

Solar physics and solar neutrinos

F. L. Villante – University of L'Aquila and LNGS-INFN

Hydrogen Burning: PP chain and CNO cycle

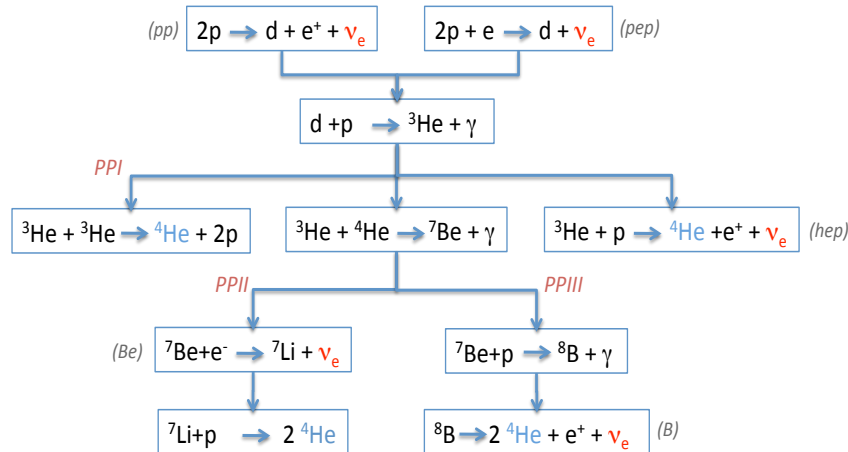
The Sun is powered by nuclear reactions that transform H into ^4He :



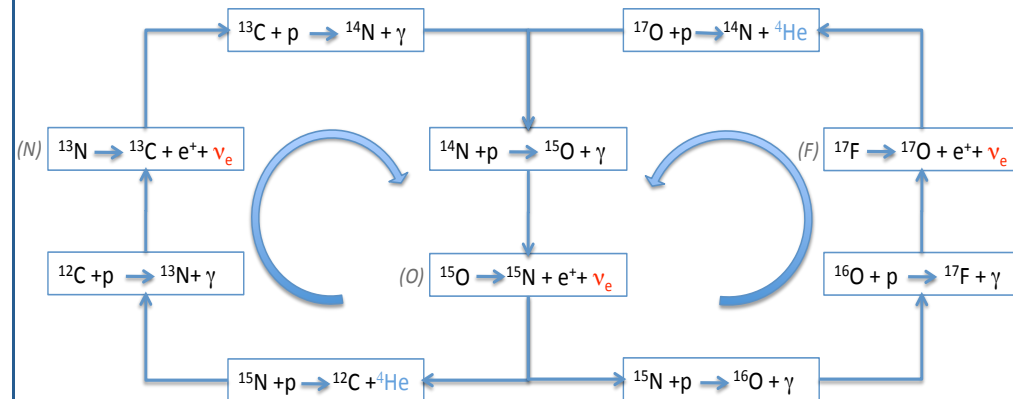
$Q = 26,7 \text{ MeV}$ (globally)

Free stream – 8 minutes to reach the earth
Direct information on the energy producing region.

The PP-chain



The CN-NO bi-cycle

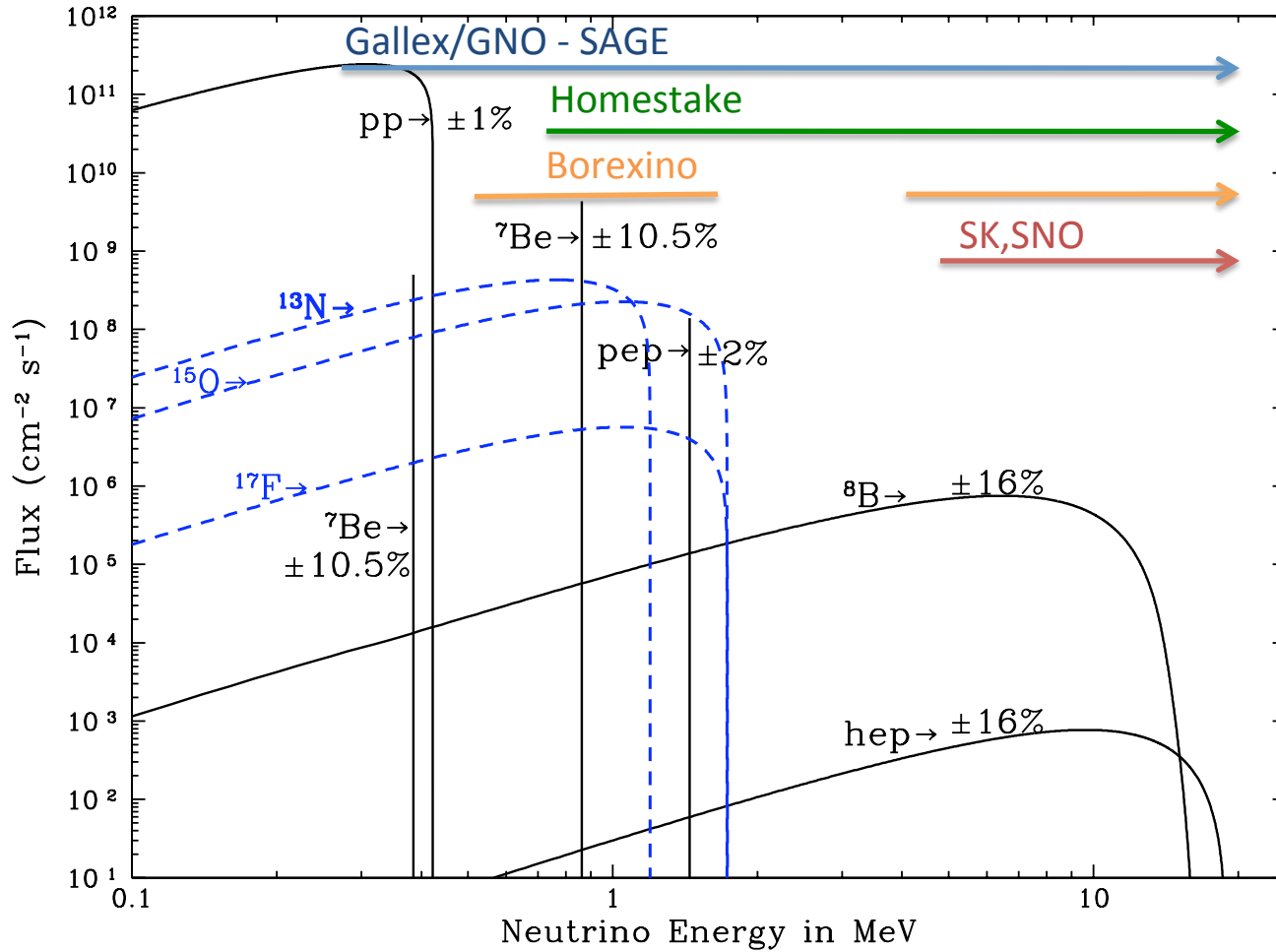


The **pp chain** is responsible for about 99% of the total energy (and neutrino) production.

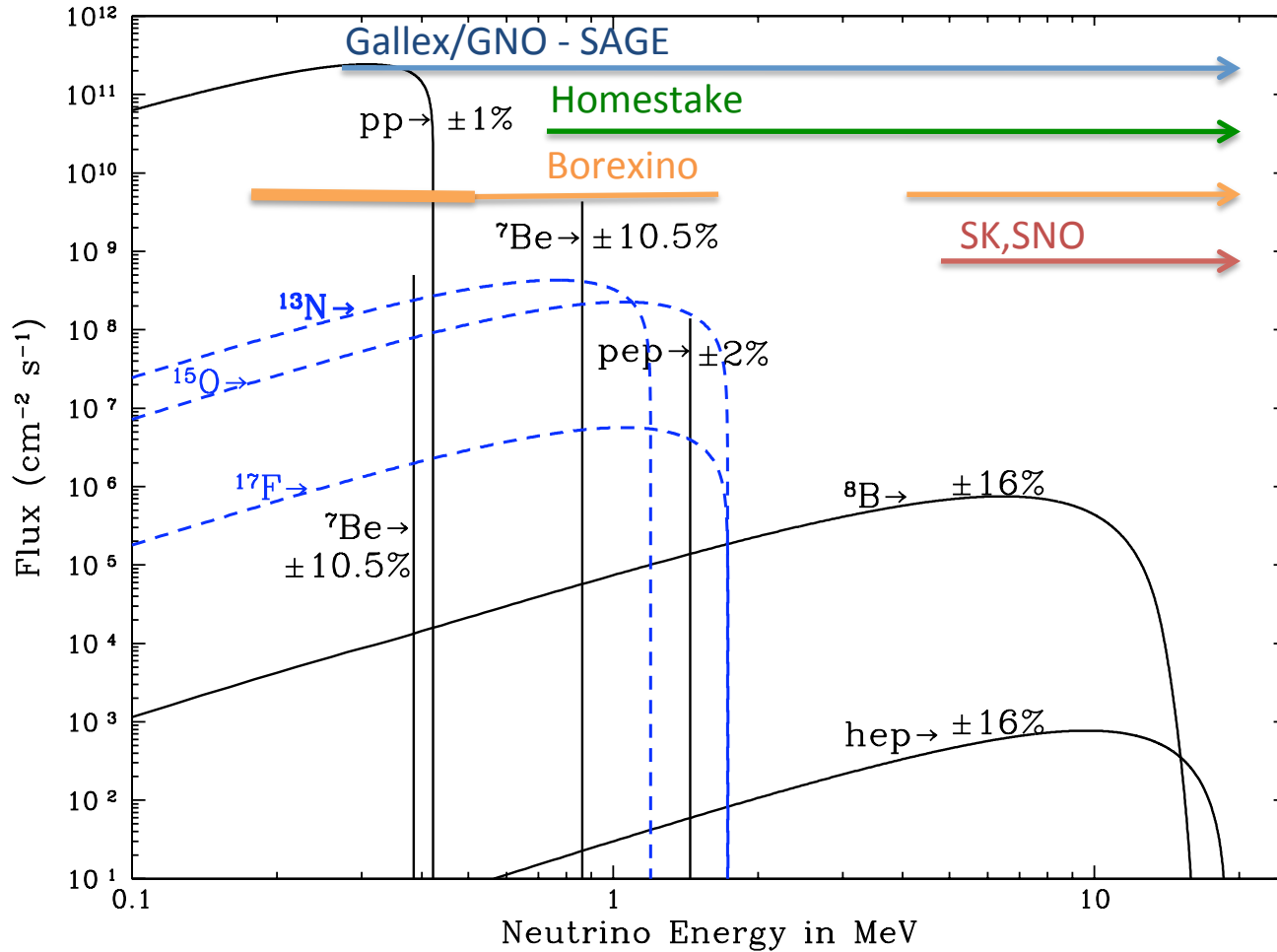
C, N and O nuclei are used as catalysts for hydrogen fusion.

CNO cycle is responsible for about 1% of the total neutrino (and energy) budget. Important for more advanced evolutionary stages

The solar neutrino spectrum



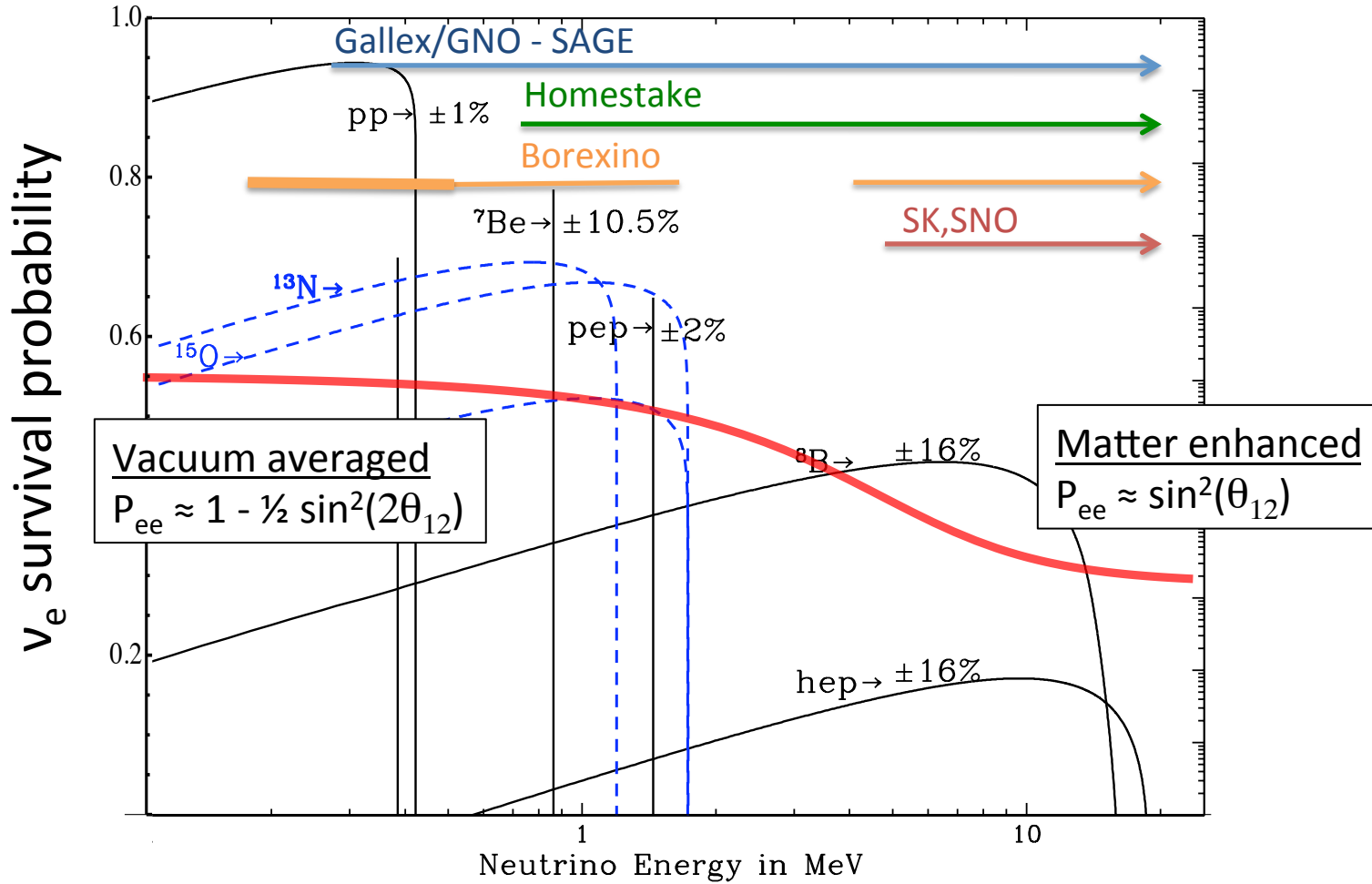
The solar neutrino spectrum



$$\Phi_{pp} = (6.6 \pm 0.7) \times 10^{10} \text{ cm}^{-2} \text{ s}^{-1}$$

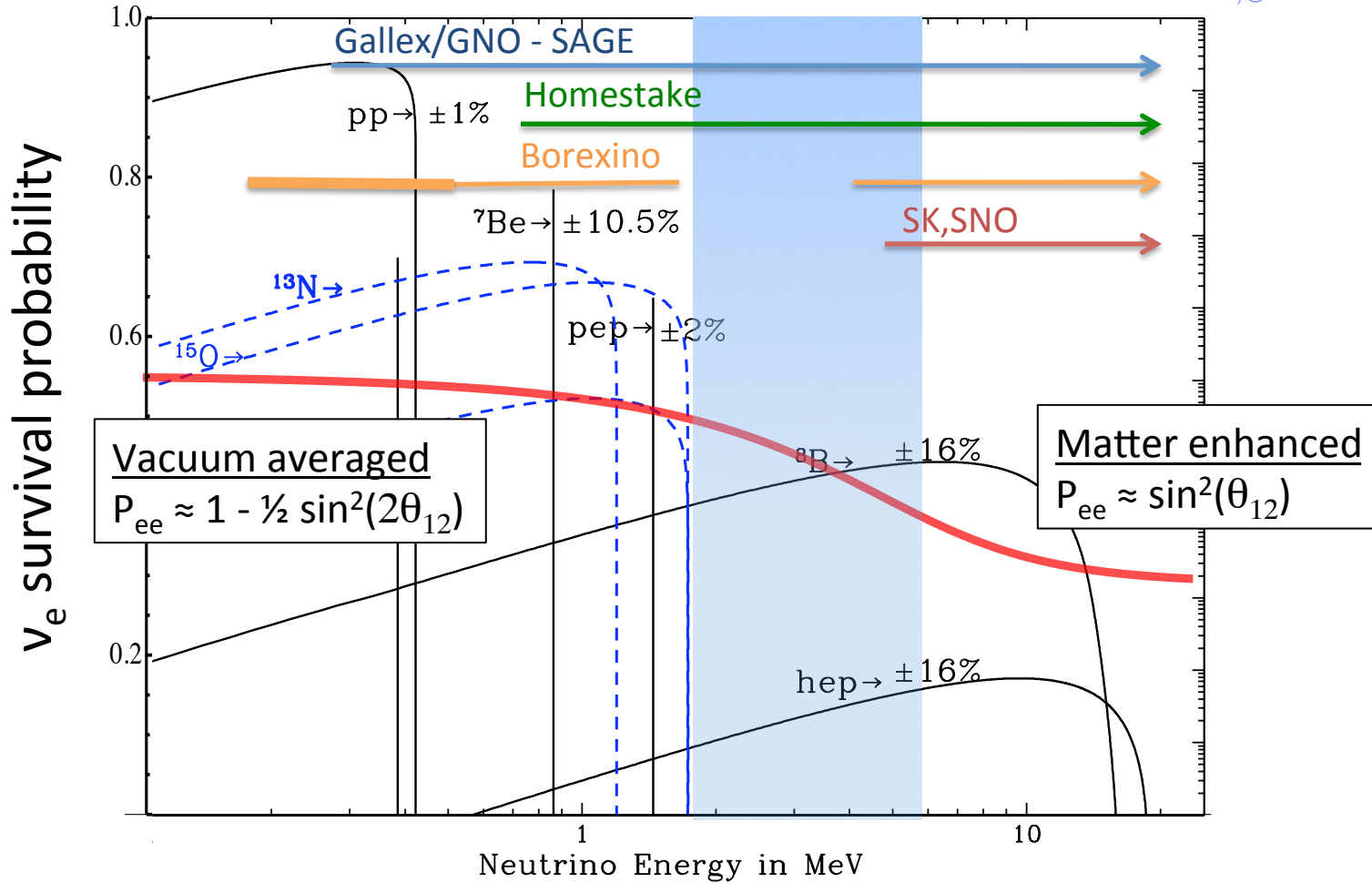
Borexino, Nature 2014
**First direct measurement of
the solar pp-component**

The solar neutrino survival probability



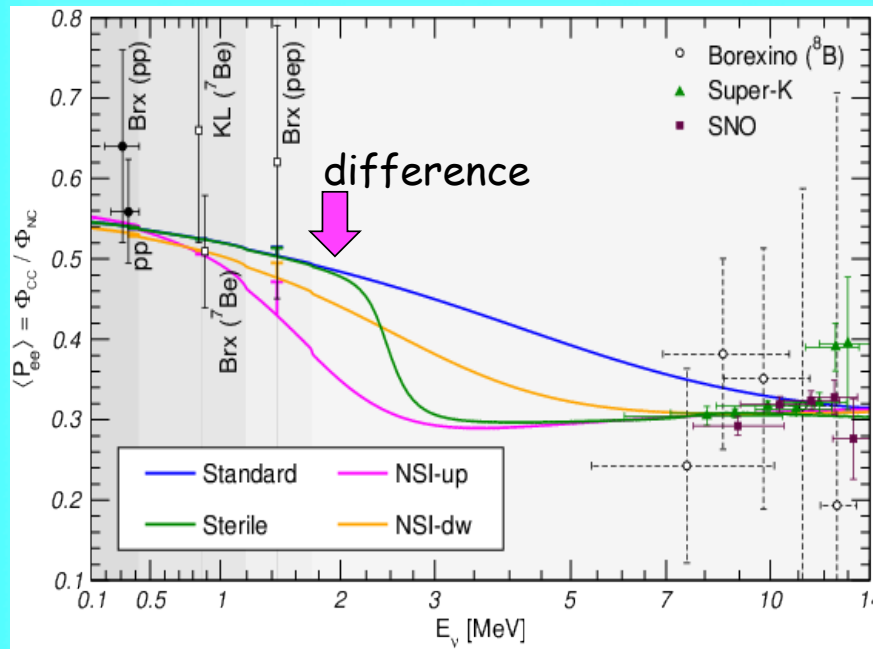
The solar neutrino survival probability

“Transition” at: $E^* = \frac{\Delta m_{21}^2 \cos(2\theta_{12})}{2\sqrt{2} G_F n_{e,\odot}}$



Confirm LMA-MSW
Search for new physics

New physics effects



M. Maltoni, A.Y.S.

Extra sterile neutrino with $\Delta m_{01}^2 = 1.2 \times 10^{-5} \text{ eV}^2$, and $\sin^2 2\alpha = 0.005$

Non-standard interactions with

$$\varepsilon_D^u = -0.22, \varepsilon_N^u = -0.30$$

$$\varepsilon_D^d = -0.12, \varepsilon_N^d = -0.16$$

NSI due exchange by light (MeV scale mass) mediators with small couplings allow to avoid existing bounds

*M. Pospelov
Y. Farzan*

The present situation

Experimental results agree with *Standard Solar Models (SSM)* + flavor oscillations:

Serenelli, Haxton, Pena-Garay, ApJ 2011

ν flux	AGSS09	GS98	Solar
Φ_{pp}	6.03 (1 ± 0.006)	5.98 (1 ± 0.006)	6.05 ($1^{+0.003}_{-0.011}$)
Φ_{pep}	1.47 (1 ± 0.012)	1.44 (1 ± 0.012)	1.46 ($1^{+0.010}_{-0.014}$)
Φ_{Be}	4.56 (1 ± 0.07)	5.00 (1 ± 0.07)	4.82 ($1^{+0.05}_{-0.04}$)
Φ_B	4.59 (1 ± 0.14)	5.58 (1 ± 0.14)	5.00 (1 ± 0.03)
Φ_{hep}	8.31 (1 ± 0.30)	8.04 (1 ± 0.30)	18 ($1^{+0.4}_{-0.5}$)
Φ_N	2.17 (1 ± 0.14)	2.96 (1 ± 0.14)	≤ 6.7
Φ_O	1.56 (1 ± 0.15)	2.23 (1 ± 0.15)	≤ 3.2
Φ_F	3.40 (1 ± 0.16)	5.52 (1 ± 0.16)	≤ 59

Units:

pp : $10^{10} \text{ cm}^2 \text{ s}^{-1}$;

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pep, N, O : $10^8 \text{ cm}^2 \text{ s}^{-1}$;

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^8B @ 3% (SNO & SK) and now ^7Be @ 4.5% (Borexino)

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otherwise solar luminosity matched @ 15% (Maltoni et al. 2010)

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$\Phi_{pp} = 6.6 (1 \pm 0.11)$ Borex. only
 $[\Phi_{pp} = 6.4 (1 \pm 0.08)]$ combined

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Direct measurement of pp now to 11% Borexino (90% CL)

$L_\nu(8 \text{ minutes}) \approx L_\nu(10^5 \text{ year})$ – test of solar stability

Still not accurate enough to test SSMs (\approx few % accuracy required)

Helioseismology

The Sun is a non radial oscillator. The observed oscillation frequencies can be used to determine the properties of the Sun. Linearizing around a known solar model:

$$\frac{\delta\nu_{nl}}{\nu_{nl}} = \int_0^R dr K_{u,Y}^{nl}(r) \frac{\delta u}{u}(r) + \int_0^R dr K_{Y,u}^{nl}(r) \delta Y + \frac{F(\nu_{nl})}{\nu_{nl}}$$

squared isothermal sound speed

Related to temperature stratification in the sun

surface helium abundance

See Basu & Antia 07
for a review

Impressive agreement with SSM predictions ...

Surface helium abundance

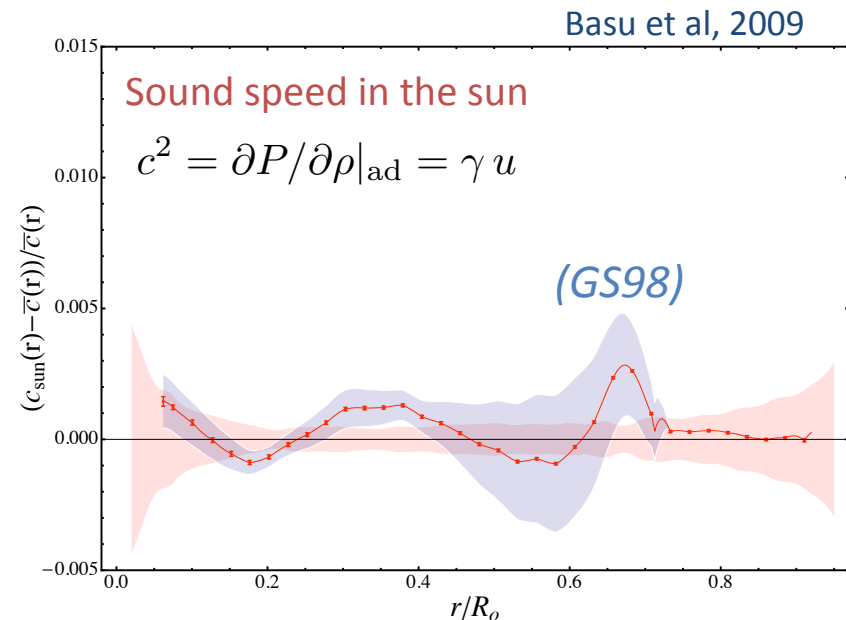
$$Y_b = 0.2485 \pm 0.0035$$

$$Y_b = 0.243 \quad (\text{GS98})$$

Inner radius of the solar convective envelope

$$R_b/R_\odot = 0.713 \pm 0.001$$

$$R_b/R_\odot = 0.712 \quad (\text{GS98})$$



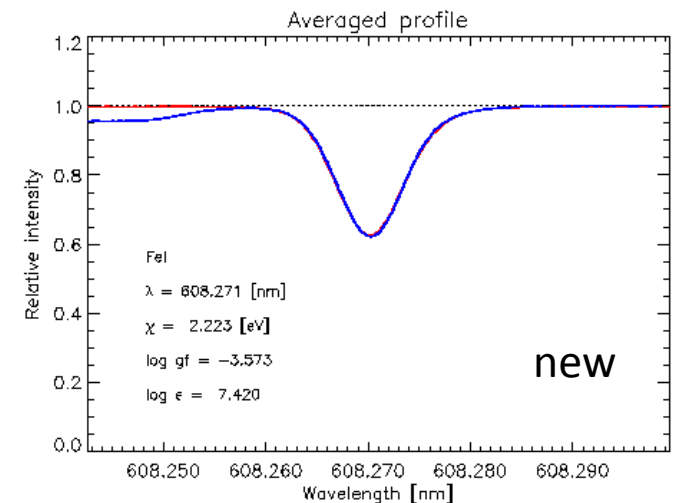
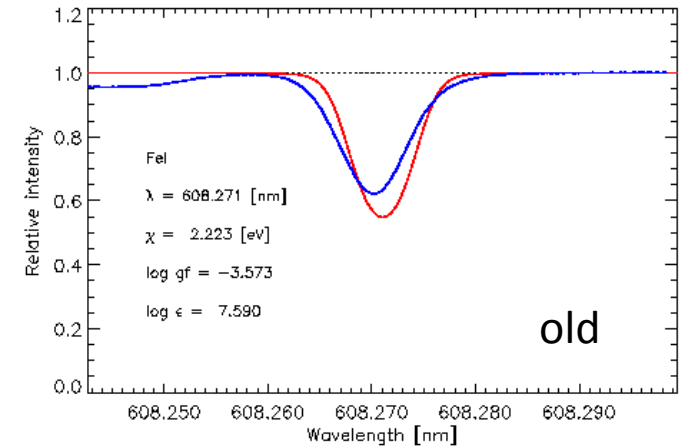
... till few years ago

Asplund et al. 05 (AGS05); Asplund et al. 09 (AGSS09)

Re-determination of the photospheric abundances of nearly all available elements (**inputs for SSM calculations**)

Improvements with respect to previous analysis^(*):

- 3D model instead of the classical 1D model of the lower solar atmosphere
- Careful and very demanding selection of the spectral lines... **AVOID blends!!! NOT TRIVIAL!!!**
- Careful choice of the atomic and molecular data **NOT TRIVIAL!!!!**
- NLTE instead of the classical LTE hypothesis... **WHEN POSSIBLE !!!**
- Use of **ALL** indicators (atoms as well as molecules,CNO)



^(*)N. Grevesse talk at PHYSUN10

Less metallic sun ...

AGS05 and AGSS09

Downward revision of heavy elements
photospheric abundances ...

Element	GS98	AGSS09	δz_i
C	8.52 ± 0.06	8.43 ± 0.05	0.23
N	7.92 ± 0.06	7.83 ± 0.05	0.23
O	8.83 ± 0.06	8.69 ± 0.05	0.38
Ne	8.08 ± 0.06	7.93 ± 0.10	0.41
Mg	7.58 ± 0.01	7.53 ± 0.01	0.12
Si	7.56 ± 0.01	7.51 ± 0.01	0.12
S	7.20 ± 0.06	7.15 ± 0.02	0.12
Fe	7.50 ± 0.01	7.45 ± 0.01	0.12
Z/X	0.0229	0.0178	0.29

$$[I/H] \equiv \log(N_I/N_H) + 12$$

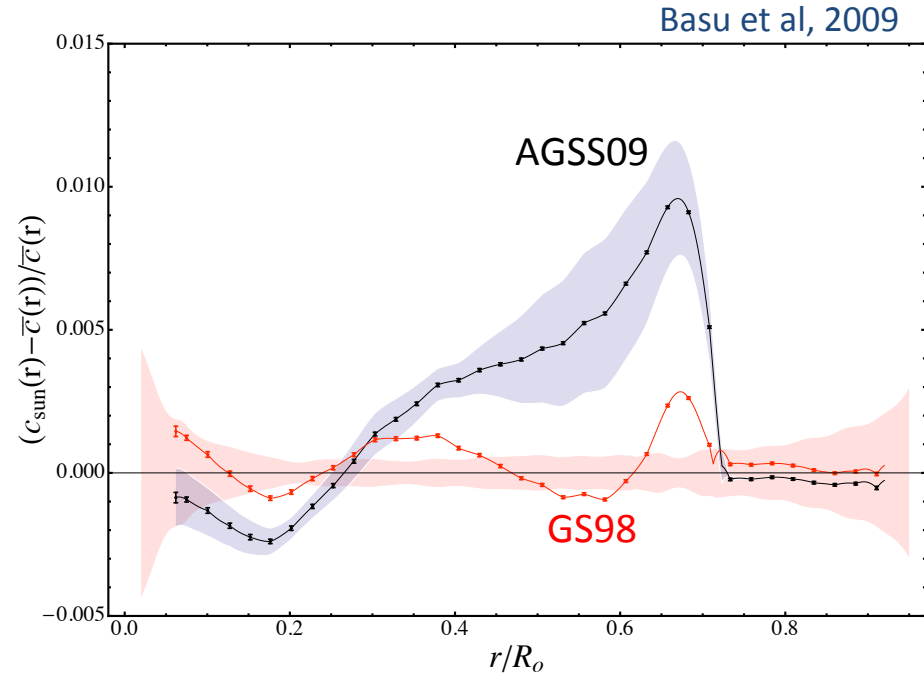
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... leads to SSMs which do not correctly reproduce helioseismic observables

	AGSS09	GS98	Obs.
Y_b	$0.2319 (1 \pm 0.013)$	$0.2429 (1 \pm 0.013)$	0.2485 ± 0.0035
R_b/R_\odot	$0.7231 (1 \pm 0.0033)$	$0.7124 (1 \pm 0.0033)$	0.713 ± 0.001
Φ_{pp}	$6.03 (1 \pm 0.005)$	$5.98 (1 \pm 0.005)$	$6.05 (1^{+0.003}_{-0.011})$
Φ_{Be}	$4.56 (1 \pm 0.06)$	$5.00 (1 \pm 0.06)$	$4.82 (1^{+0.05}_{-0.04})$
Φ_B	$4.59 (1 \pm 0.11)$	$5.58 (1 \pm 0.11)$	$5.00 (1 \pm 0.03)$
Φ_N	$2.17 (1 \pm 0.08)$	$2.96 (1 \pm 0.08)$	≤ 6.7
Φ_O	$1.56 (1 \pm 0.10)$	$2.23 (1 \pm 0.10)$	≤ 3.2

($\approx 4\sigma$ discrepancies)

The solar composition problem

There is something **wrong** or **unaccounted** in solar models

- Are properties of the solar matter (e.g. **opacity**) correctly described?
- Are the new abundances (i.e. the atmospheric model) **wrong**?
- Non standard effects (e.g. DM accumulation in the solar core)?
- Is the **chemical evolution** not understood (extra mixing?) or peculiar (accretion?) with respect to other stars?

Note that:

It is not just the problem of deciding between AGSS09 (new) and GS98 (old and presumably wrong) abundances

*The Sun provide the **benchmark** for stellar evolution. If there is something wrong in solar models, then this is wrong for all the stars ...*

Metals in the Sun

- Metals give a negligible contribution to EOS and energy generation

- Metals give a **substantial** contribution to **opacity**:

Energy producing region ($R < 0.3 R_{\odot}$)

$$\kappa_Z \approx \frac{1}{2} \kappa_{tot}$$

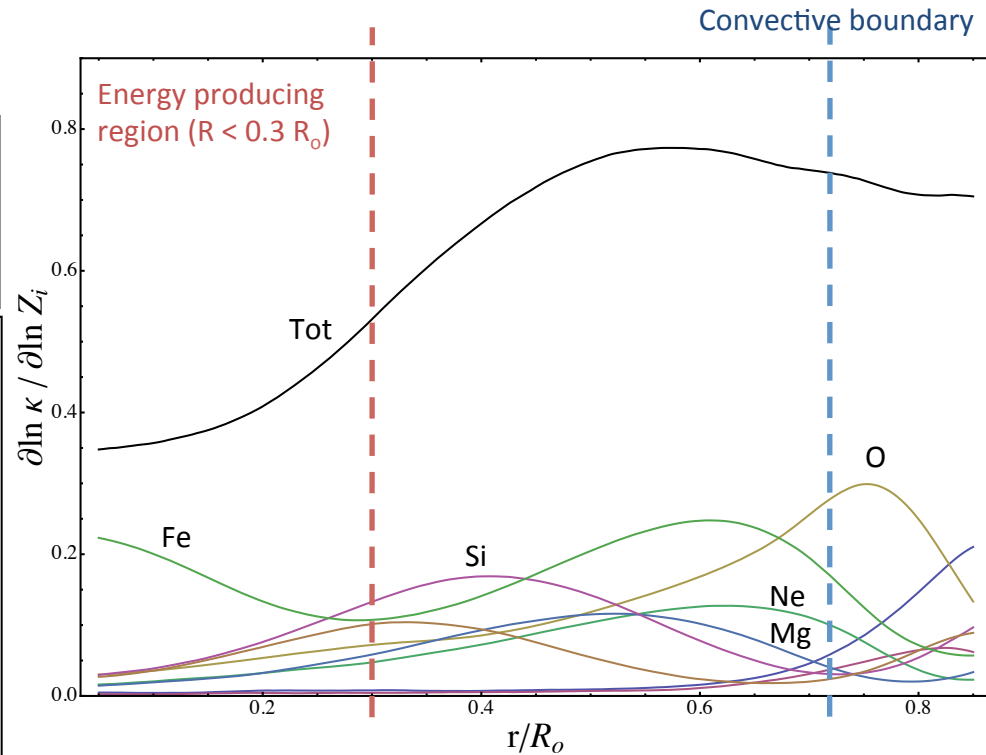
Fe gives the largest contribution.

Outer radiative region
($0.3 < R < 0.73 R_{\odot}$)

$$\kappa_Z \sim 0.8 \kappa_{tot}$$

Relevant contributions from several diff. elements (O, Fe, Si, Ne, ...)

- Z_{CNO} control the efficiency of CNO cycle



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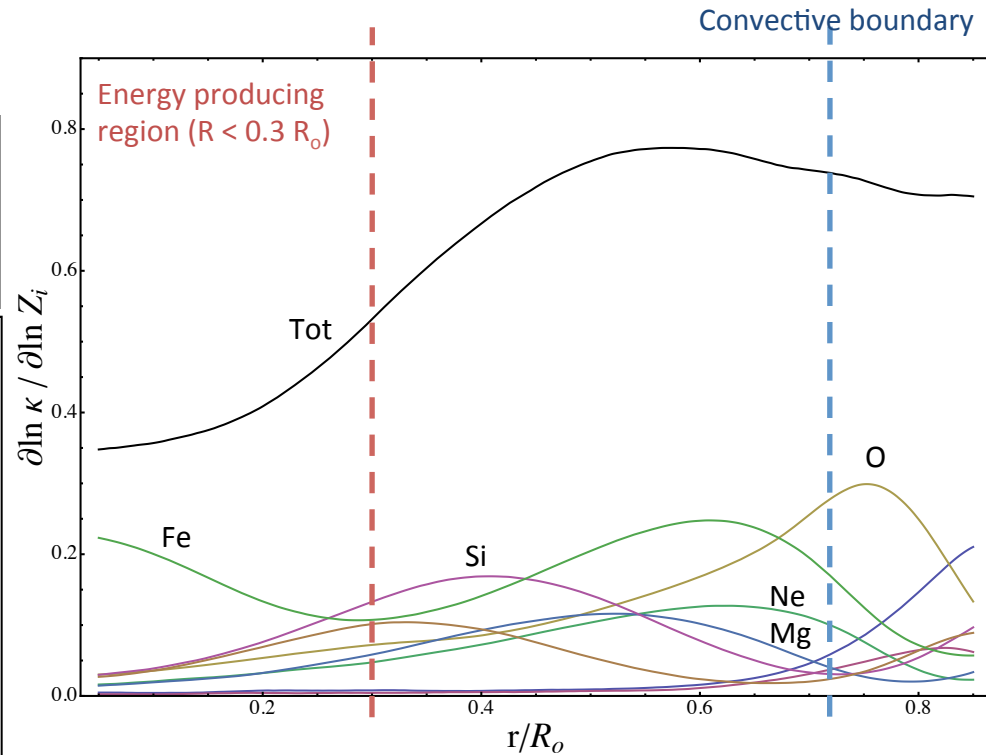
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*A change of solar composition produces the same effects on the helioseismic observables and on ^8B and ^7Be neutrinos of a **suitable change of the solar opacity profile $\delta\kappa(r)$.***

$$\delta\kappa(r) = \frac{\partial \ln \kappa(r)}{\partial \ln Z_j} \delta z_j$$

What we know about the opacity profile of the present sun?

The solar opacity profile

The “optimal” opacity profile (**i.e. the temperature stratification**) of the Sun is **well determined** by observational data

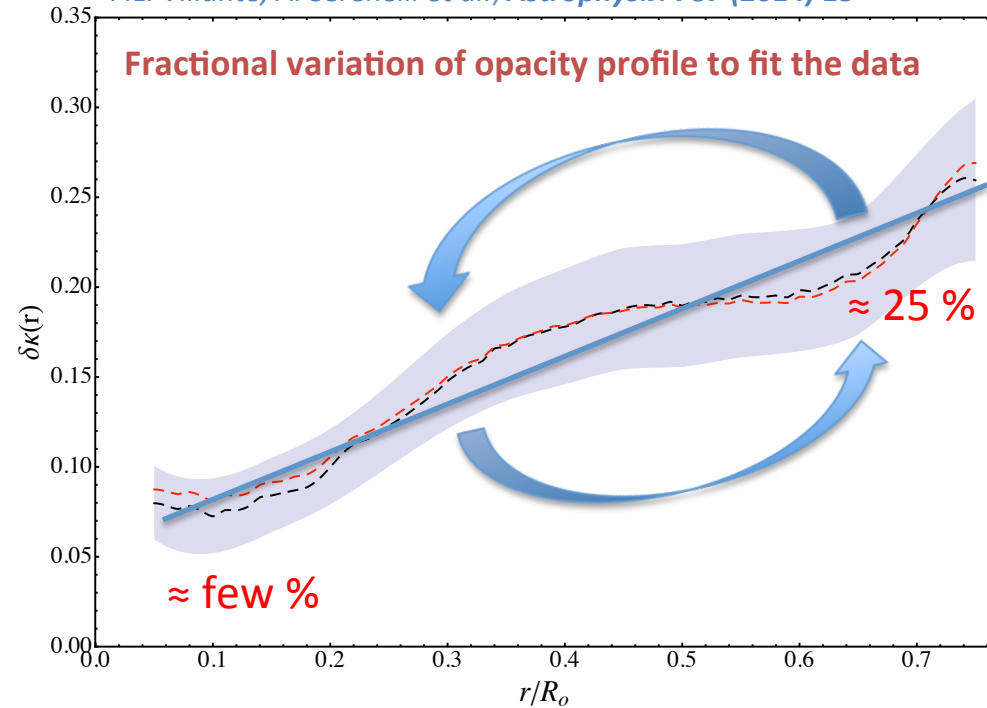
Note that:

- The sound speed and the convective radius determine **the tilt** of $\delta\kappa(r)$ (but not **the scale**)
- The surface helium and the neutrino fluxes determine **the scale** for $\delta\kappa(r)$

F.L. Villante and B. Ricci - Astrophys.J.714:944-959,2010

F.L. Villante – Astrophys.J.724:98-110,2010

F.L. Villante, A. Serenelli et al., Astrophys.J. 787 (2014) 13



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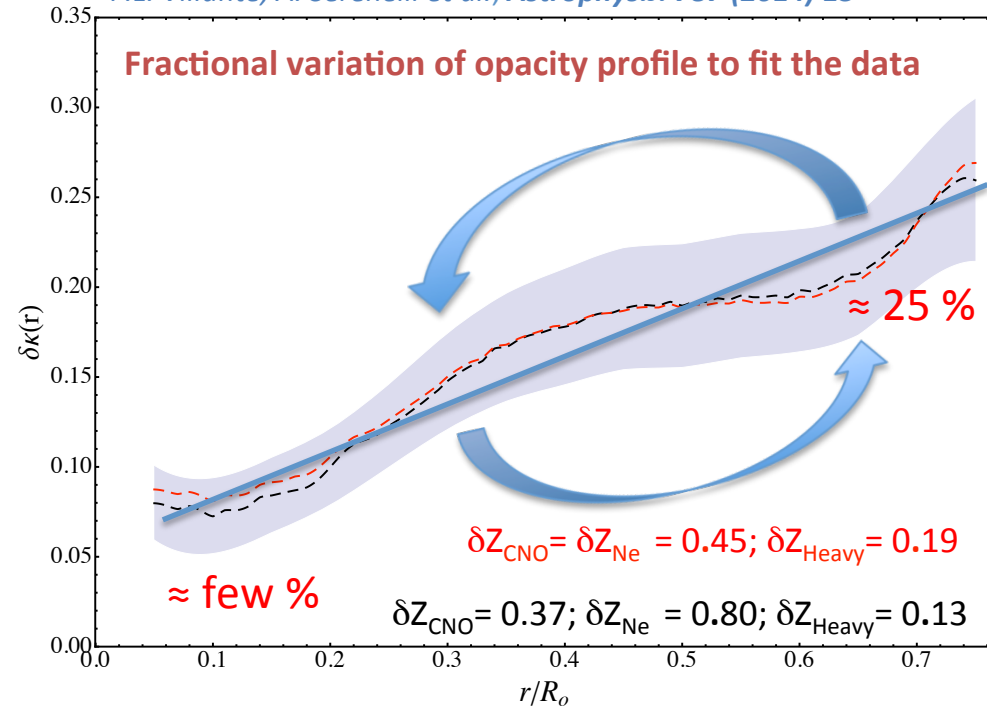
Note that:

- ✓ Opacity (not composition) is directly constrained by present obs. data.
- ✓ The required variations are too large wrt uncertainties (\approx few %)
- ✓ Different admixtures $\{\delta z_i\}$ can reproduce (equally well) the required $\delta\kappa(r)$;

F.L. Villante and B. Ricci - *Astrophys.J.* 714:944-959,2010

F.L. Villante – *Astrophys.J.* 724:98-110,2010

F.L. Villante, A. Serenelli et al., *Astrophys.J.* 787 (2014) 13

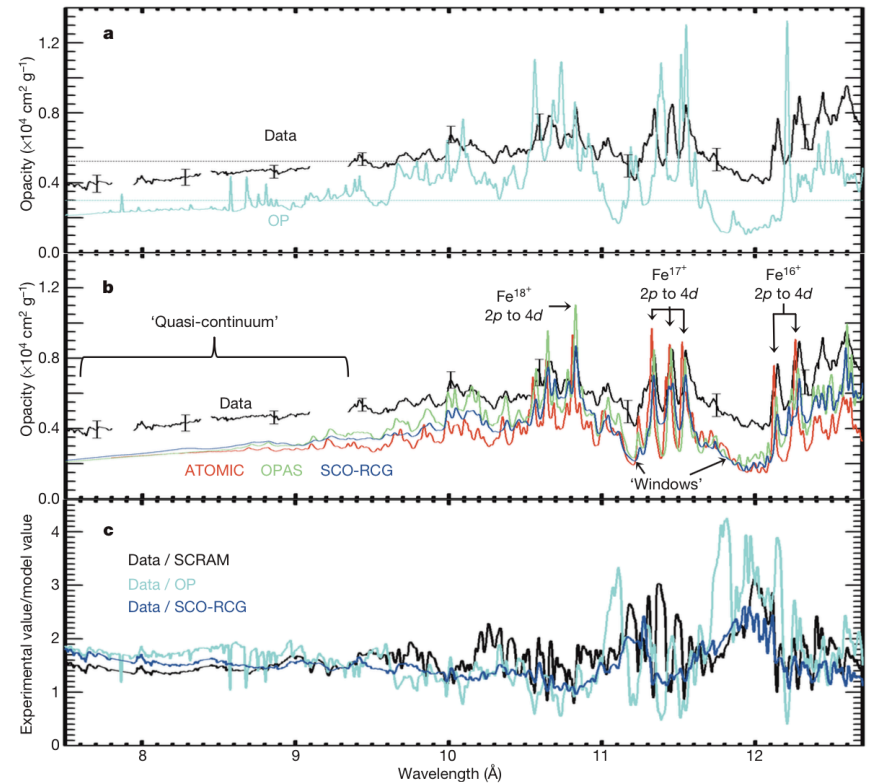


Wrong opacity?

Bailey et al., Nature 2015

(Very) recent progress:

- Opacity is being measured at stellar interiors conditions (see [Bailey et al., Nature 2015](#));
- Monochromatic opacity is higher than expected for iron (up to a factor 2);
- Total opacity of solar plasma (integrated over the wavelength and summed over the composition), is increased by about 7%



Wrong chemical evolution?

Helioseismic observables and neutrino fluxes are sensitive to **the metallicity of the radiative core of the Sun.**

The observations determine **the chemical composition of the convective envelope** (2-3% of the solar mass).

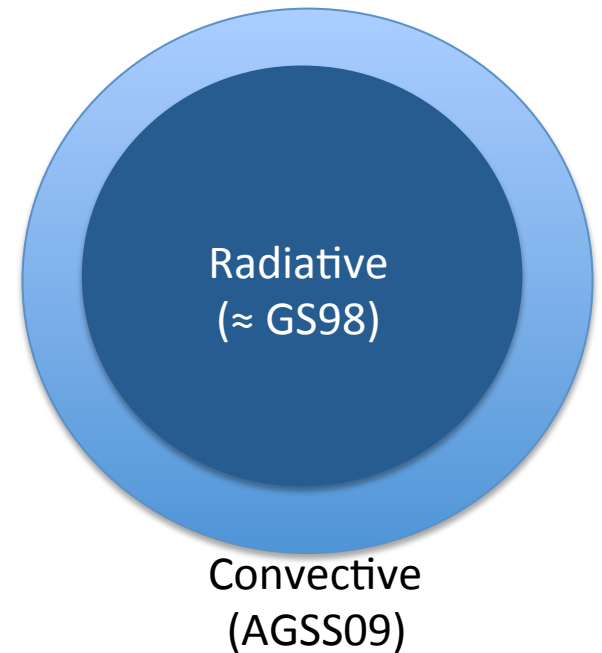
Difference between AGSS09 and GS98 correspond to $\approx 40M_{\oplus}$ of metal, when integrated over the Sun's convective zone.

Could this difference be accounted in non standard chemical evolution scenarios (e.g. by accretion of material with non standard composition)?

See A. Serenelli et al. – ApJ 2011

This is a well posed and extremely important question but ...

... no satisfactory solutions have been proposed up to now, in my opinion



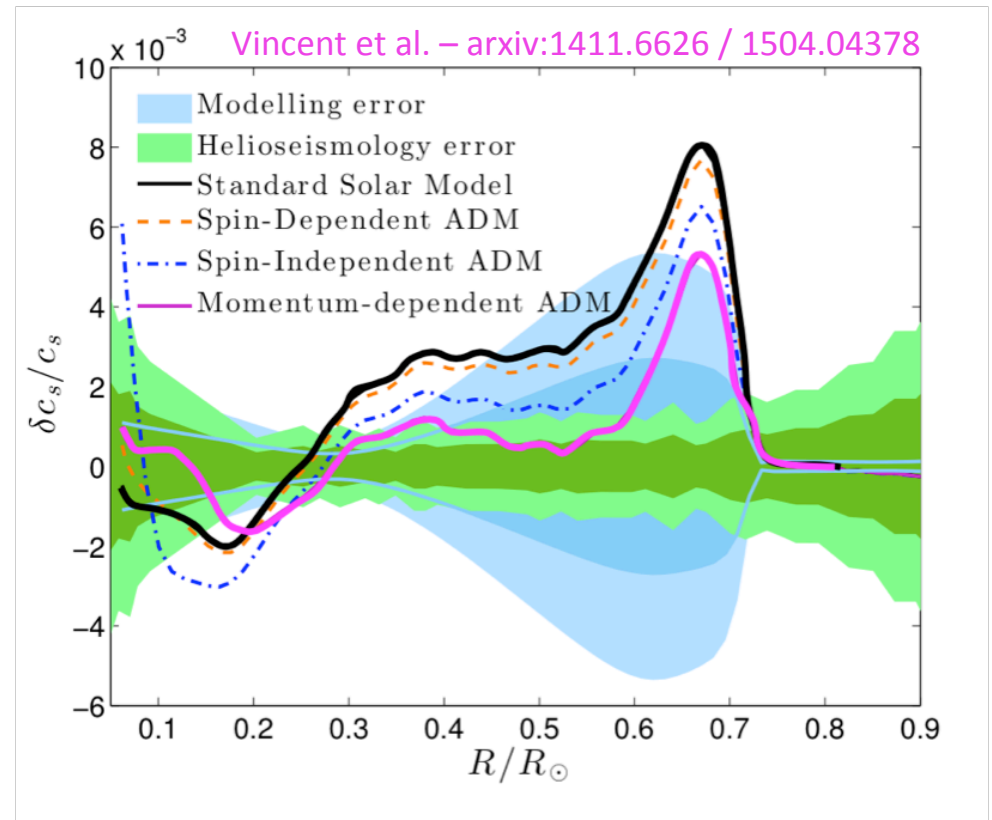
Asymmetric DM

DM accumulation in the solar core:

- Additional energy transport;
- **Reduction** of the “effective opacity”;
- Modification of temperature profile;

Agreement with helioseismic data can be improved. However:

- DM accumulation do not provide the optimal opacity profile;
- Potential tension with neutrino fluxes and surface helium;
- **Caveat:** DM evaporation not accounted for (relevant for few GeV masses)



$$\sigma = \sigma_0 \left(\frac{q}{q_0} \right)^2 \quad \begin{cases} m_{\chi} = 3 \text{ GeV} \\ \sigma_0 = 10^{-37} \text{ cm}^2 \\ q_0 = 40 \text{ MeV} \end{cases}$$

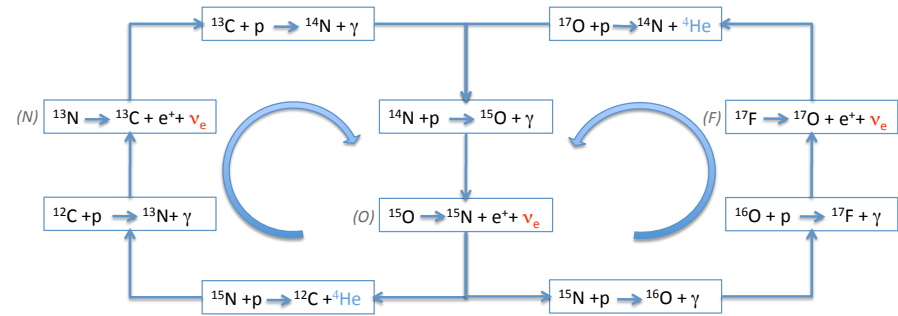
CNO neutrinos

CNO neutrinos allows to determine directly the C+N abundance in the solar core:

$$1 + \delta\Phi_\nu = (1 + \delta X_{\text{CN}}) \left[1 + \int dr K_\nu(r) \delta\kappa(r) \right]$$

$$X_{\text{CN}} \equiv X_{\text{C}}/12 + X_{\text{N}}/14$$

Total number of catalysts for CN-cycle



Determines the central temperature

Constrained by Φ_B and Φ_{Be}

At present, we only have a loose upper limit on CNO neutrino fluxes:

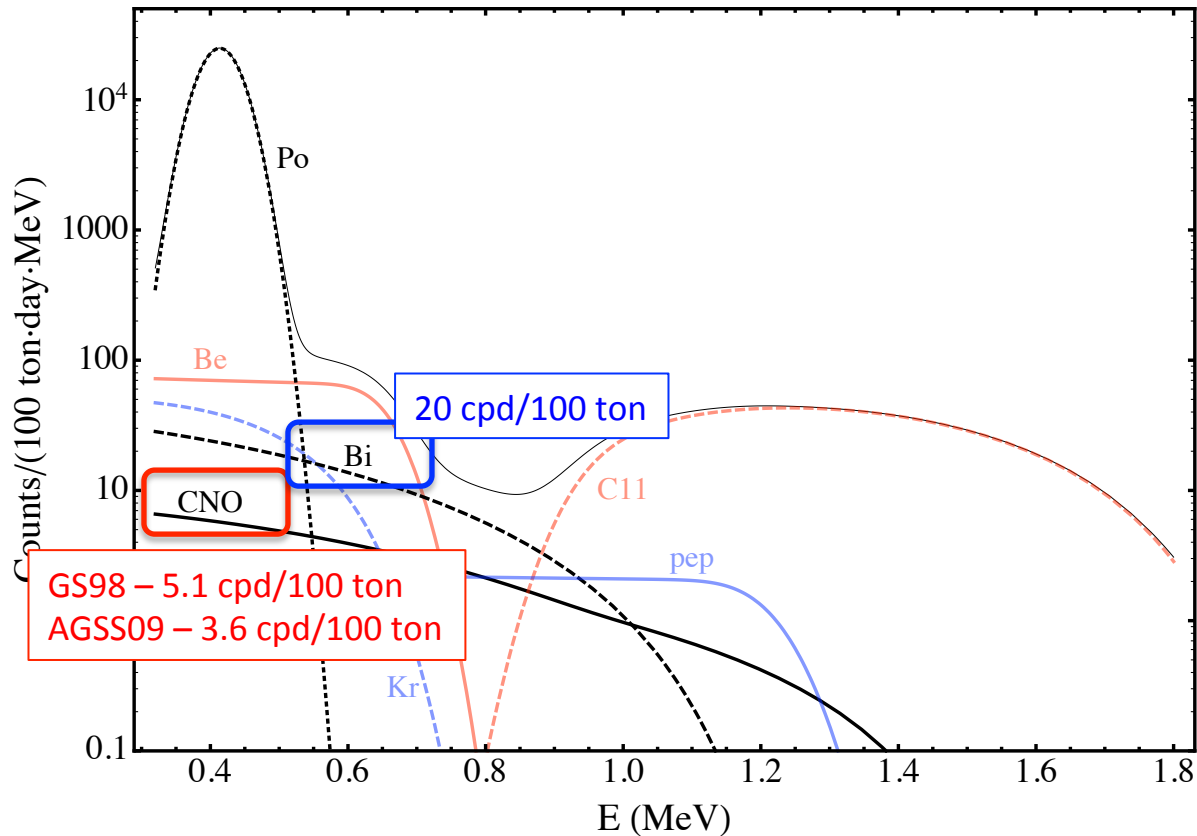
ν flux	GS98	AGSS09	Solar
^{13}N ($10^8 \text{ cm}^{-2} \text{ s}^{-1}$)	2.96(1 ± 0.14)	2.17(1 ± 0.14)	≤ 6.7
^{15}O ($10^8 \text{ cm}^{-2} \text{ s}^{-1}$)	2.23(1 ± 0.15)	1.56(1 ± 0.15)	≤ 3.3
^{17}F ($10^6 \text{ cm}^{-2} \text{ s}^{-1}$)	5.52(1 ± 0.17)	3.04(1 ± 0.16)	≤ 59

Is it possible to observe CNO neutrinos in LS?

The detection of CNO neutrinos is very difficult:

- Low energy neutrinos → endpoint at about 1.5 MeV
- Continuous spectra → do not produce recognizable features in the data.
- Limited by the background produced by beta decay of ^{210}Bi .

Event spectrum in ultrapure liquid scintillators (Borexino-like)



Will it be possible to detect CNO neutrino?

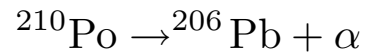
Very difficult, in practice. Not impossible, in principle

F.L. Villante et al., Phys.Lett. B701 (2011) 336

Determining ^{210}Bi with the help of ^{210}Po ?

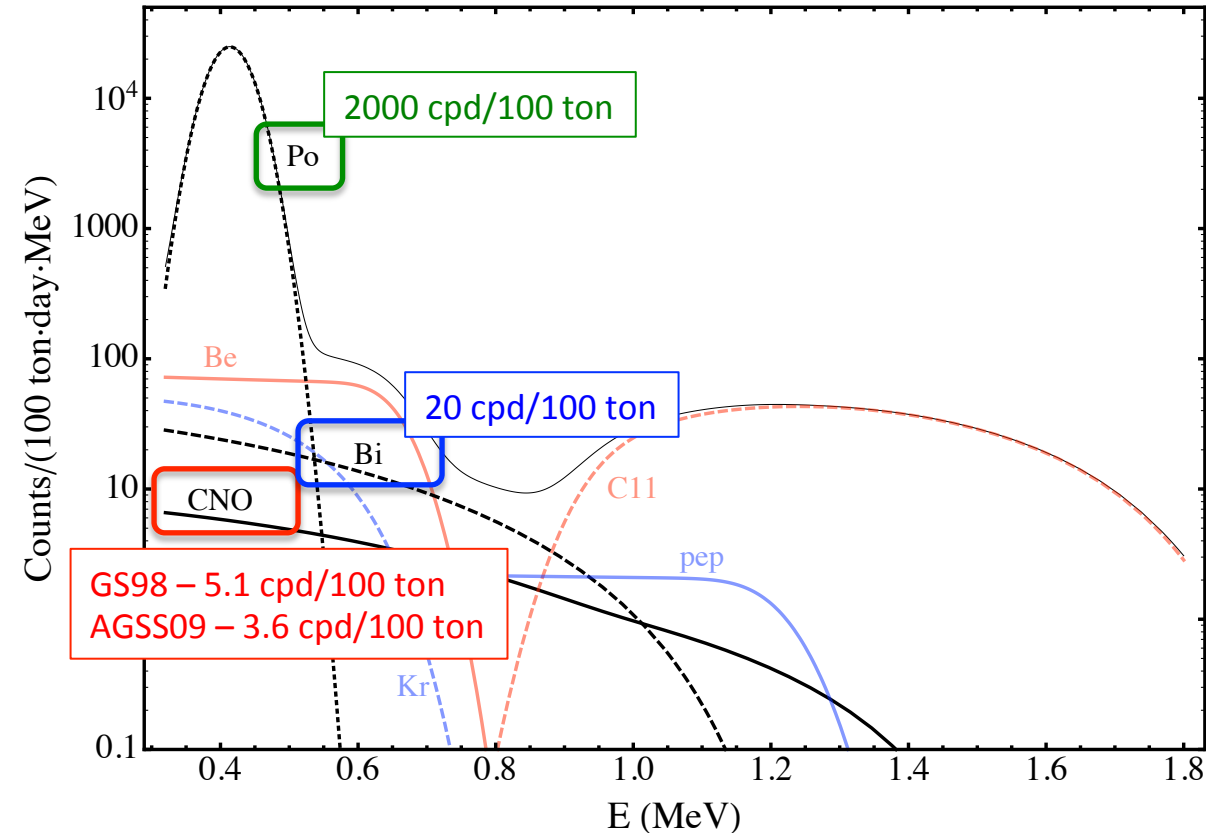


$$\tau_{\text{Bi}} = 7.232 \text{ d}$$



$$\tau_{\text{Po}} = 199.634 \text{ d}$$

Event spectrum in ultrapure liquid scintillators



*F.L. Villante et al. - Phys.Lett.
B701 (2011) 336-341*

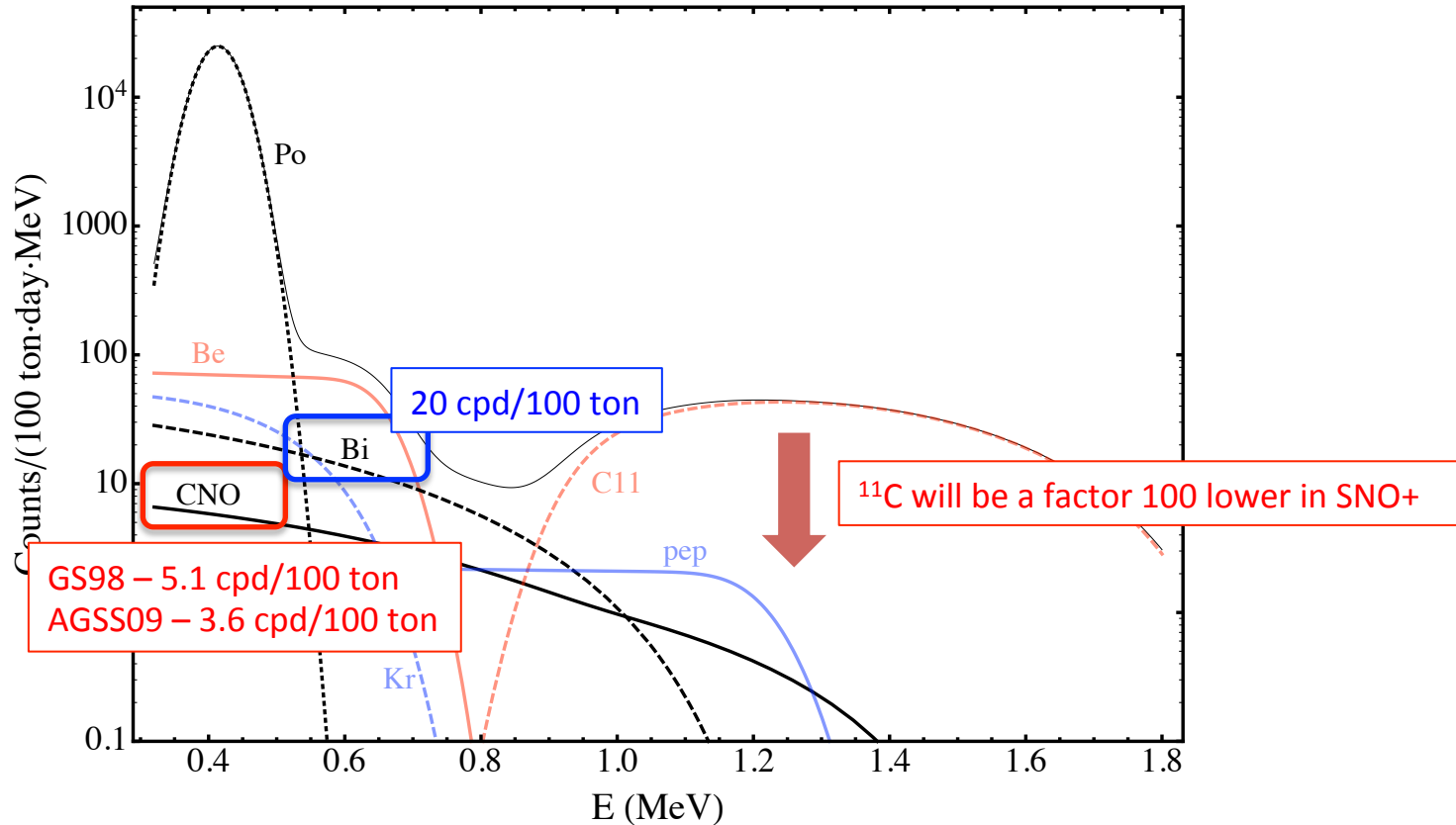
- Deviations from the exponential decay law of ^{210}Po can be used to determine ^{210}Bi
- Borexino already have the potential to probe the CNO neutrino flux ... but the detector should be stable (no convective motions) over long time scales.

How to improve?

Increase the detector depth
Consider larger detectors

→ reduction of cosmogenic ^{11}C background
→ Stat. uncertainties scales as $1/M^{1/2}$
SNO+ (1 kton), LENA (50 kton)

Event spectrum in ultrapure liquid scintillators (Borexino-like)



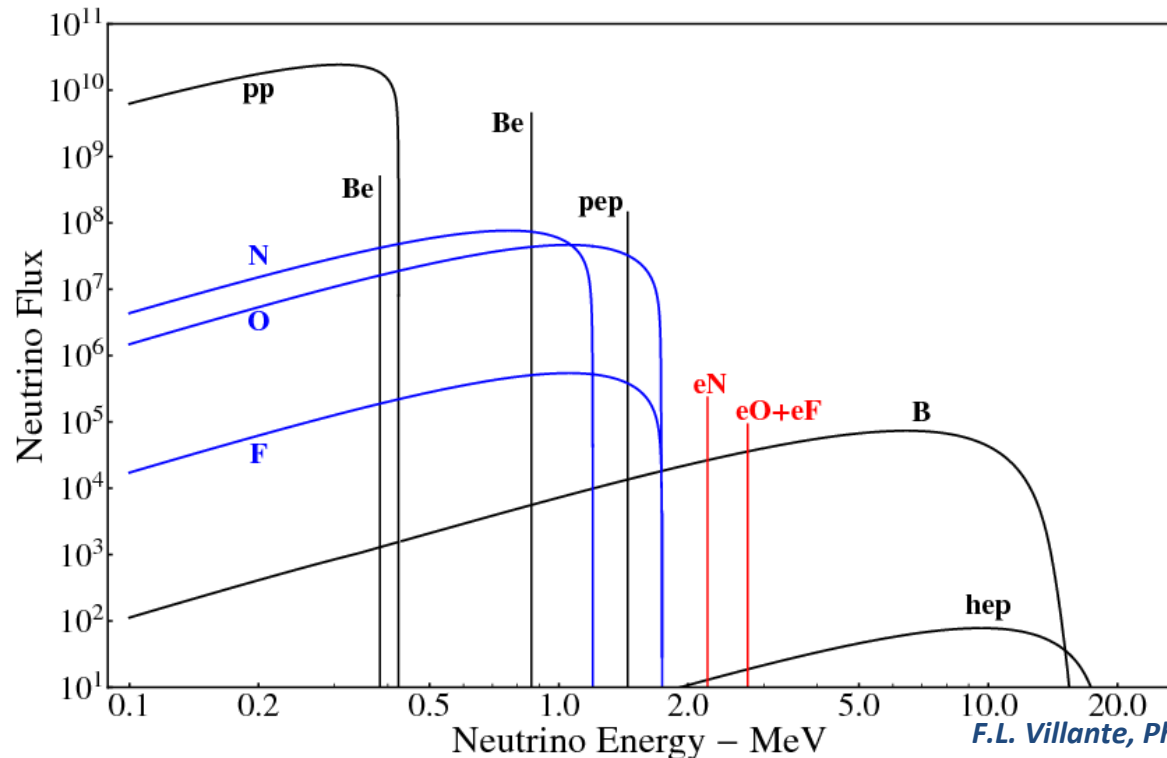
The final accuracy depends, however, on the internal background (^{210}Bi)
Borexino: 20cpd/100 ton → 150 nuclei / 100 ton

ecCNO neutrinos: a challenge for gigantic ultrapure LS

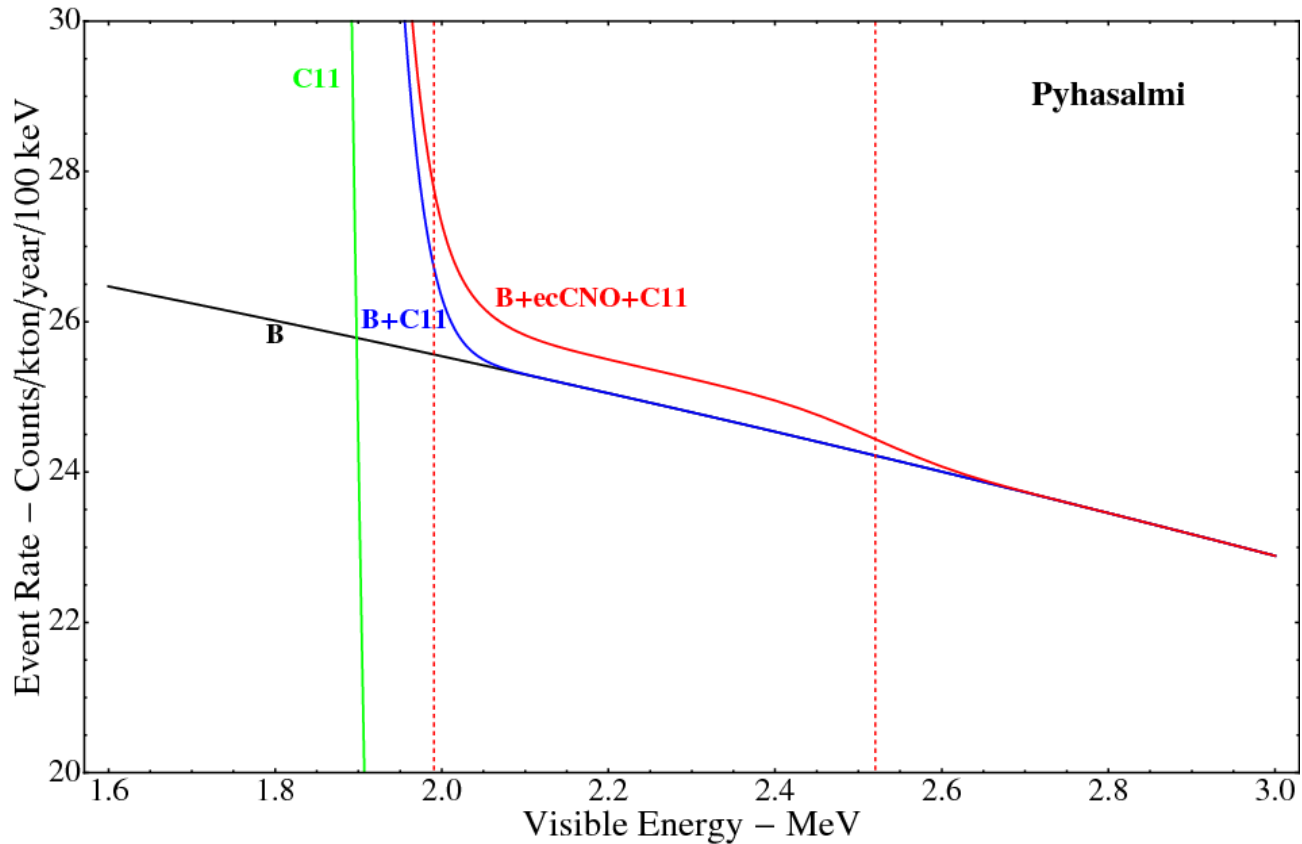
In the CNO cycle, (**monochromatic**) neutrinos are also produced by **electron capture reactions**:



- ecCNO neutrinos probe the **core metallicity** and **Pee in the transition region**.
- fluxes are extremely low: $\Phi_{\text{ecCNO}} \approx (1/20) \Phi_{\text{B}}$



ecCNO neutrinos: expected event rate in LENA



Below 2.5 MeV, the ecCNO neutrino signal is comparable to stat. fluctuations for a detector with an exposure $\epsilon = 10 \text{ kton} \times \text{year}$ or larger.

100 counts / year above 1.8 MeV in 20 kton detector $\rightarrow 3\sigma$ detection in 5 year in LENA

Summary and conclusions

- ✦ Solar neutrino physics is still interesting
- ✦ The **solar composition** problem is open and is potentially pointing at inadequacy in standard solar model paradigm.
- ✦ Borexino opened the way to **pp-neutrino** flux determinations and tested the solar stability. We look forward for future measurements.
- ✦ **CNO neutrino** detection requires careful bkgd evaluation in existing or next future LS detectors and/or new experimental approaches.

Thank you

Standard Solar Models

Stellar structure equations are solved, starting from a ZAMS model to present solar age (we neglect rotation, magnetic fields, etc.):

$$\begin{aligned}\frac{\partial m}{\partial r} &= 4\pi r^2 \rho \\ \frac{\partial P}{\partial r} &= -\frac{G_N m}{r^2} \rho \\ P &= P(\rho, T, X_i) \\ \frac{\partial l}{\partial r} &= 4\pi r^2 \rho \epsilon(\rho, T, X_i) \\ \frac{\partial T}{\partial r} &= -\frac{G_N m T \rho}{r^2 P} \nabla\end{aligned}\quad \nabla = \text{Min}(\nabla_{\text{rad}}, \nabla_{\text{ad}}) \rightarrow \begin{cases} \nabla_{\text{rad}} = \frac{3}{16\pi ac G_N} \frac{\kappa(\rho, T, X_i) l P}{m T^4} \\ \nabla_{\text{ad}} = (d \ln T / d \ln P)_s \simeq 0.4 \end{cases}$$

Chemical evolution driven by nuclear reaction, diffusion and gravitational settling, convection

Standard input physics for equation of states, nuclear reaction rates, opacity, etc.

Free-parameters (**mixing length**, Y_{ini} , Z_{ini}) adjusted to match the observed properties of the Sun (**radius**, **luminosity**, Z/X).

Note that equations are non-linear \rightarrow Iterative method to determine mixing length, Y_{ini} , Z_{ini}

A quantitative analysis of the solar composition problem

Villante et al. 2014

To combine observational infos, we need an estimator that is **non-biased** and that can be used as a **figure-of-merit** for solar models with different composition:

$$\chi^2 = \min_{\{\xi_I\}} \left[\sum_Q \left(\frac{\delta Q - \sum_I \xi_I C_{Q,I}}{U_Q} \right)^2 + \sum_I \xi_I^2 \right] .$$

$$\delta Q = \frac{Q_{\text{obs}} - Q}{Q}$$

Fogli et al. 2002

where:

$$\{\delta Q\} = \{ \delta\Phi_B, \delta\Phi_{Be}, \delta Y_b, \delta R_b; \delta c_1, \delta c_2, \dots, \delta c_{30} \}$$

${}^7\text{Be}$ and ${}^8\text{B}$ neutrino fluxes

Surface helium and convective radius

Sound speed data points (from Basu et al, 2009)

and: $\begin{cases} U_Q & \text{Uncorrelated (observational) errors} \\ C_{Q,I} & \text{Correlated (systematical) uncertainties} \end{cases}$

We consider 18 input parameters:

$\{I\} = \{ \text{opa, age, diffu, lum, } S_{11}, S_{33}, S_{34}, S_{17}, S_{e7}, S_{1,14}, S_{\text{hep}}, \text{C, N, O, Ne, Mg, Si, S, Fe} \}$

Environmental

Nuclear

Composition

The status of the AGSS09 standard solar model

The SSM implementing the AGSS09 composition provides a poor fit of the observational data. By considering $(R_b, Y_b; \Phi_B, \Phi_{Be}; c_1, \dots, c_{30})$, we obtain $\chi^2/\text{d.o.f.} = 72.5/34$ ($\chi^2_{\text{obs}} = 42.9$; $\chi^2_{\text{syst}} = 29.6$)

$$\chi^2 \equiv \chi_{\text{obs}}^2 + \chi_{\text{syst}}^2 = \sum_Q \tilde{X}_Q^2 + \sum_I \tilde{\xi}_I^2$$

$$\bar{\xi}_I \equiv \text{Pulls of systematic}$$

$$\tilde{X}_Q \equiv \frac{\delta Q_{\text{obs}} - \sum_I \tilde{\xi}_I C_{Q,I}}{U_Q}$$

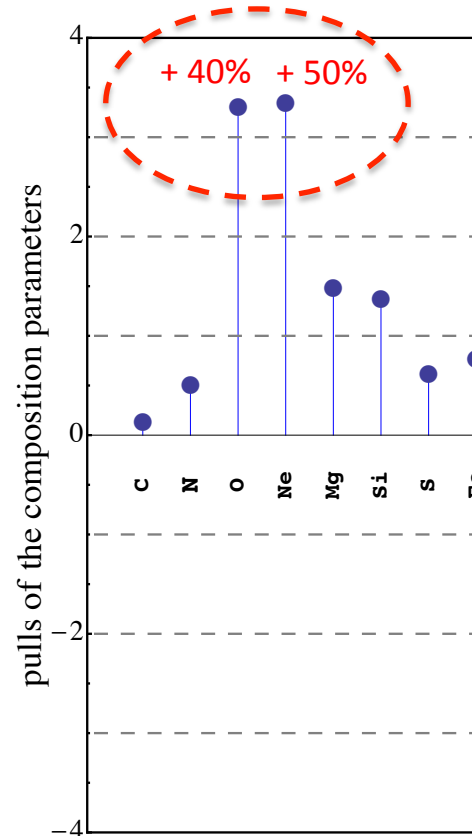
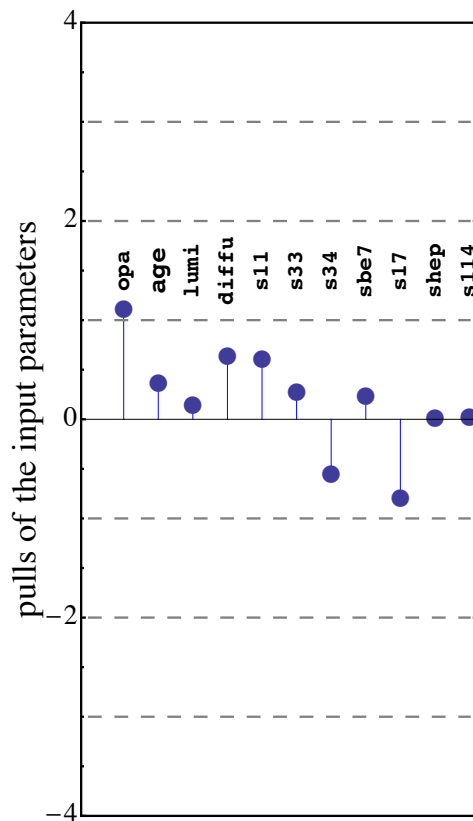
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$$\begin{aligned} \bar{\xi}_I &\equiv \text{Pulls of systematic} \\ \tilde{X}_Q &\equiv \frac{\delta Q_{\text{obs}} - \sum_I \tilde{\xi}_I C_{Q,I}}{U_Q} \end{aligned}$$

The distribution of the pulls of systematics (input for SSM) highlight tensions in the model:



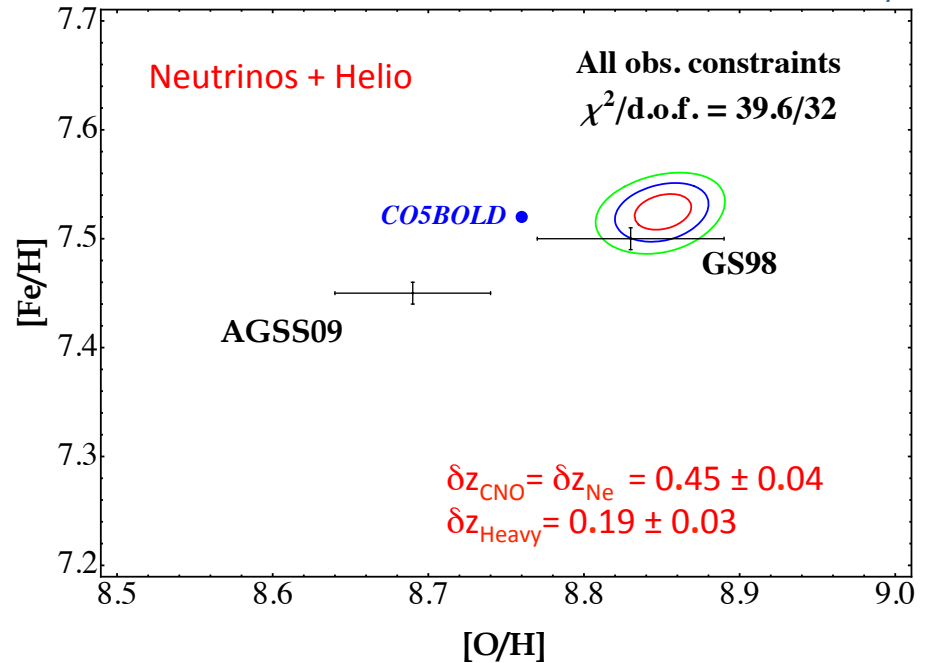
Obs. data requires an increase of the metal abundance of the sun, in particular for light elements (O, Ne).

Wrong surface composition?

We can use helioseismology + neutrinos ($R_b, Y_b; \Phi_B, \Phi_{Be}; c_1, \dots, c_{30}$) to determine the optimal composition (F.L. Villante et al. – ApJ 2014):

- The best-fit abundances are **consistent** at 1σ with **GS98**. The **errors** on the inferred abundances **are smaller** than what is obtained by observational determinations.
- Substantial agreement between the infos provided by the various obs. constraints. The quality of the fit is quite good being $\chi^2/\text{d.o.f.} = 39.6/32$.

Two parameter analysis ($\delta z_{\text{CNO}}; \delta z_{\text{Heavy}}$)



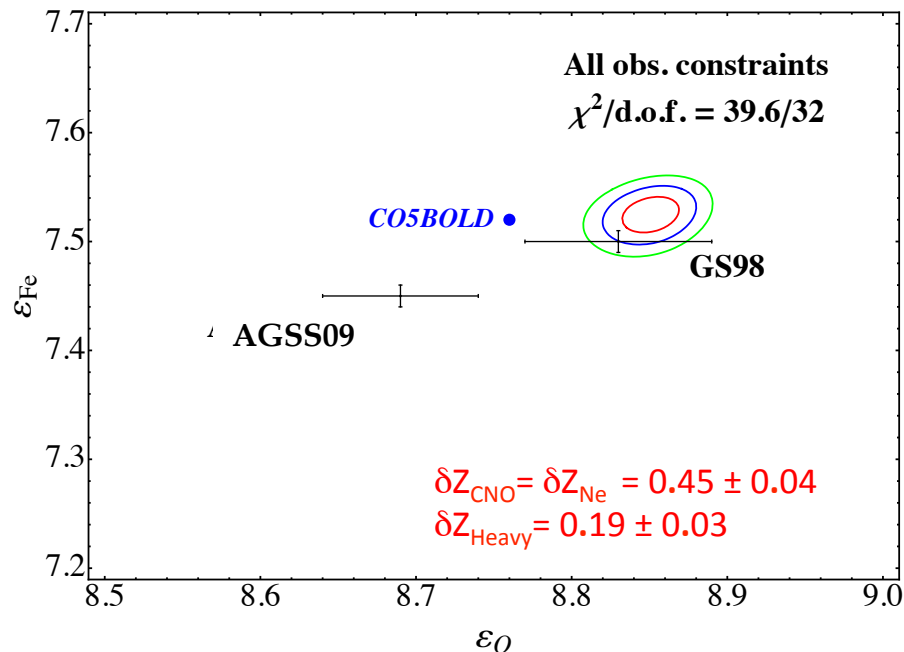
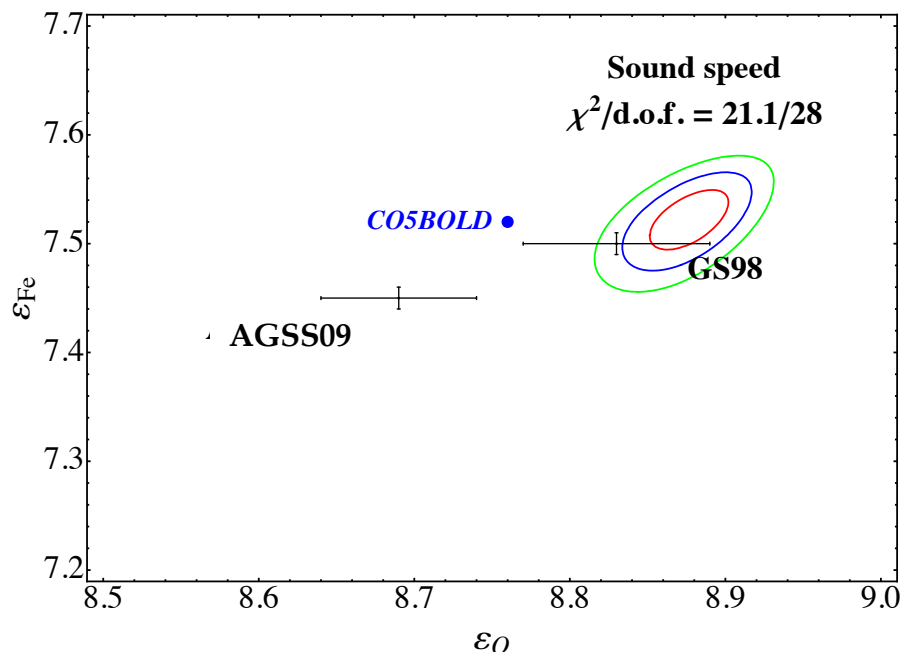
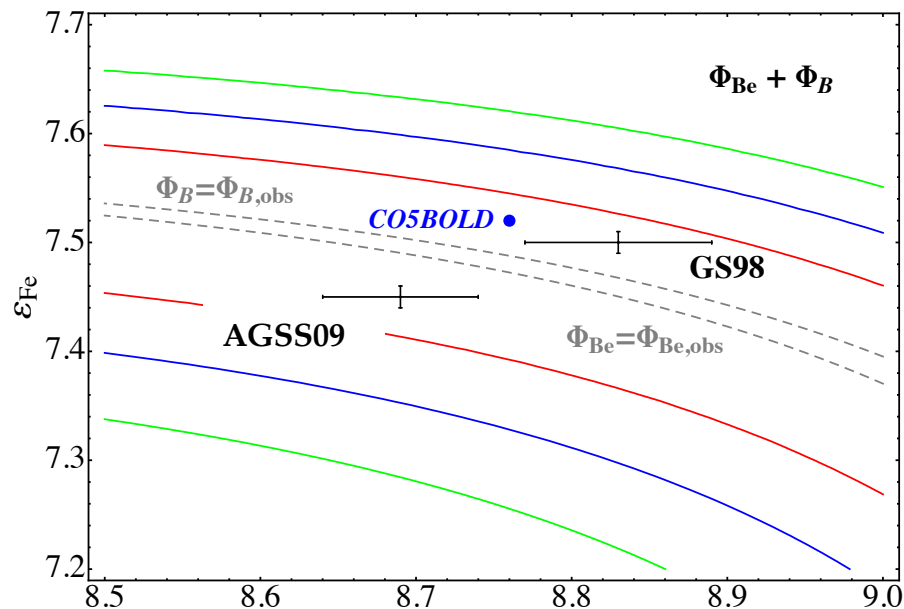
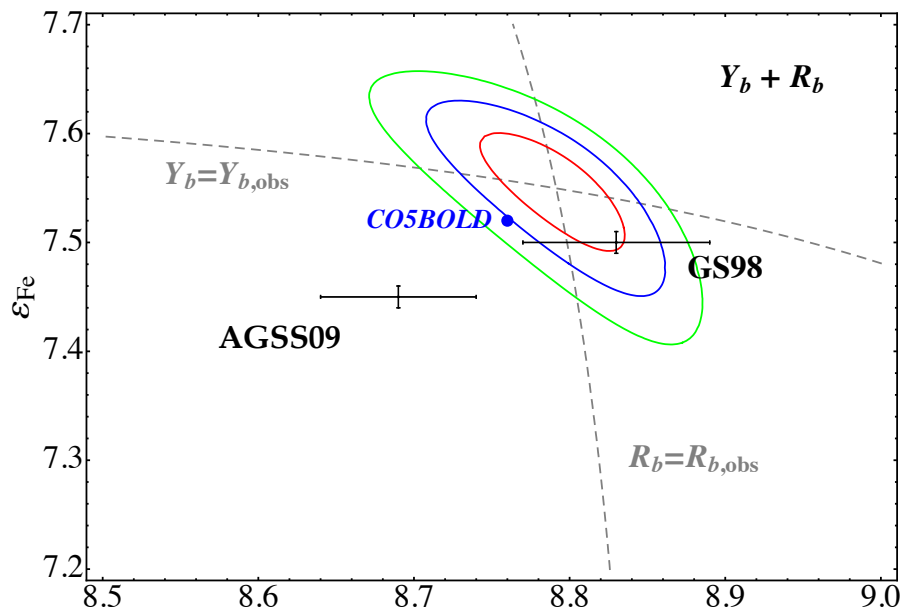
$$[\text{O}/\text{H}] = \overline{[\text{O}/\text{H}]} + \log(1 + \delta z_{\text{CNO}})$$

$$[\text{Fe}/\text{H}] = \overline{[\text{Fe}/\text{H}]} + \log(1 + \delta z_{\text{Heavy}})$$

However, data are not effective in constraining composition **in more realistic scenarios**:

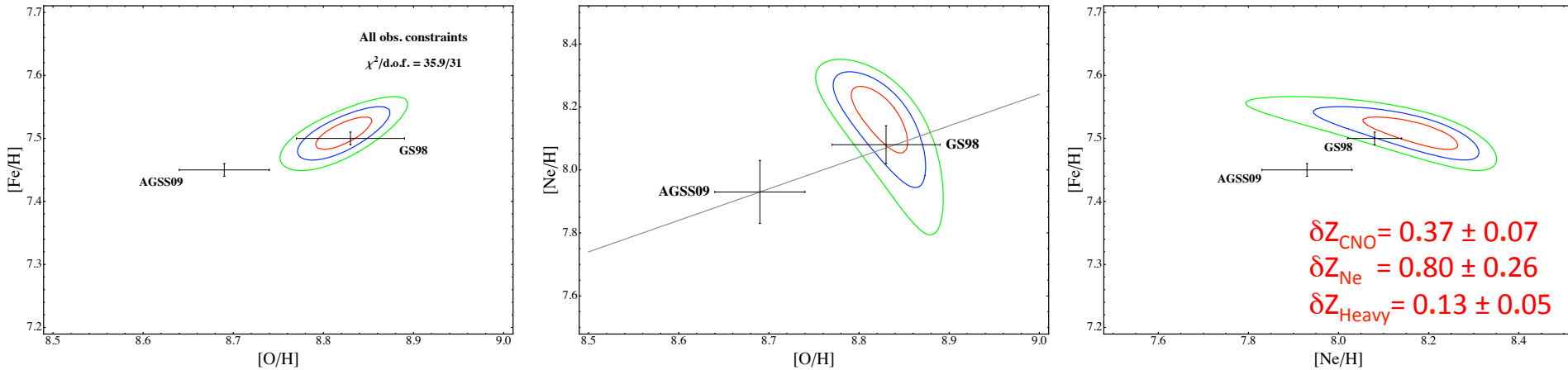
- different admixtures $\{\delta z_i\}$ can reproduce (equally well) the required $\delta k(r)$;
- no real constraints on the Ne/O ratio

Two parameter analysis ($\delta Z_{\text{CNO}} = \delta Z_{\text{Ne}} ; \delta Z_{\text{Heavy}}$)



Three parameter analysis (δZ_{CNO} ; δZ_{Ne} ; δZ_{Heavy})

Prior: Neon-to-oxygen ratio forced at the AGSS09 value with 30% accuracy



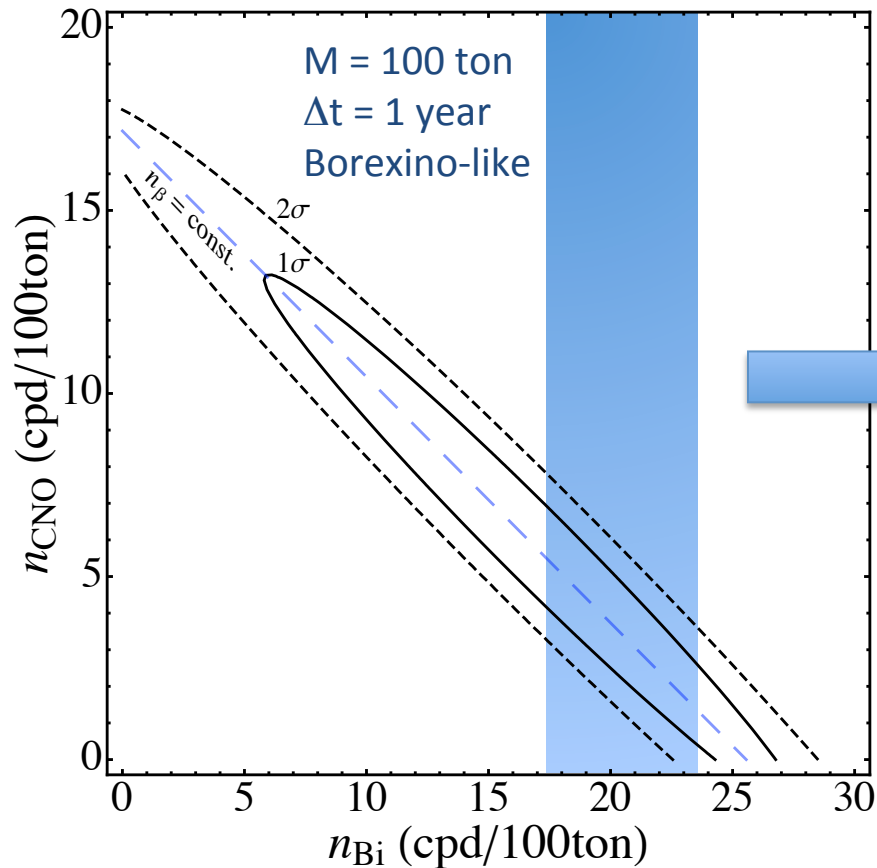
GS98 still favored by observational data but:

- errors in the inferred abundances larger than before;
- degeneracies appear among the various δZ_i ;
- obs.data do not effectively constrain the Ne/O ratio (we recover the prior).

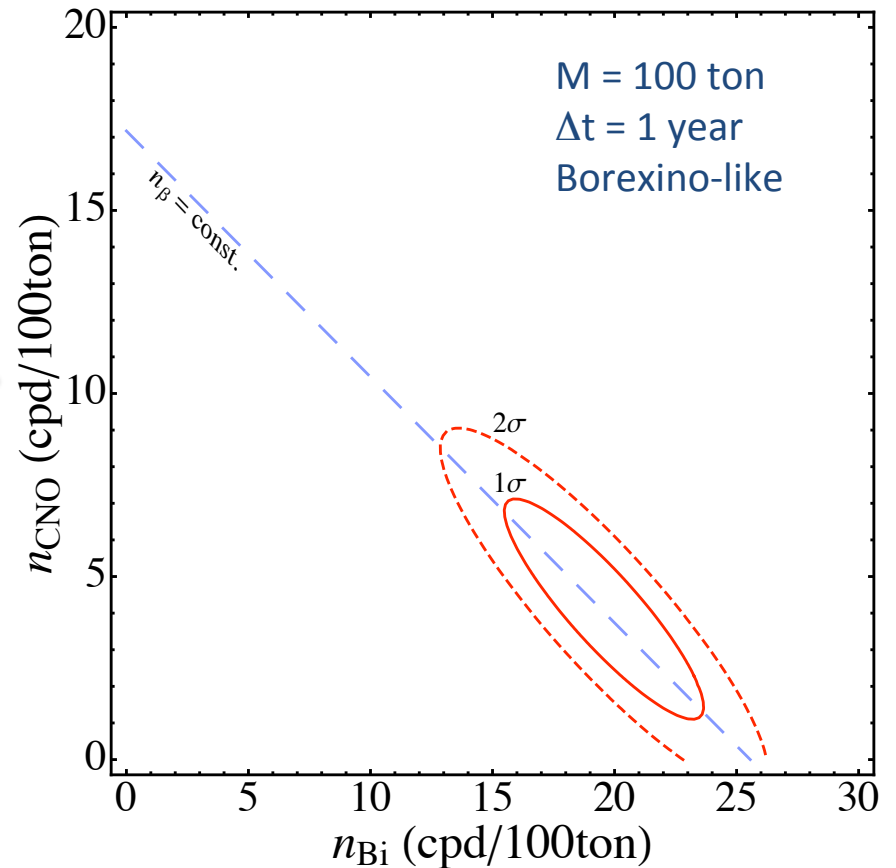
Borexino, already has the potential to probe the CNO neutrino flux

Future Kton-scale detectors (e.g. SNO+) will be able to start discriminating between high and low metallicity solar models (uncertainties scales as $1/M^{1/2}$)

Fit to simulated data (energy)



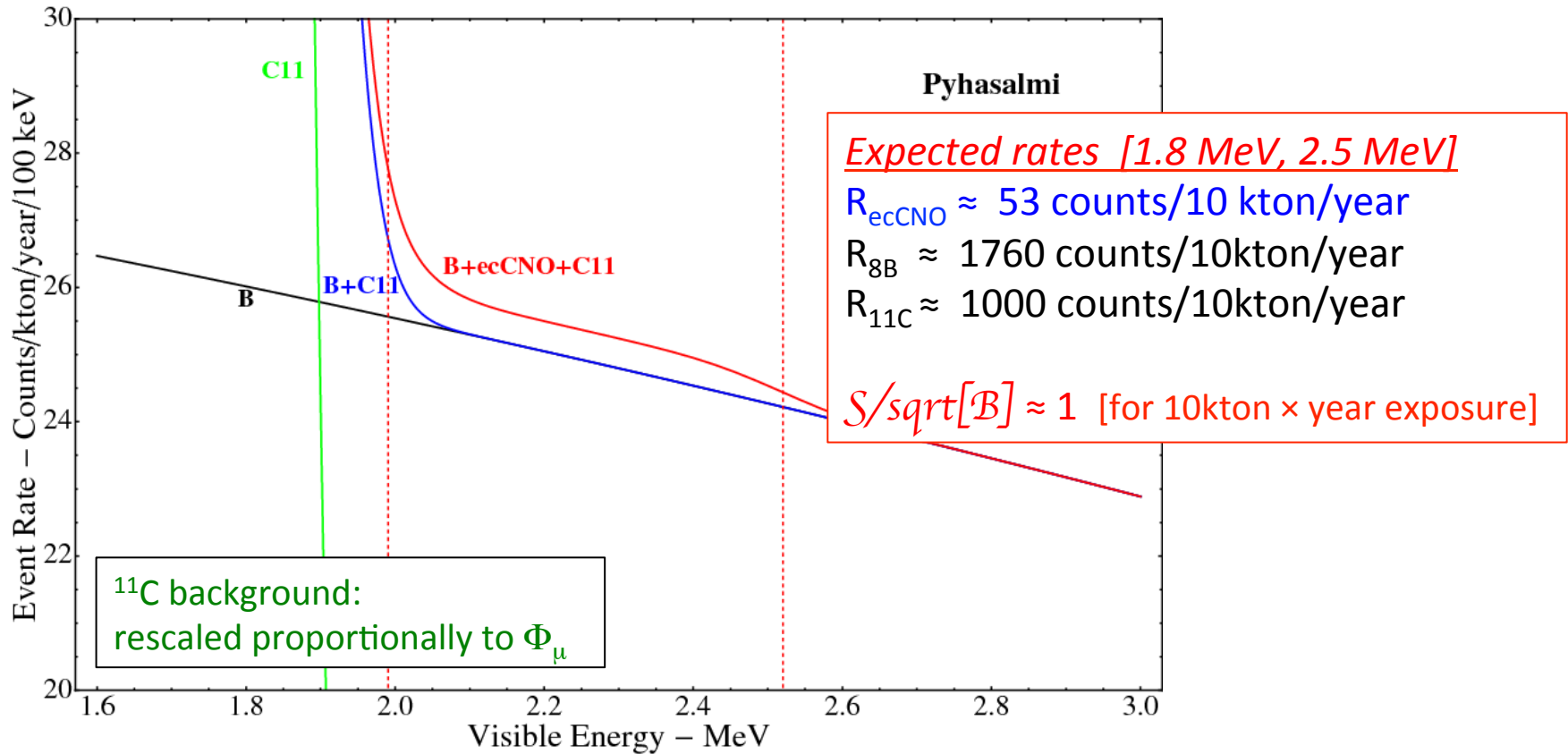
Fit to simulated data (energy and time)



Expected rates in Liquid Scintillators

Additional background sources:

- **Intrinsic:** negligible/tagged (with Borexino Phase-I radio-purity levels);
- **External:** reduced by self-shielding (Fid. mass reduced from 50 to ≈ 20 kton in LENA);
- **Cosmogenic:** ^{11}C overlap with the observation window.



Signal comparable to stat. fluctuations for exposures 10 kton \times year or larger.

100 counts / year above 1.8 MeV in 20 kton detector $\rightarrow 3\sigma$ detection in 5 year in LENA

Significance of CNO measurement in LENA

From Michael Wurm talk @ NNN14

Assuming constraints of ^{210}Bi rate at the 1% level:

Time	CNO prec (stat.)	PEP prec. (stat.)	CNO significance
1 y	10.7 %	2.5 %	4.2 σ (avg)
2 y	9.2 %	1.9 %	5.5 σ (avg)
3 y	8.2 %	1.7 %	6.5 σ (avg)
4 y	7.5 %	1.6 %	> 5 σ (99% prob.)
5 y	7.0 %	1.4 %	> 5 σ (99% prob.)
10 y	5.6 %	1.1 %	> 5 σ (99% prob.)

Assuming no constraints of ^{210}Bi rate:

Time	CNO prec (stat.)	PEP prec. (stat.)	CNO significance
1 y	22.7 %	4.3 %	0.7 σ (avg)
2 y	16.0 %	3.0 %	1.8 σ (avg)
3 y	13.1 %	2.5 %	2.8 σ (avg)
4 y	11.3 %	2.2 %	3.7 σ (avg)
5 y	10.1 %	1.9 %	4.5 σ (avg)
10 y	7.2 %	1.4 %	8.1 σ (avg)

In the future ... Advanced Scintillator Detector Concept (ASDC)

It combines:

- Water based Liquid Scintillators (WbLS)
- High efficiency and ultra fast photosensor
- Deep underground location

“Salty” WbLS \rightarrow doped (1% by mass) with ${}^7\text{Li}$
CC detection of ν_e on ${}^7\text{Li}$ enhances spectral separation

30-100 kton scale detector
Cherenkov + Scintillation
100pe/MeV

