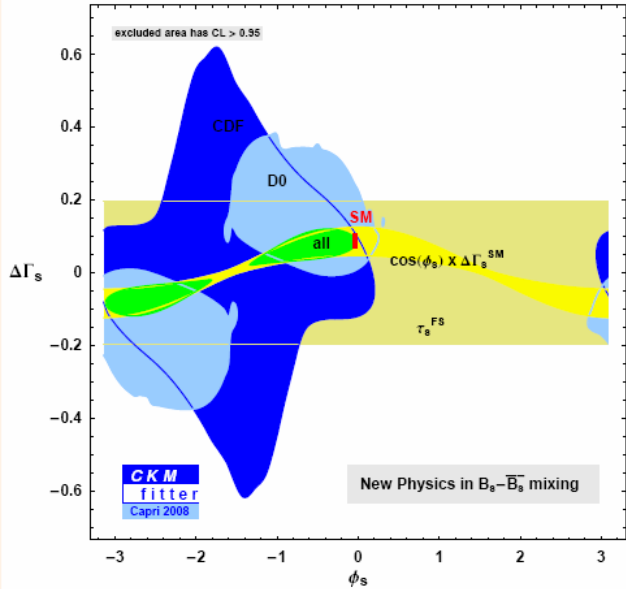
UTfit

FIRST EVIDENCE OF NEW PHYSICS IN  $b \leftrightarrow s$  TRANSITIONS  
(UTfit Collaboration)

With the procedure we followed to combine the available data, we obtain an evidence for NP at more than  $3\sigma$ .

UTfit Collab., 0803.0659

CKMfitter



J. Charles, Talk @ 2nd Workshop on Theory, Phenomenology & Experiments in HF Physics - Capri 08

using all  $(\phi_s, \Delta\Gamma_s)$  inputs,  
 $\phi_s = -2\beta_s$  is excluded at  $2.4\sigma$ ,  
while the 2D hypothesis  $\phi_s = -2\beta_s,$   
 $\Delta\Gamma_s = \Delta\Gamma_s^{SM}$  is excluded at only  $1.9\sigma$

in contrast to UTfit, we do not find an "evidence" ( $\geq 3\sigma$ ) for New Physics in  $\phi_s$ , even with the non conservative treatment of Tevatron data errors

# New Physics: a model independent parameterisation

New Physics may affect  $\Delta M_s$  and  $\phi_s \rightarrow$

$$\Delta m_s = \Delta m_s^{SM} \left[ 1 + k_s e^{i\sigma_d} \right]$$

$$\phi_s = \phi_s^{SM} + \phi_s^{NP} = \phi_s^{SM} + \arg(1 + k_s e^{i\sigma_d})$$

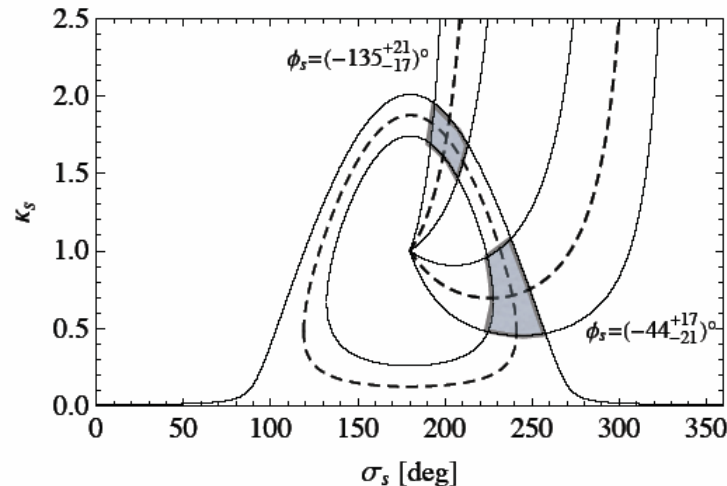


$$\rho_s = \frac{|\Delta m_s^{\text{exp}}|}{\Delta m_s^{SM}} = \sqrt{1 + 2k_s \cos \sigma_s + k_s^2} \quad \Rightarrow \quad k_s = -\cos \sigma_s \pm \sqrt{\rho_s^2 - \sin^2 \sigma_s}$$

$$k_s = \frac{\tan \phi_s^{NP}}{\sin \sigma_s - \cos \sigma_s \tan \phi_s^{NP}}$$



Constraints in the  $(\sigma_s, k_s)$  plane



## Rare $b \rightarrow s$ induced $B_s$ decays

Can provide information on NP scenarios, in particular can constrain the size of possible extra dimensions

### Appelquist-Cheng-Dobrescu (ACD) Model with a single Universal Extra Dimension (UED)

- Compactification on a orbifold: the 5th dim  $y$  varies on a circle of radius  $R$  with periodic boundary conditions; fields are required to have a definite parity under  $y \rightarrow -y$
- MFV model
- The existence of an extra dim reflects in the appearance of a tower of KK modes for each particle of the model



Modification of the Wilson coefficients in effective hamiltonians

$$C\left(x_t, \frac{1}{R}\right) = C_{(0)}(x_t) + \sum_{n=1}^{\infty} C_n(x_t, x_n) \quad x_n = \frac{m_n^2}{M_W^2}$$

SM result

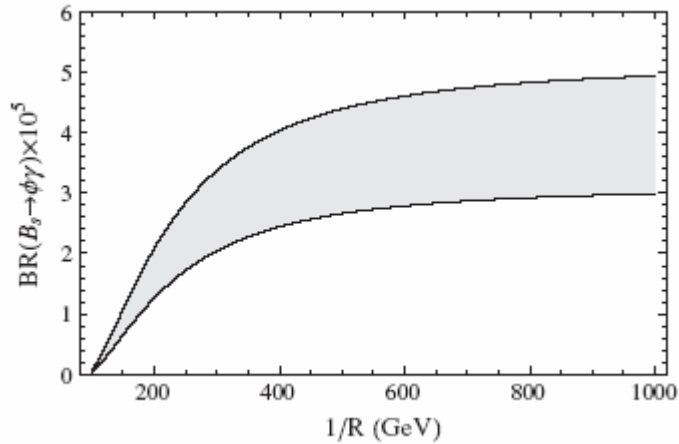
$$m_n = \frac{n}{R}$$

A bound on  $1/R$  might be established studying various observables in these modes

Colangelo, Ferrandes, Pham, FDF  
PRD 77 (08) 019

$B_s \rightarrow \phi \gamma$

Branching ratio vs  $1/R$



SM result

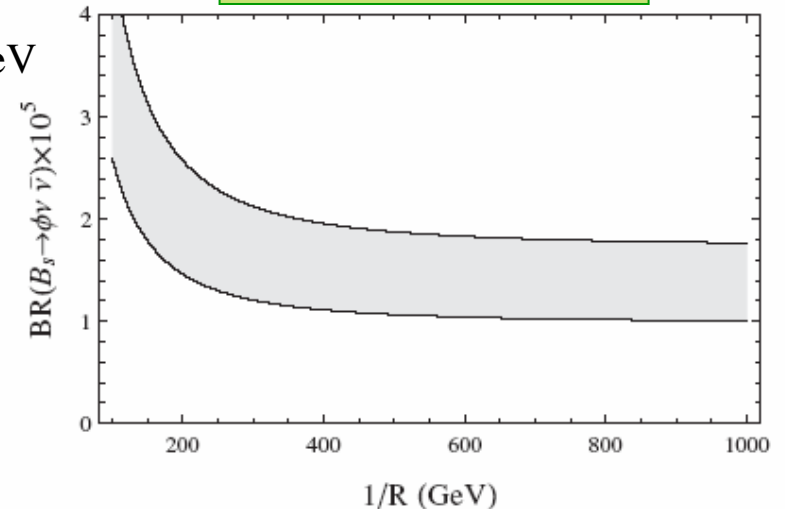
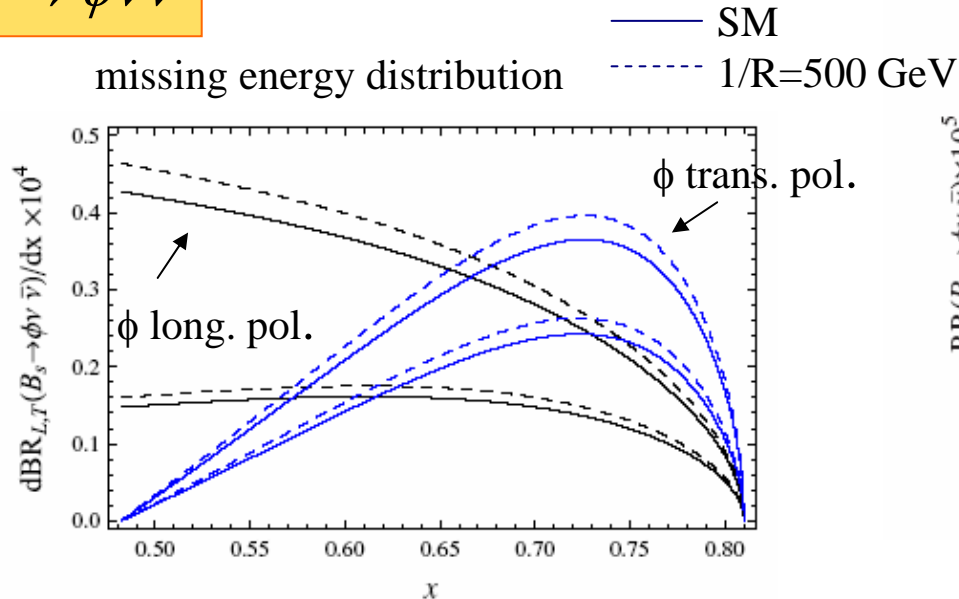
$$\mathcal{B}(B_s \rightarrow \phi \gamma) = (4.2 \pm 0.3) \times 10^{-5}$$

To be compared to Belle's result

$$\mathcal{B}(B_s \rightarrow \phi \gamma)_{\text{exp}} = (5.7^{+1.8}_{-1.5}(\text{stat})^{+1.2}_{-1.1}(\text{syst})) \times 10^{-5}$$

$B_s \rightarrow \phi \nu \bar{\nu}$

Branching ratio vs  $1/R$



SM

$$\mathcal{B}(B_s \rightarrow \phi \nu \bar{\nu}) = (1.4 \pm 0.4) \times 10^{-5}$$

# Conclusions

$B_s$  Physics will give us fundamental insights in the research for New Physics

## Future directions:

- reduction of theoretical and experimental uncertainties
- explore new channels
- analyse rare  $B_s$  decays as a probe of new Physics  
(combine with analogous information from rare B decays)

# Incontri di Fisica delle Alte Energie

IFAE 2009 - VIII Edizione

15 - 17 Aprile  
Bari

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Fisica del Sapore  
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gli incontri si terranno presso il Centro Congressi - Palace Hotel - via Lombardi 13

Backup slides

## Untagged decays

$$\begin{aligned}\Gamma(f, t) &= \Gamma(B^0(t) \rightarrow f) + \Gamma(\bar{B}^0(t) \rightarrow f) = \\ &= N_f |A_f|^2 \left(1 + |\lambda_f|^2\right) e^{-\Gamma t} \left[ \cosh\left(\frac{\Delta\Gamma t}{2}\right) + A_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma t}{2}\right) \right]\end{aligned}$$

Integrating over time:

$$\begin{aligned}Br(f)_{\text{untagged}} &= \frac{1}{2} \int_0^{\infty} dt \Gamma(f, t) = \\ &= \frac{N_f}{2} |A_f|^2 \left(1 + |\lambda_f|^2\right) \frac{1}{\Gamma} \left[ 1 + \frac{\Delta\Gamma}{2\Gamma} A_{\Delta\Gamma} + \mathcal{O}\left(\frac{(\Delta\Gamma)^2}{\Gamma^2}\right) \right]\end{aligned}$$



$$\Gamma(f, t) = 2Br(f)_{\text{untagged}} \Gamma e^{-\Gamma t} \left[ 1 + \frac{\Delta\Gamma}{2} A_{\Delta\Gamma} \left(t - \frac{1}{\Gamma}\right) \right] + \mathcal{O}\left((\Delta\Gamma t)^2\right)$$

A fit to this quantity allows to determine the product

$$\Delta\Gamma \cdot A_{\Delta\Gamma}$$



# Asymmetries in $fs$ final state

$$A_0(t) = \frac{\Gamma(B^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow \bar{f})}{\Gamma(B^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow \bar{f})}$$

When  $f=fs$

$$\Gamma(B^0(t) \rightarrow f) = N_f |A_f|^2 \frac{e^{-\Gamma t}}{2} \left[ \cosh\left(\frac{\Delta\Gamma t}{2}\right) + \cos(\Delta m t) \right]$$

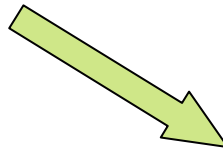
$$\Gamma(B^0(t) \rightarrow \bar{f}) = N_f |\bar{A}_{\bar{f}}|^2 \frac{e^{-\Gamma t}}{2} (1-a) \left[ \cosh\left(\frac{\Delta\Gamma t}{2}\right) - \cos(\Delta m t) \right]$$

Assuming no direct CP violation:  $A_f = \bar{A}_{\bar{f}}$



$$A_{fs}(t) = \frac{\cos(\Delta m t)}{\cosh\left(\frac{\Delta\Gamma t}{2}\right)} + \frac{a}{2} \left[ 1 - \frac{\cos^2(\Delta m t)}{\cosh^2\left(\frac{\Delta\Gamma t}{2}\right)} \right]$$

$a$  being small:  $a = \frac{\Delta\Gamma}{\Delta m} \text{tg}\phi$



May give access to  $\Delta\Gamma$